

# Feature Indexing

COMP 388-002/488-002 Biometrics

**Daniel Moreira**

Fall 2023



**LOYOLA**  
UNIVERSITY CHICAGO

# Today you will...

*Get to know*

Methods of feature indexing for  
biometric identification.

# Today's attendance

**Please fill out the form**

<https://forms.gle/sjQKGKyMH7ogmPNa7>



# What is Biometrics?



**7 billion people**

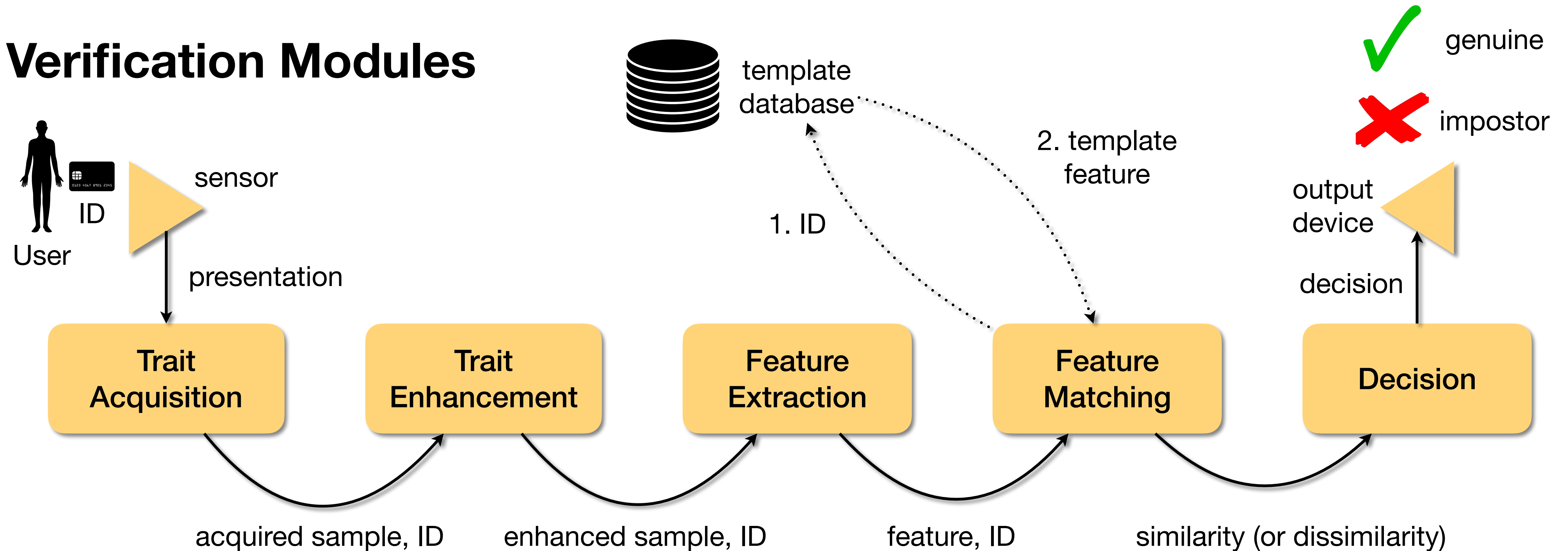
Who is this person? (*Identification*)

Is this person Jane Doe? (*Verification*)

Biometrics aims at ***identifying*** or ***verifying*** the claimed or denied identity of an individual based on their *physical, chemical or behavioral* traits.

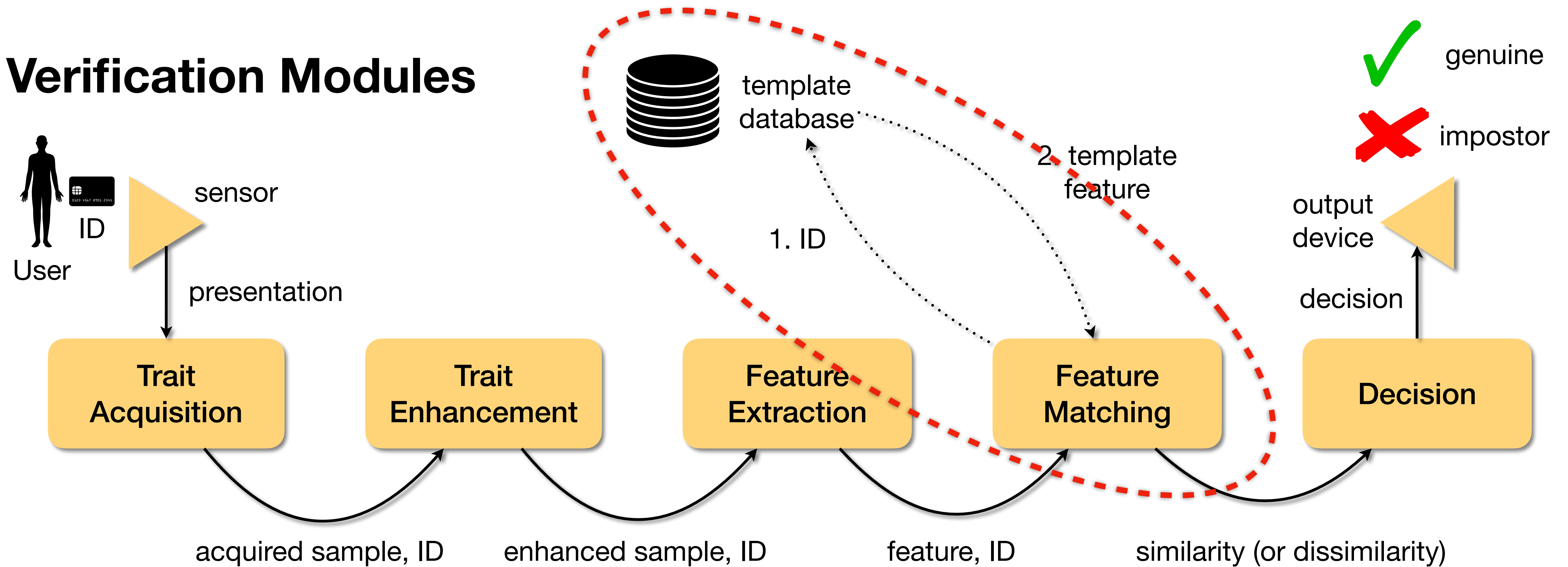
# Biometric Systems

## Verification Modules



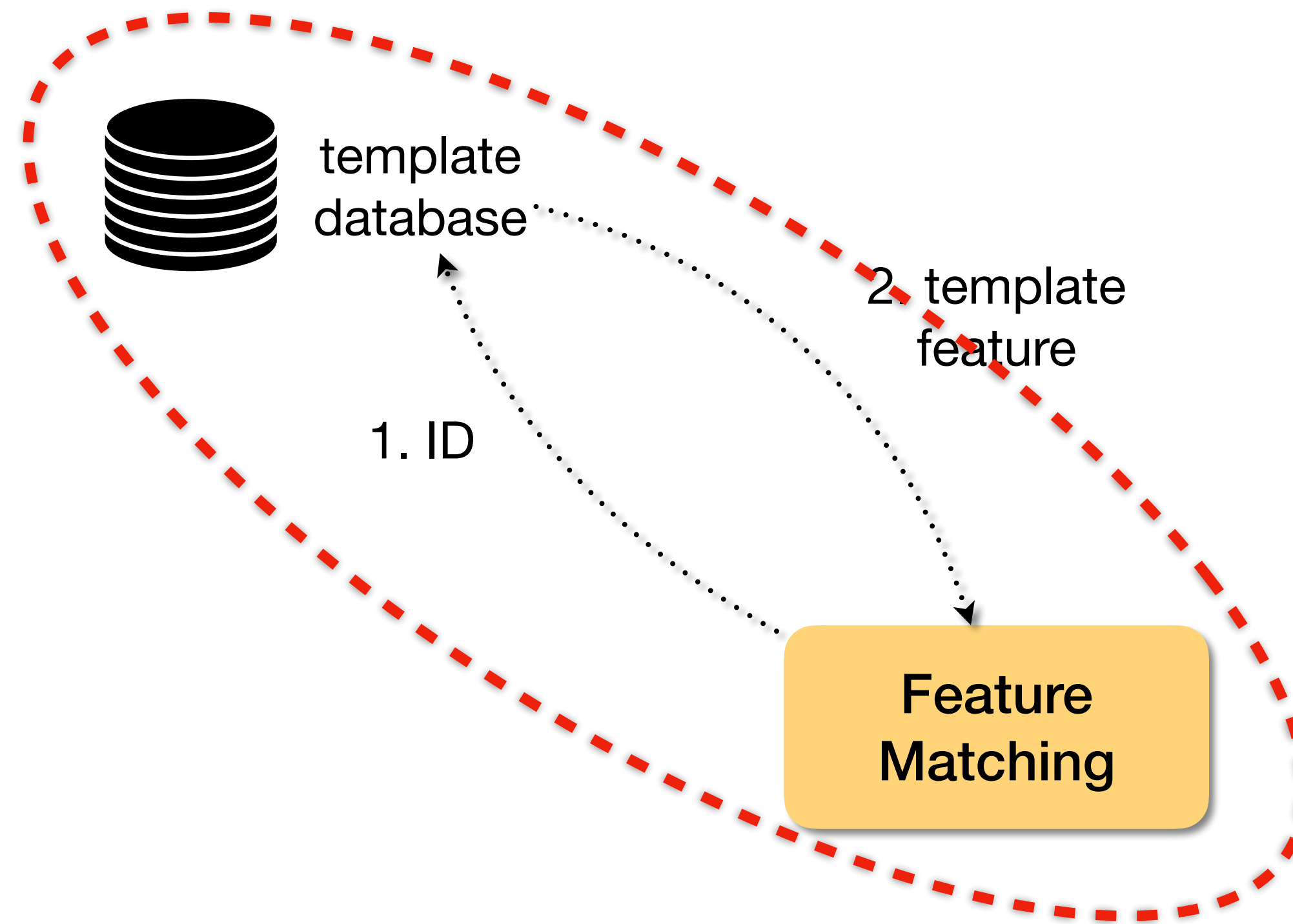
# Biometric Systems

## Verification Modules



# Biometric Verification

No need for complex feature indexing.

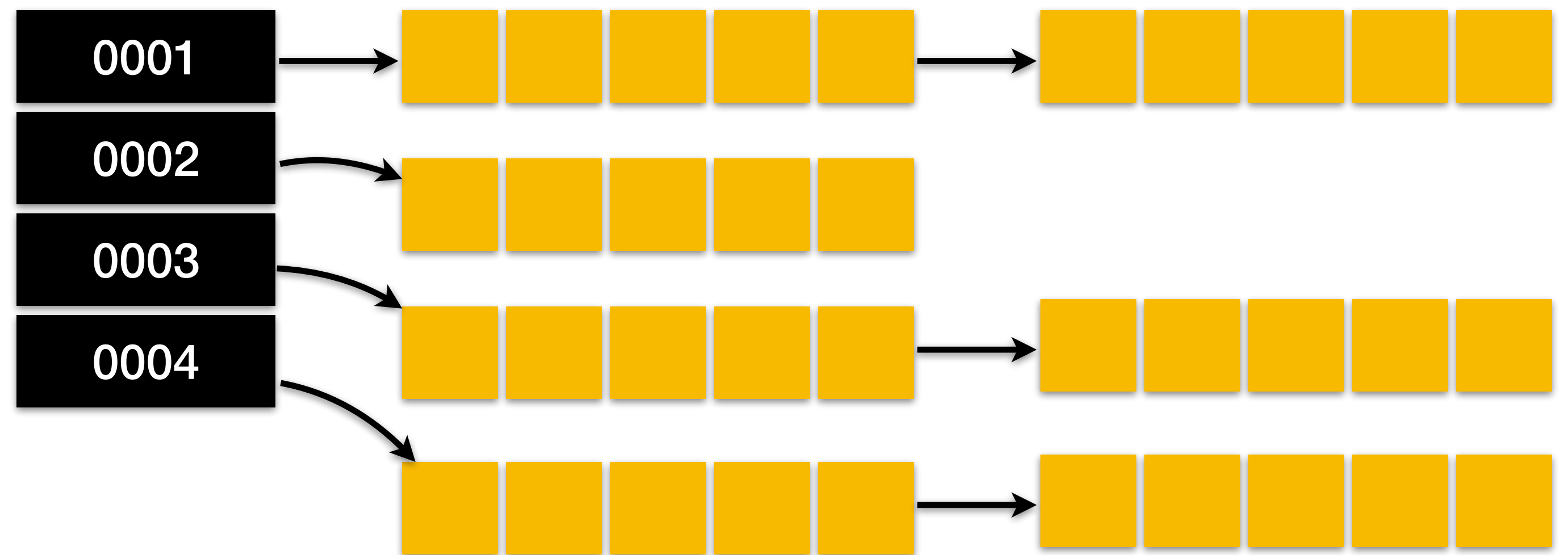


# Biometric Verification

No need for complex feature indexing.

Use unique person's ID as index (or hash function input).

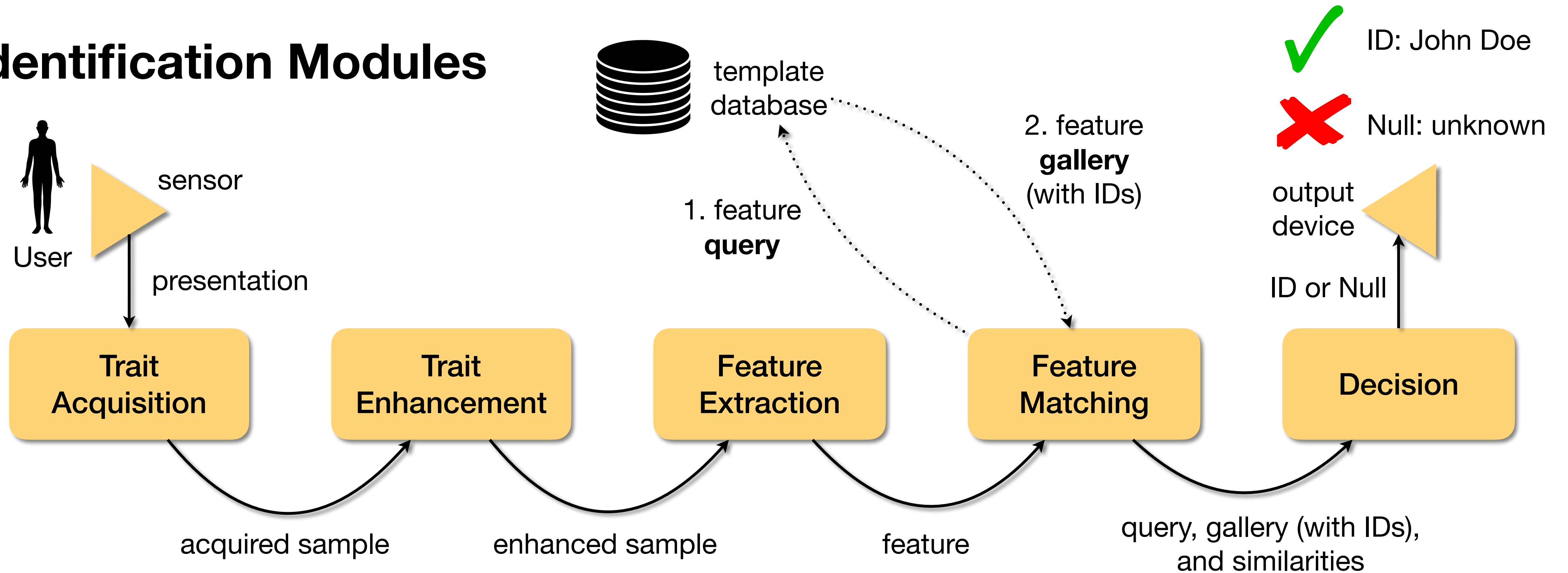
Retrieval of features in constant time.





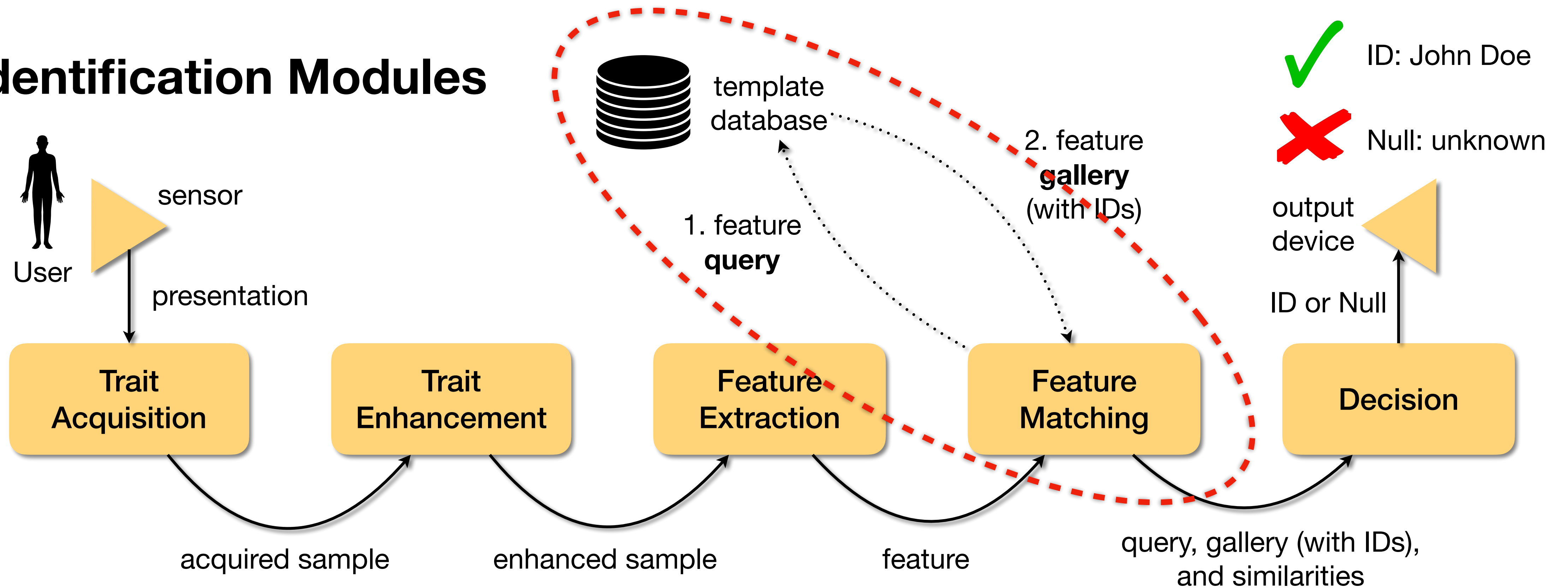
# Biometric Systems

## Identification Modules



# Biometric Systems

## Identification Modules

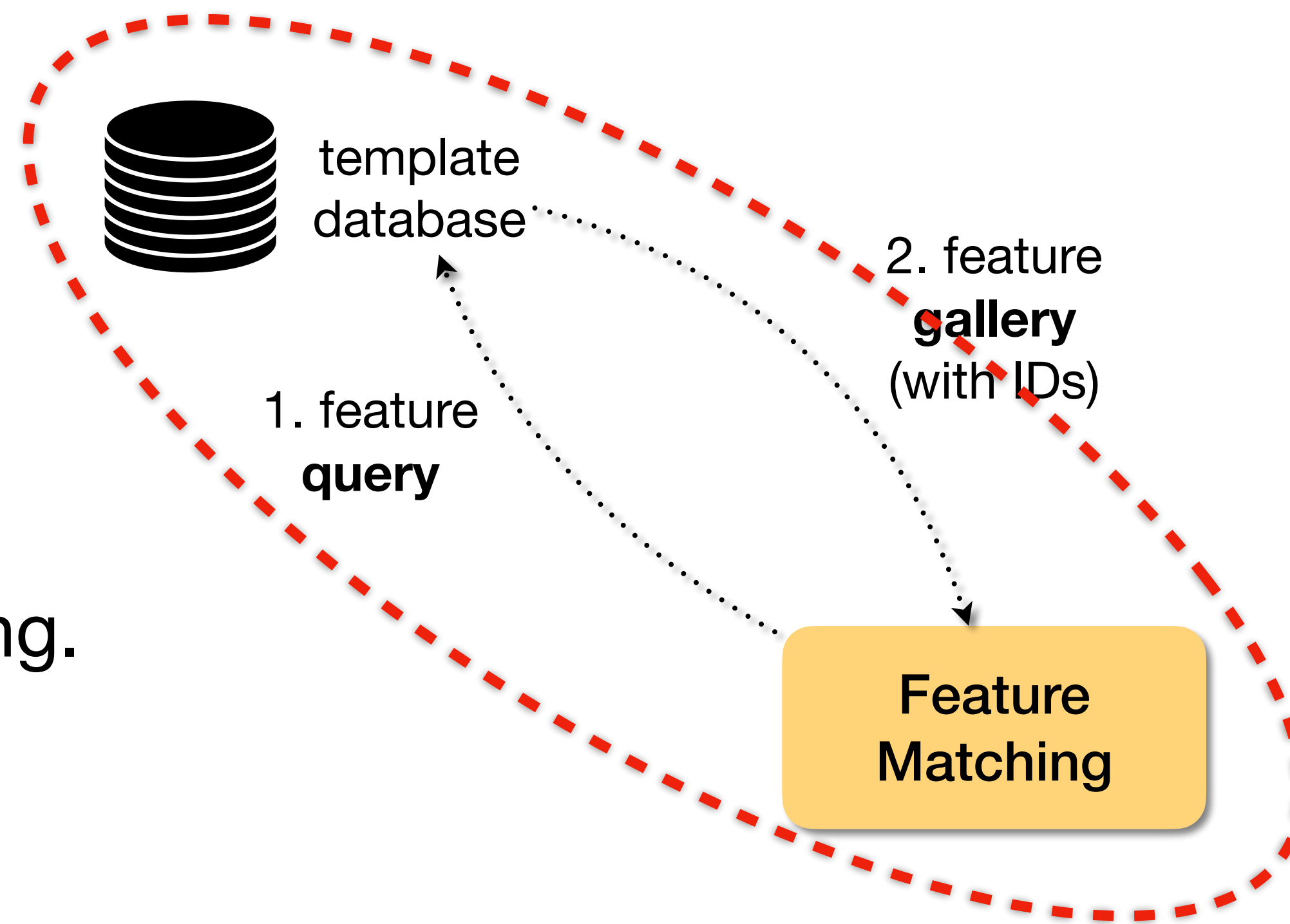


# Biometric Identification

How to retrieve  $k$ -nearest features to compose gallery?

Need for more complex indexing.

Retrieval of features as quick as possible.



# Biometric Identification

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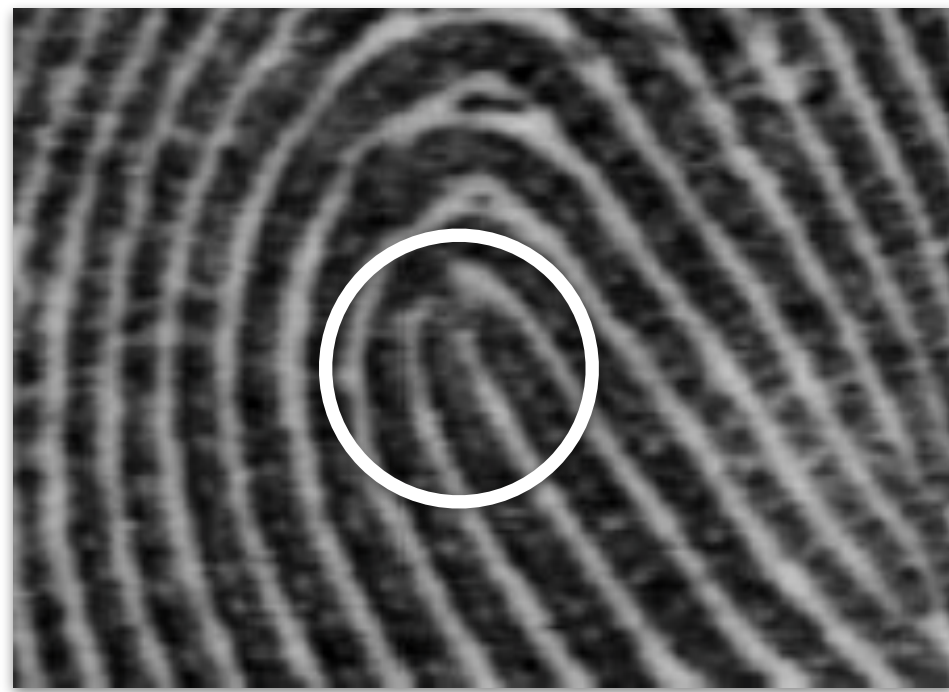
Retrieval of features as quick as possible.



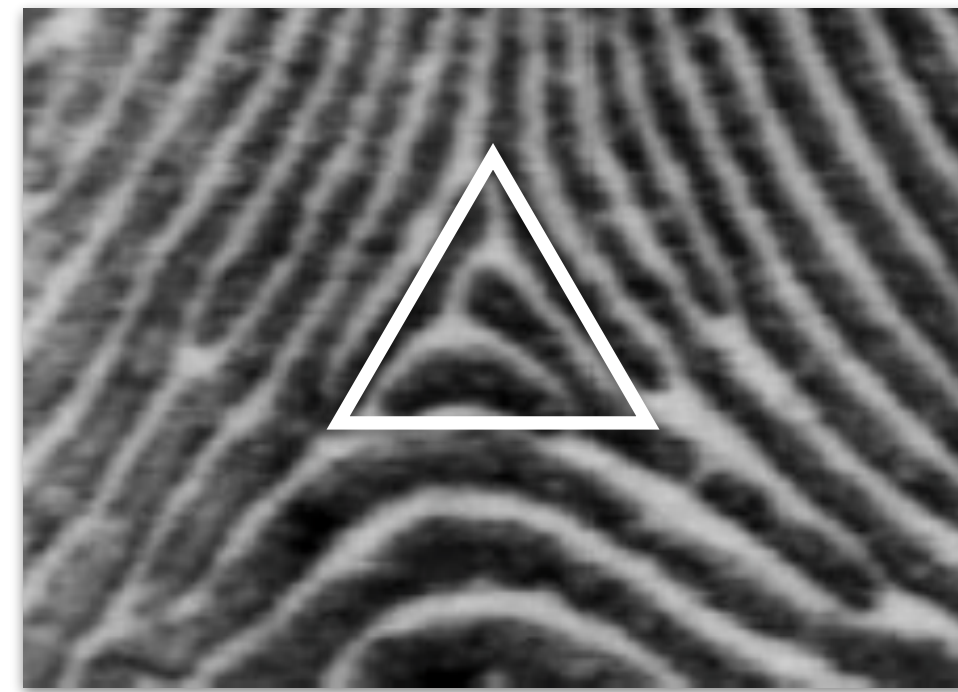
# Fingerprint Indexing

## Level-1 Features

### Usage of Singular Points and Core



loop



delta

Jain, Ross, and Nadakumar  
*Introduction to Biometrics*  
Springer Books, 2011

# Fingerprint Indexing

## Level-1 Features

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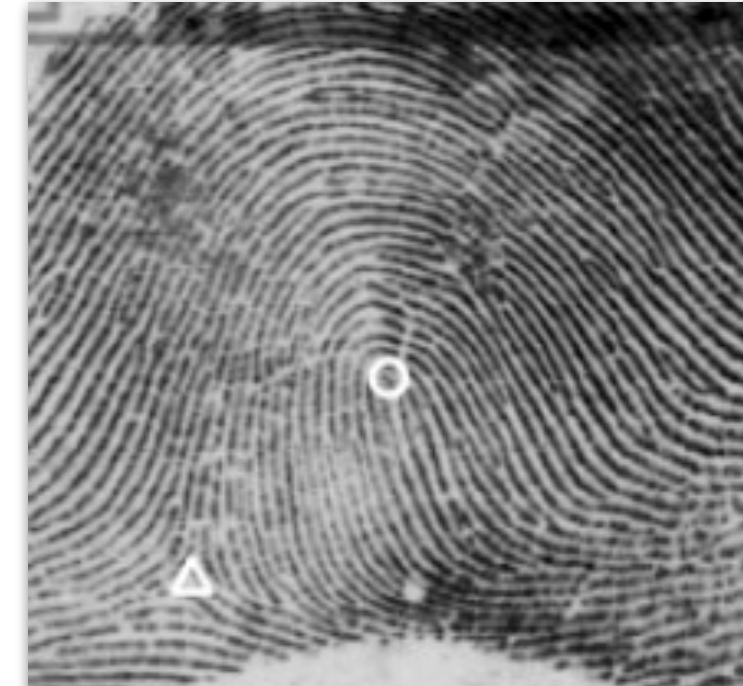
plain arch



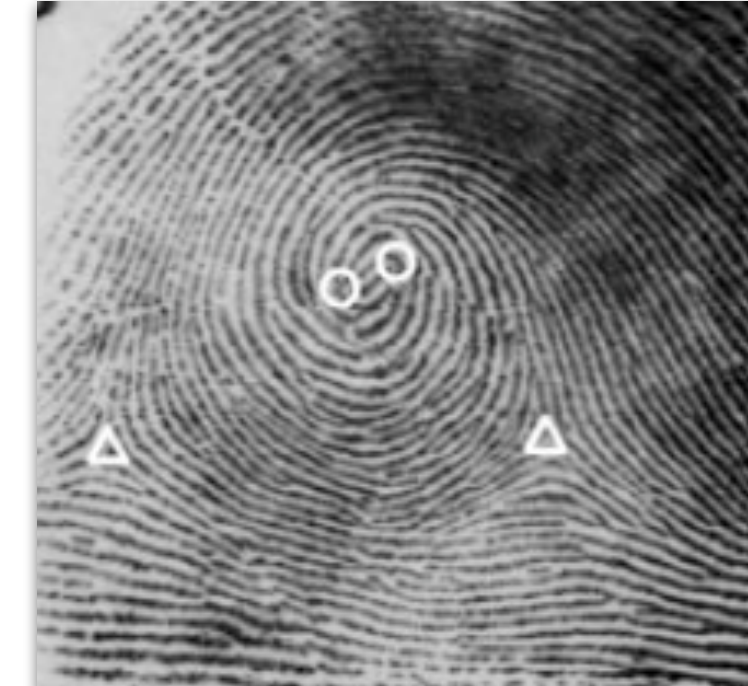
tented arch



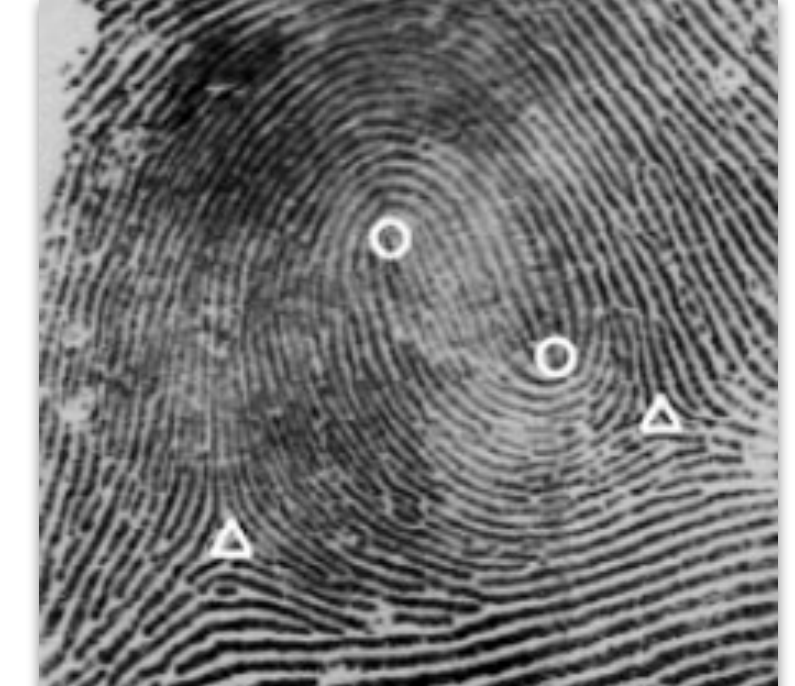
left loop



right loop



whorl



twin loop

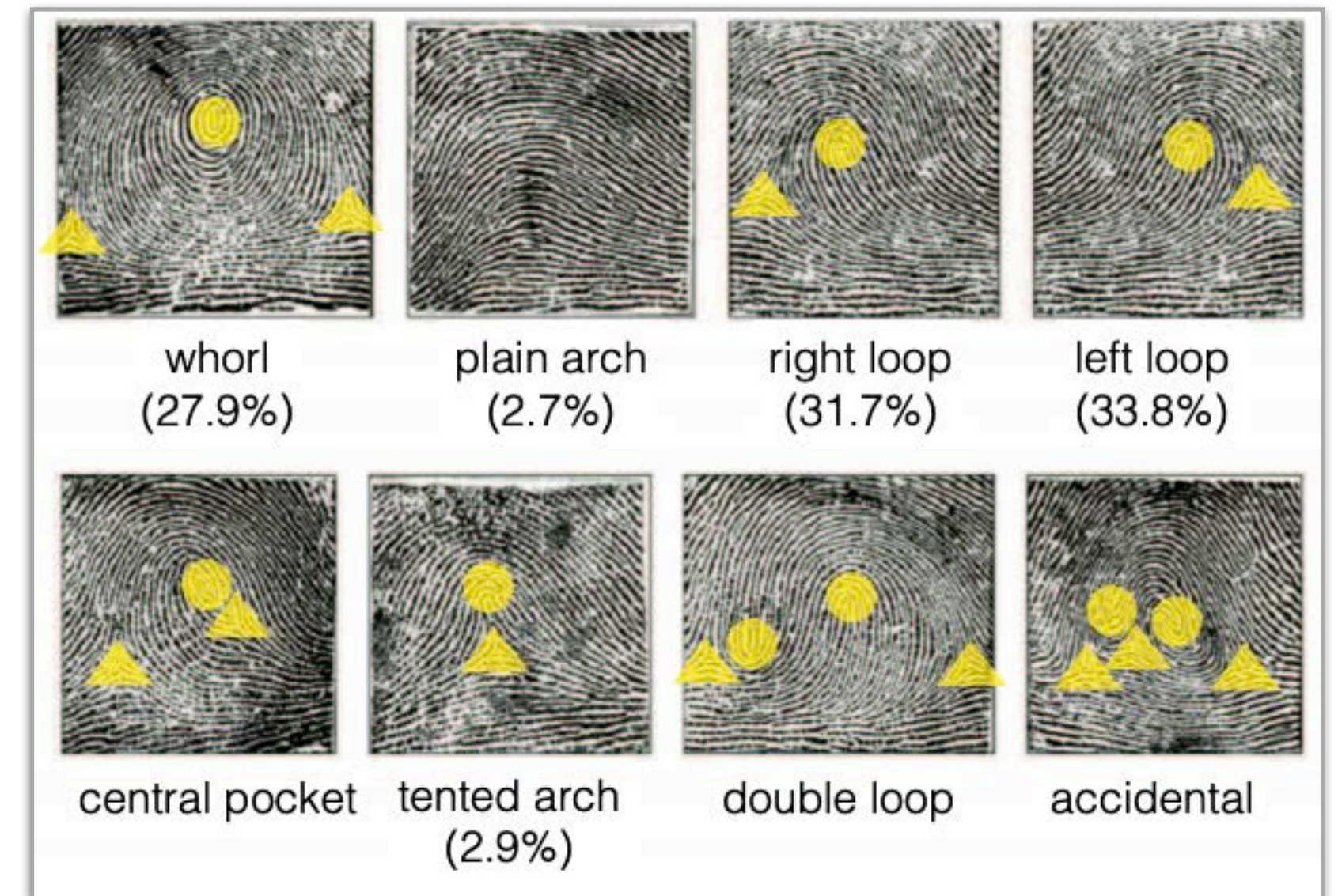
# Fingerprint Indexing

## Level-1 Features

### FBI Automated Fingerprint Identification system (AFIS)

More than 200 million dactyloscopy cards.  
Varied quality of samples.

Thanks to fingerprint classification through level-1 features, this time is reduced to **20 min.**



Henry's features, an alternative classification of level-1 features with 8 classes.

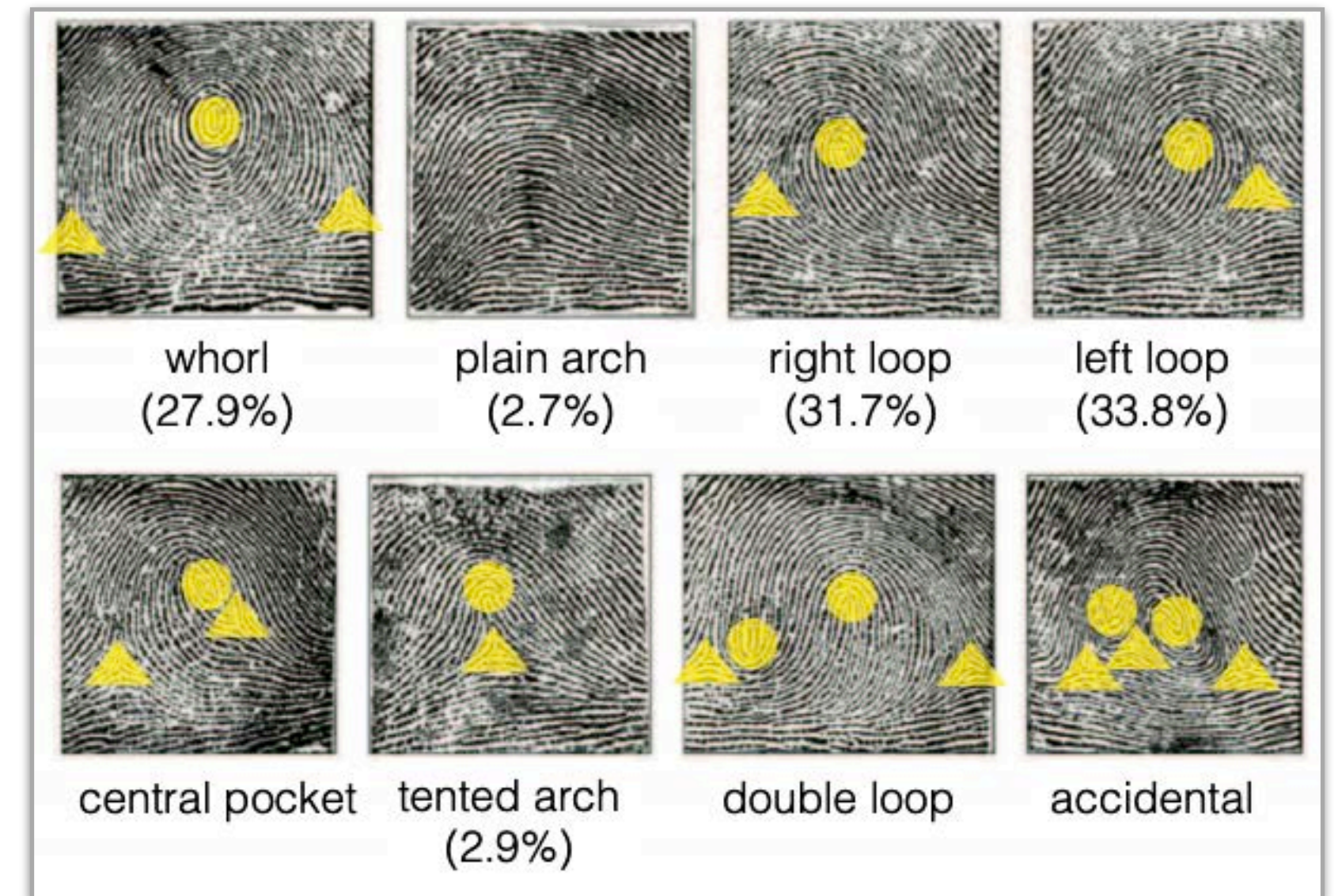
# Fingerprint Indexing

## Level-1 Features

### FBI Automated Fingerprint Identification system (AFIS)

More than 200 million dactyloscopy cards.  
Varied quality of samples.

And a computer-based solution can do it in seconds, benefitting from the same features.

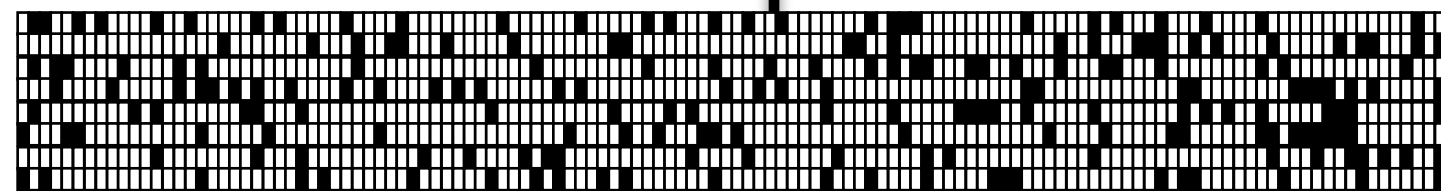
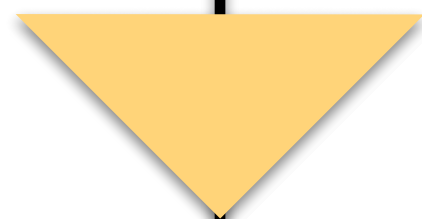
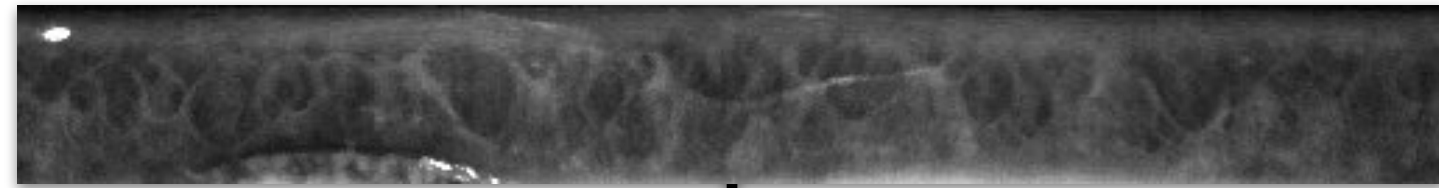


Henry's features, an alternative classification of level-1 features with 8 classes.



# Feature Indexing

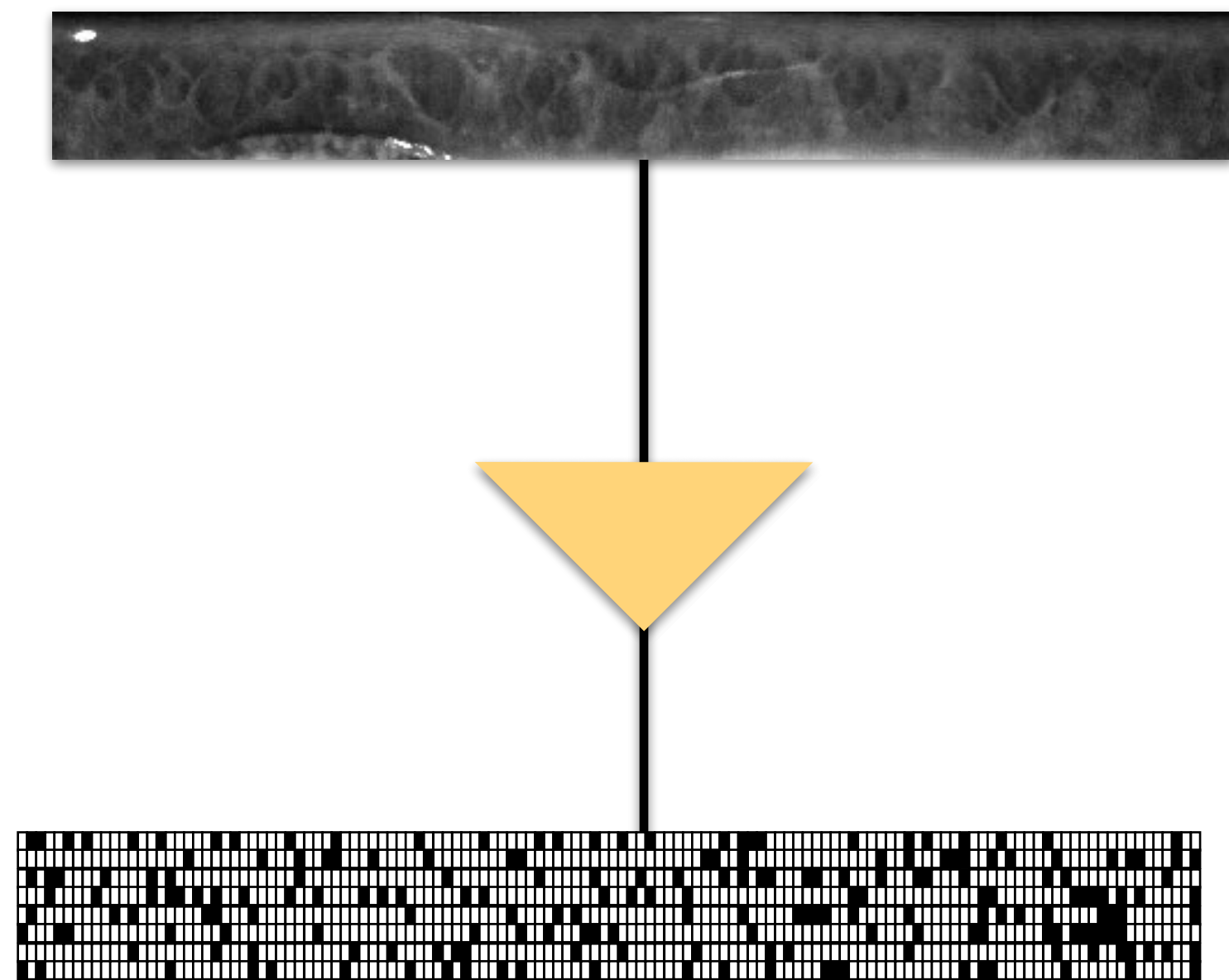
## Iris Identification



2048 bits IrisCode

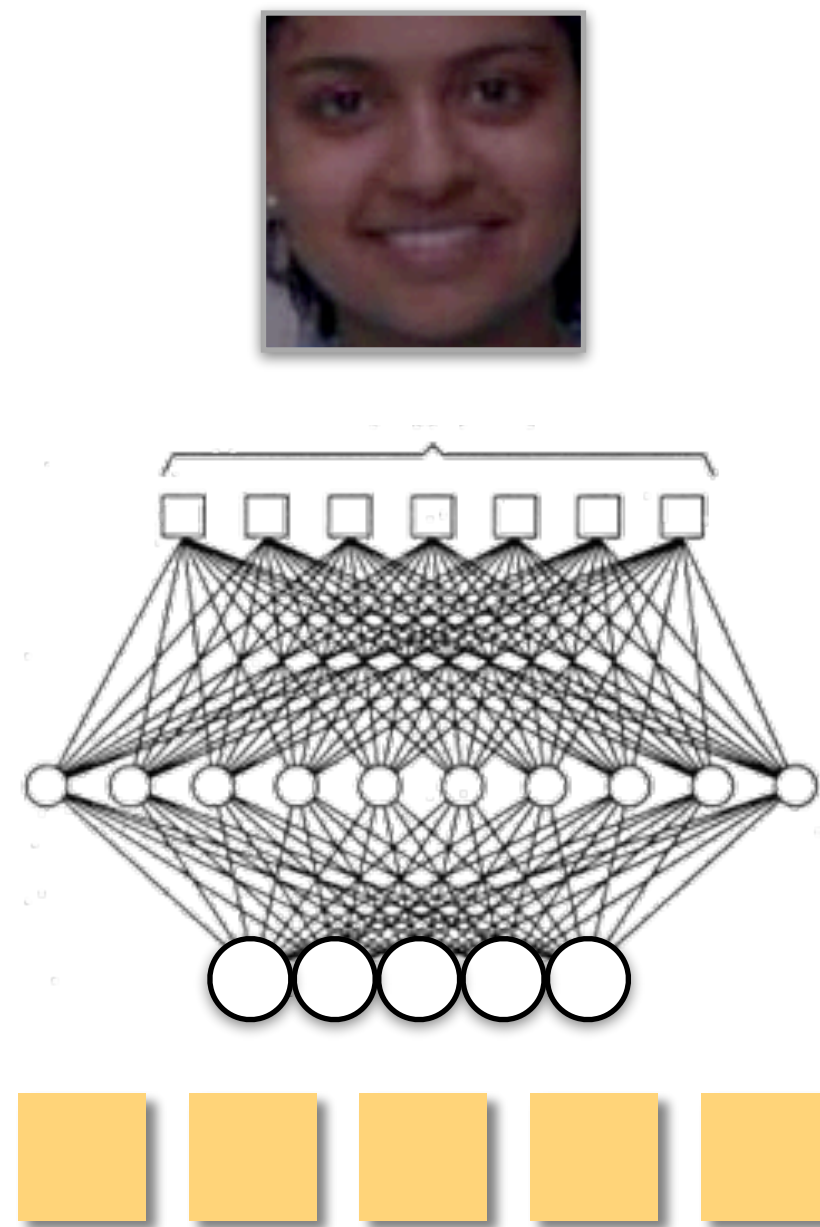
# Feature Indexing

Iris Identification



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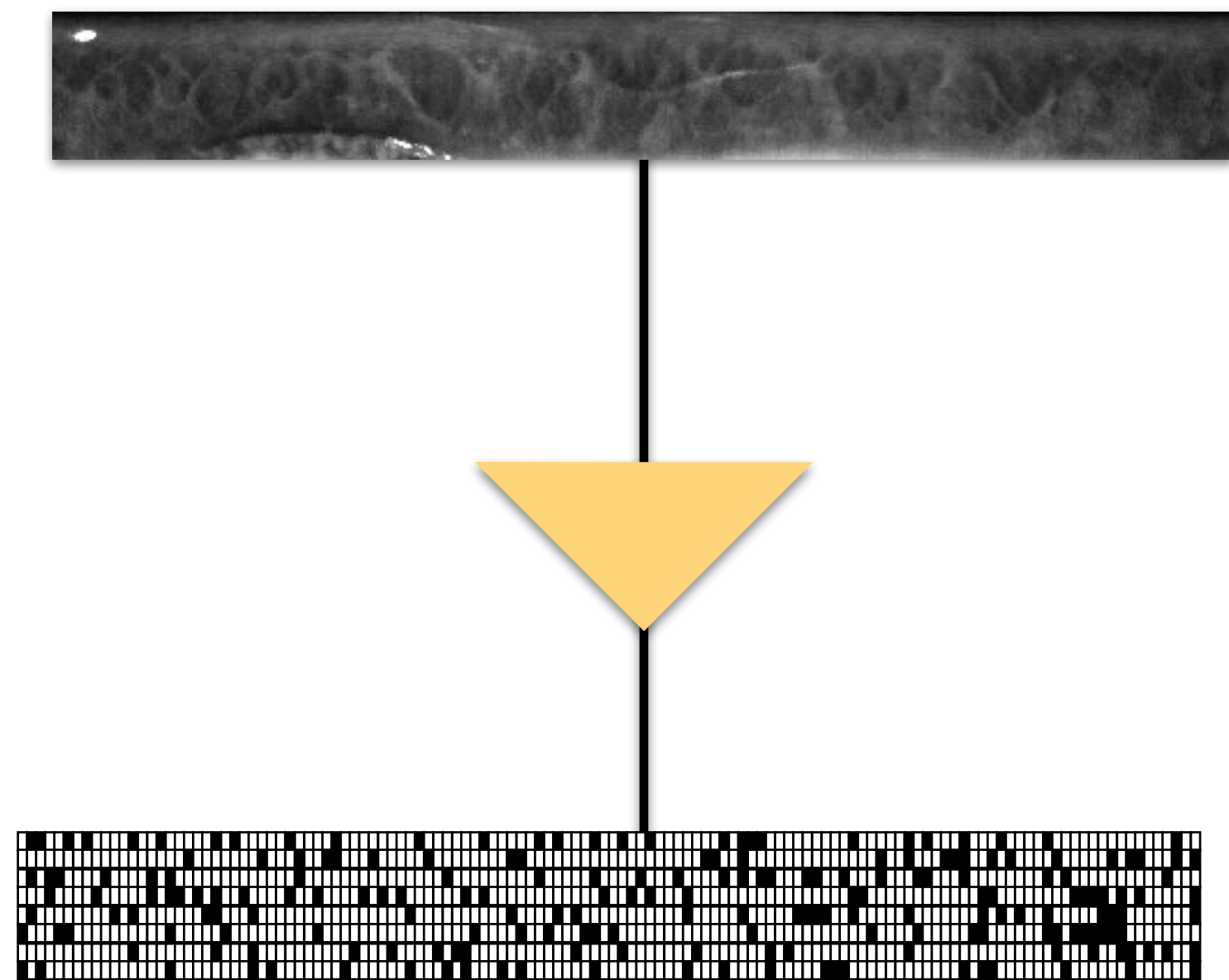
Face Identification



512D ArcFace embedding

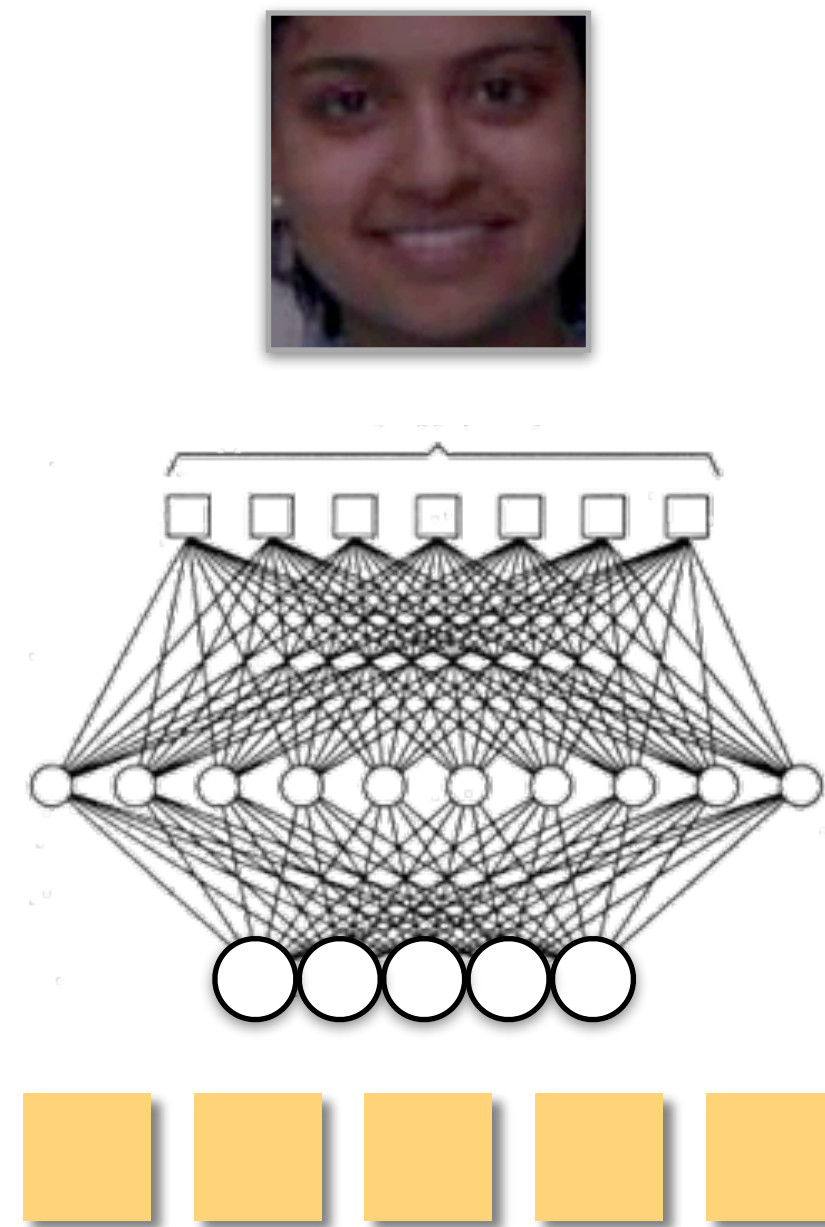
# Feature Indexing

Iris Identification



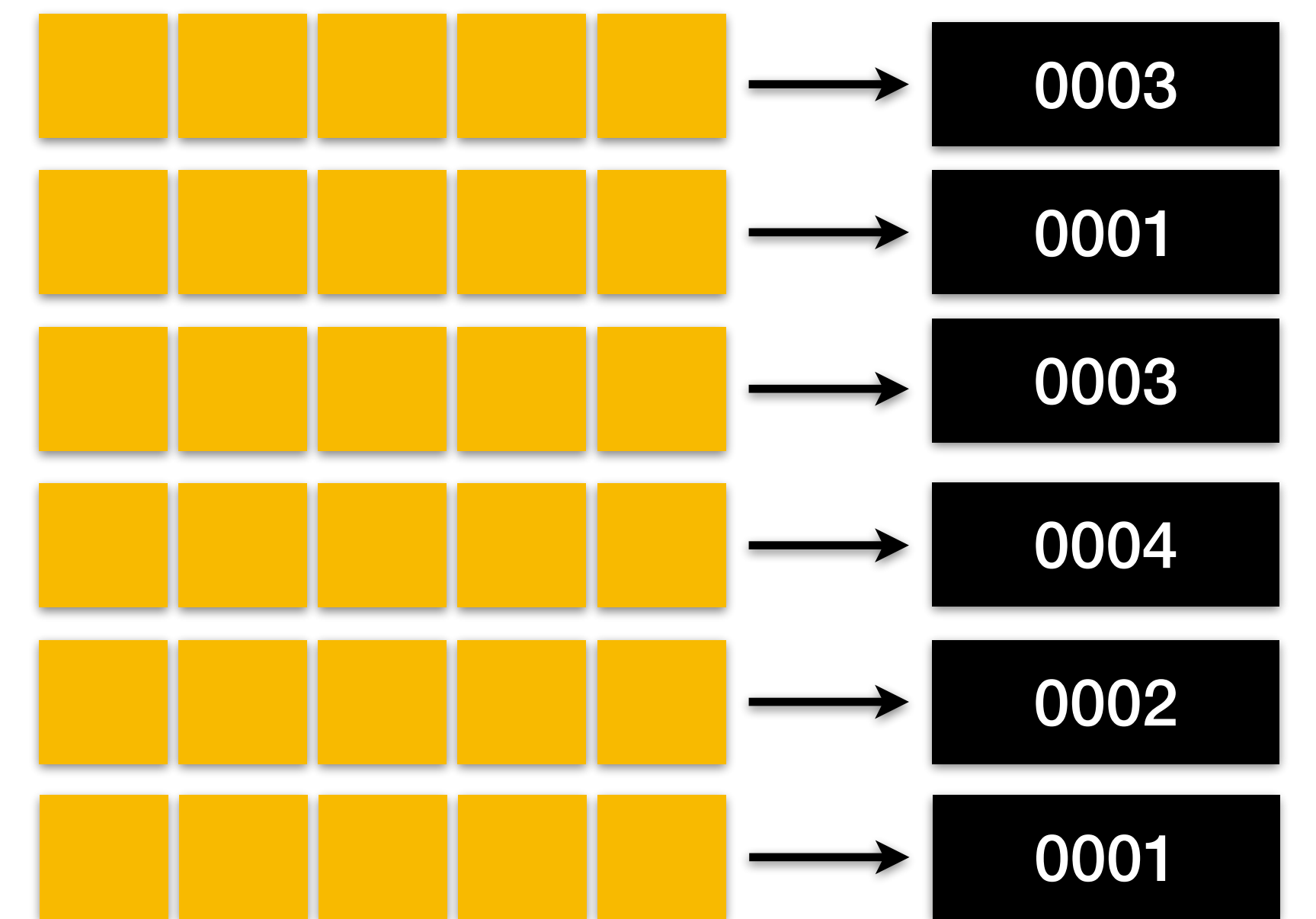
2048 bits IrisCode

Face Identification



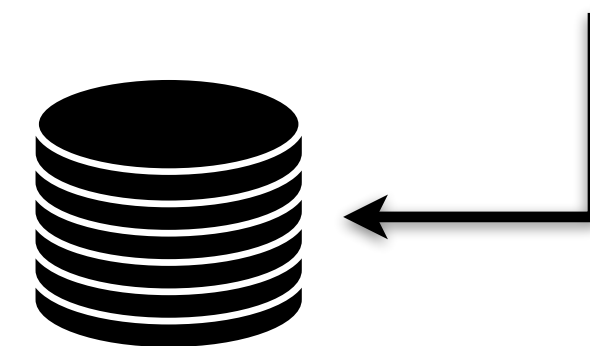
512D ArcFace embedding

Inverted Index



Feature space

Person's IDs



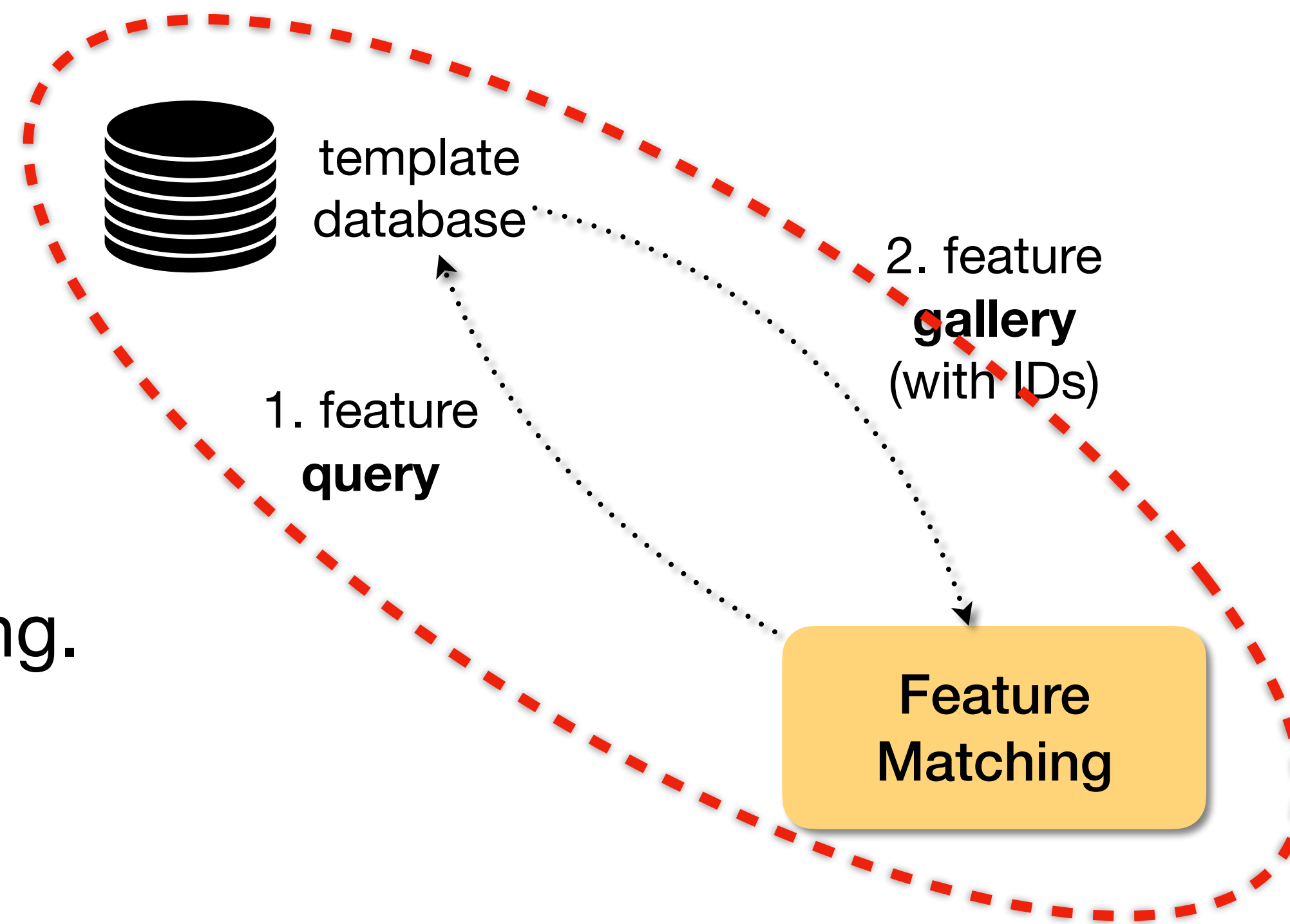
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UNIVERSITY CHICAGO

# Feature Indexing

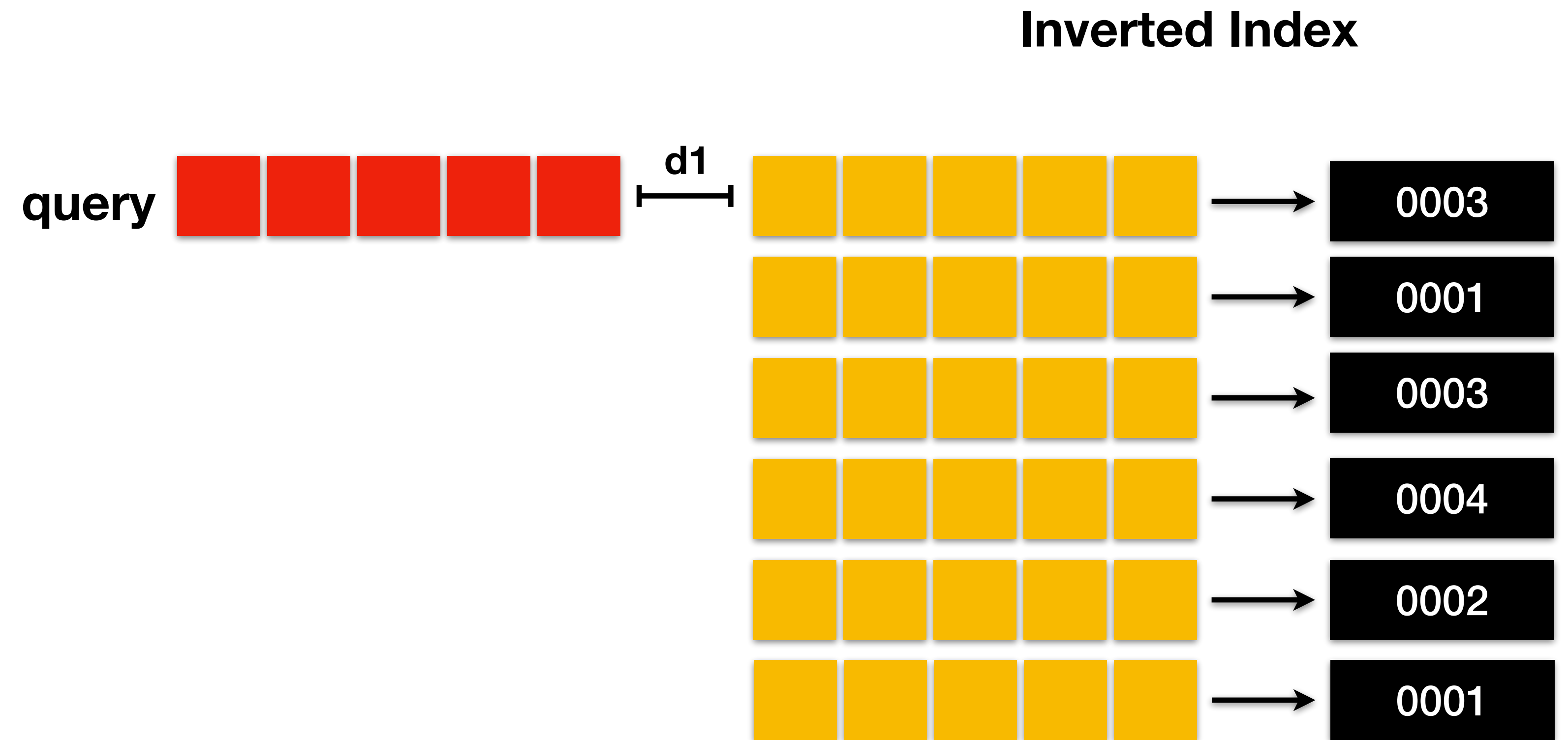
How to retrieve  $k$ -nearest features to compose gallery?

Need for more complex indexing.

Retrieval of features as quick as possible.



# Brute Force Search

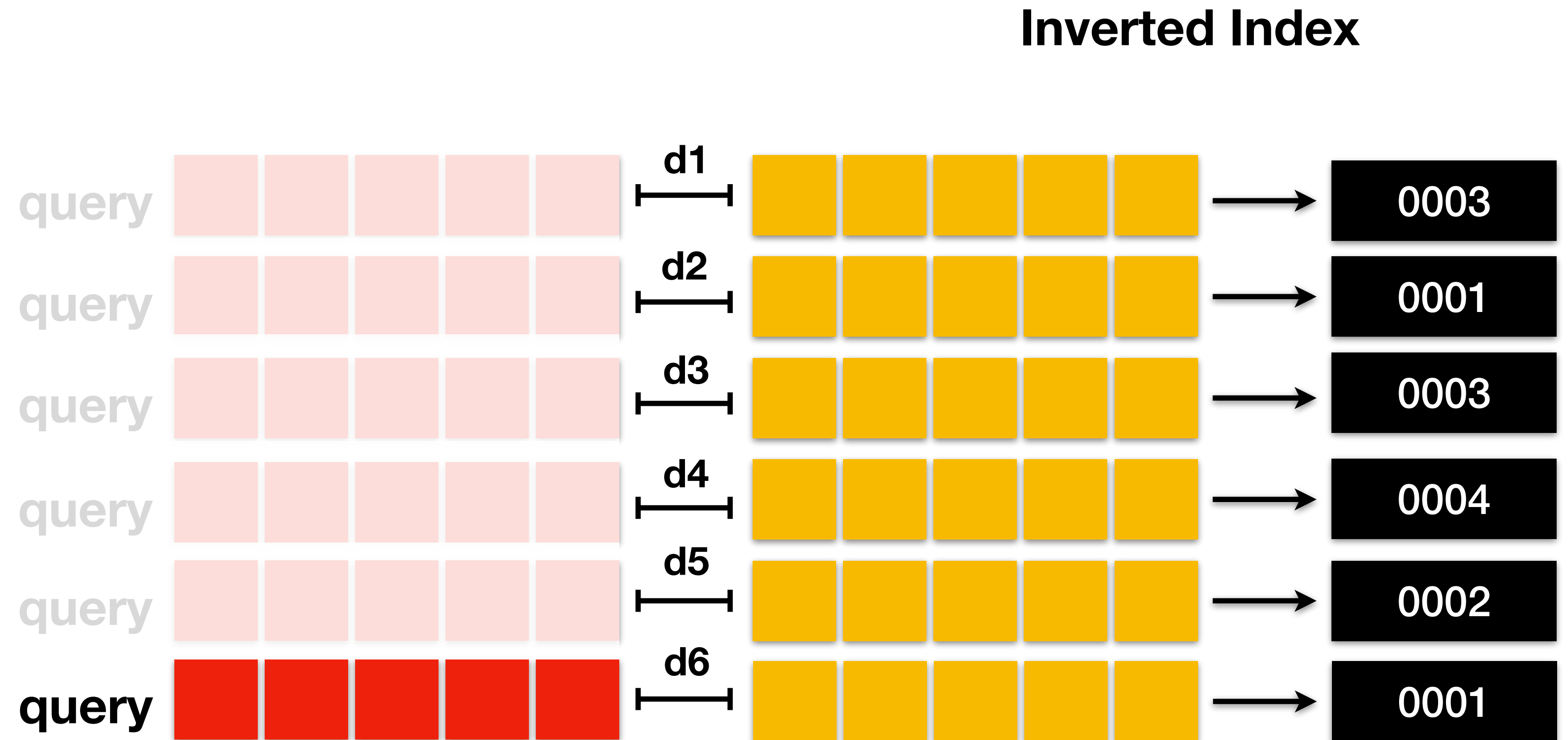


# Brute Force Search

What is the computational complexity?

Linear:  $O(n)$ , where  $n$  is the number of features.

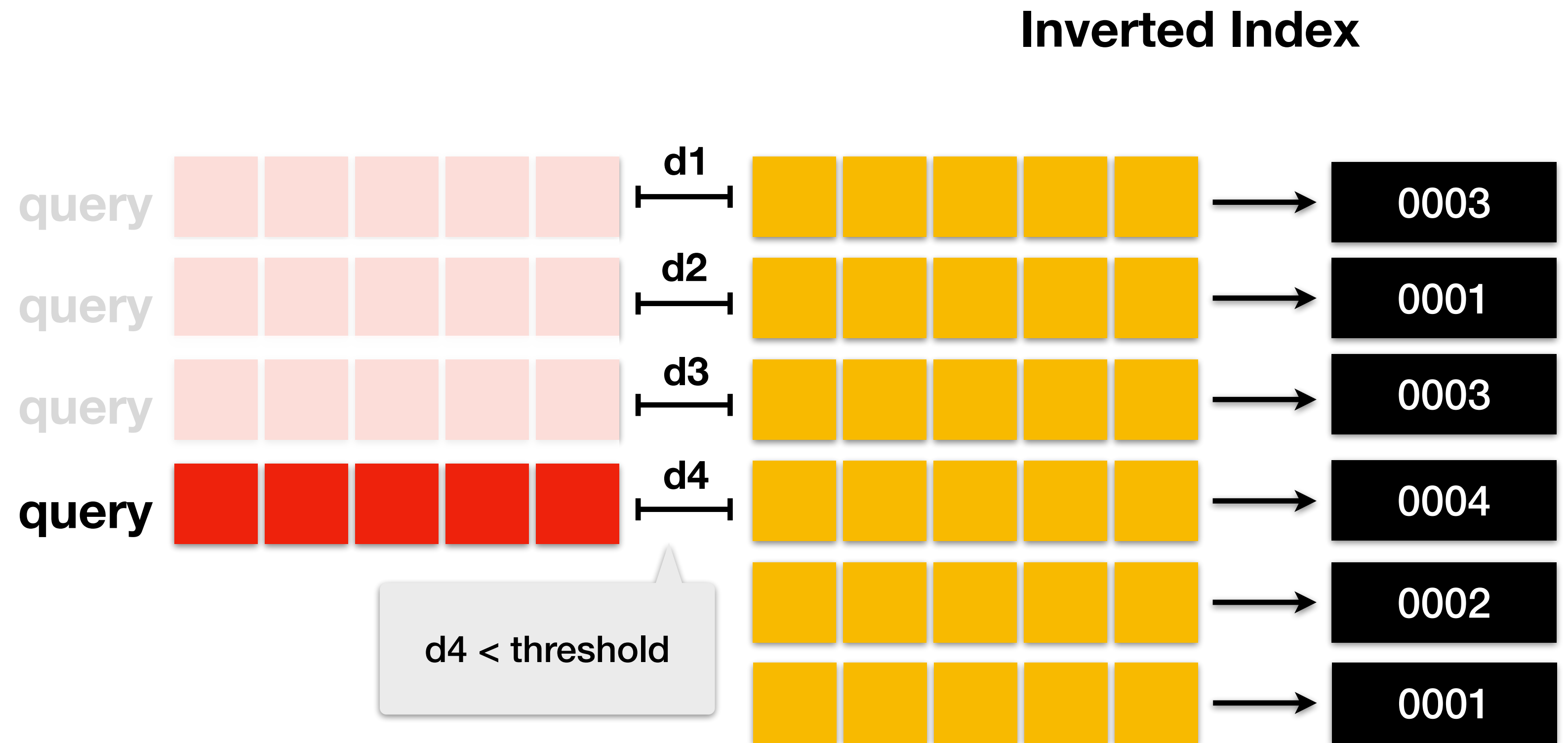
How to reduce it?



# Early Stop Search

How to reduce complexity?

Stop when you find a feature that is close enough.

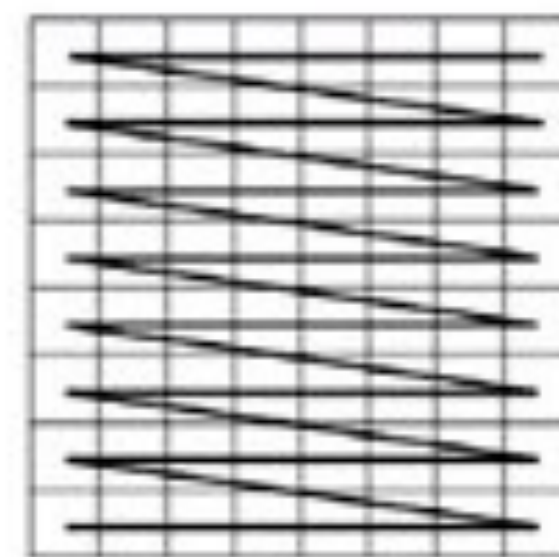


# Space Filling Curves

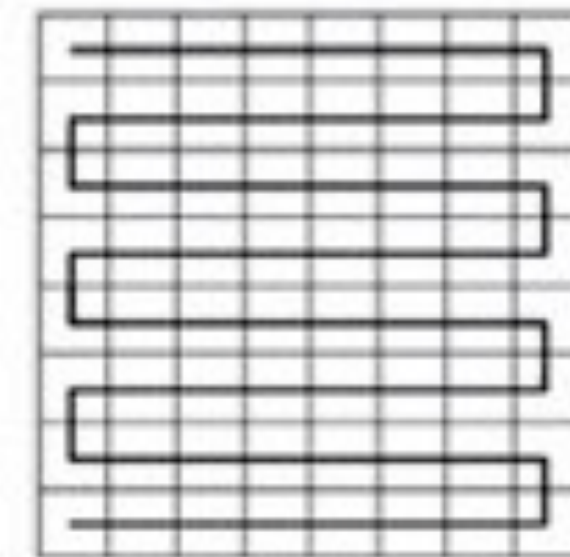
2D space examples

How to reduce complexity?

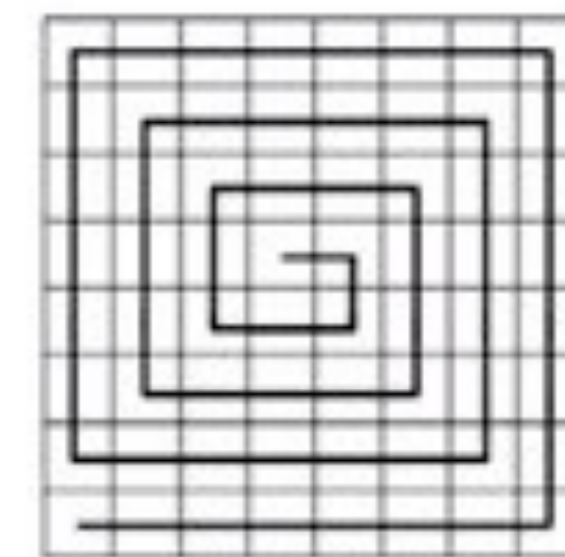
Curves determined by index mapping functions that pass once through every point of an  $N$ -dimensional space.



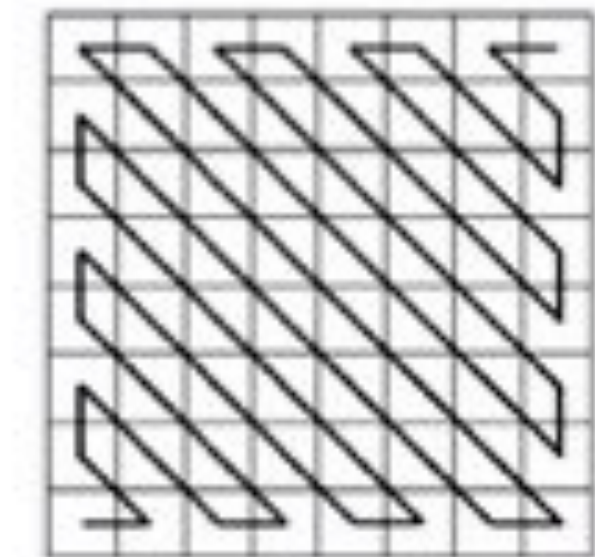
(a)



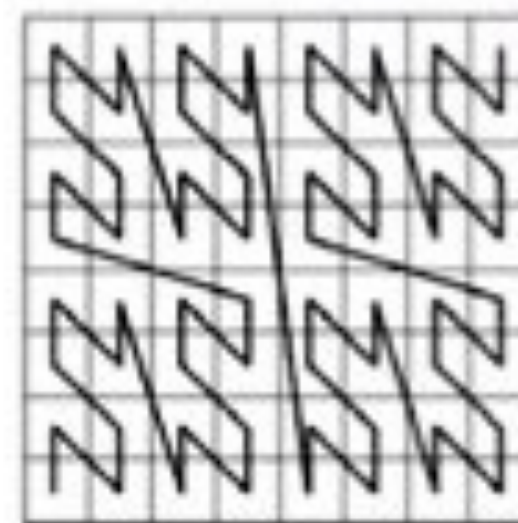
(b)



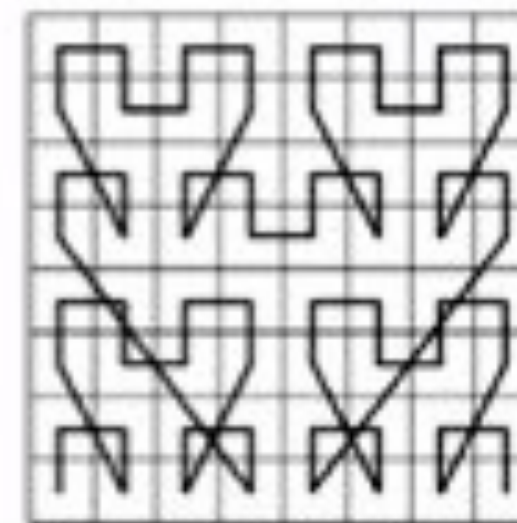
(c)



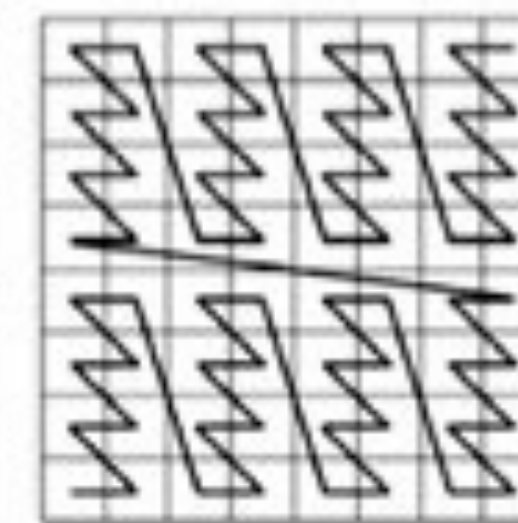
(d)



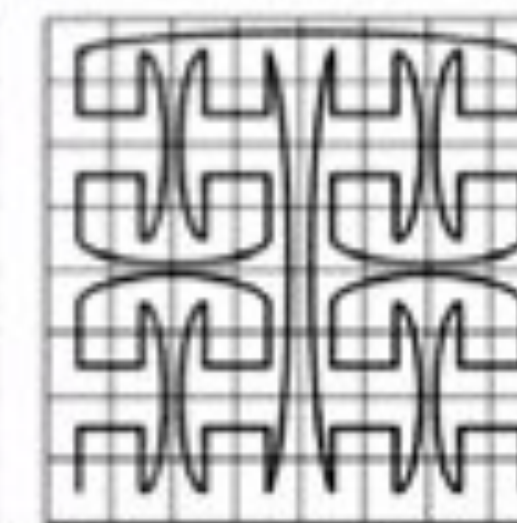
(e)



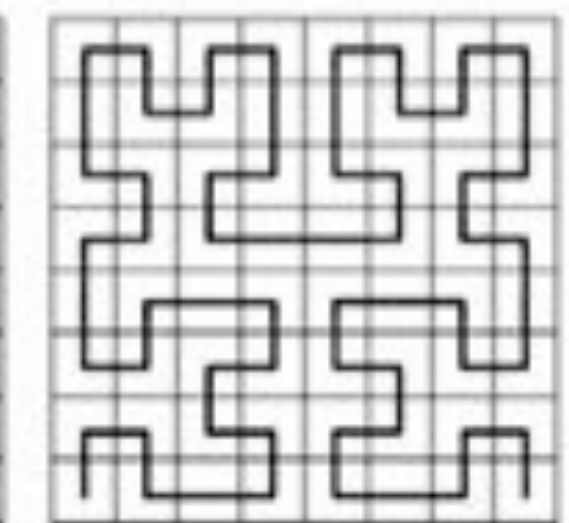
(f)



(g)



(h)



(i)

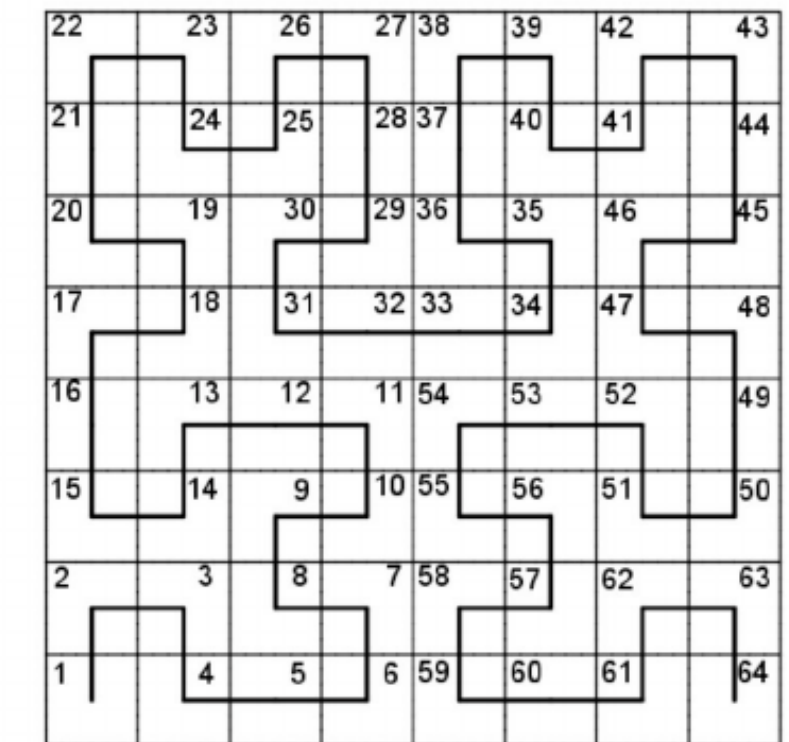
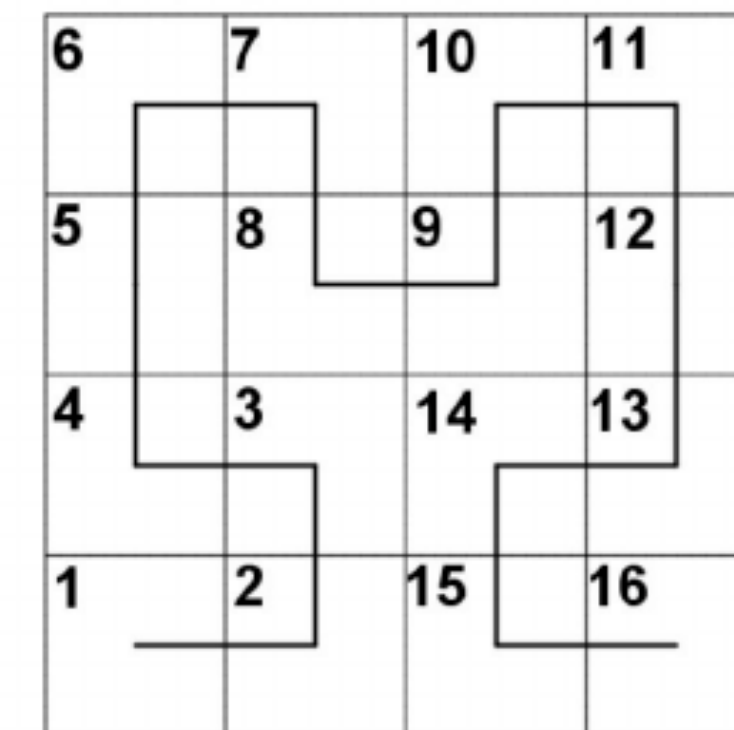
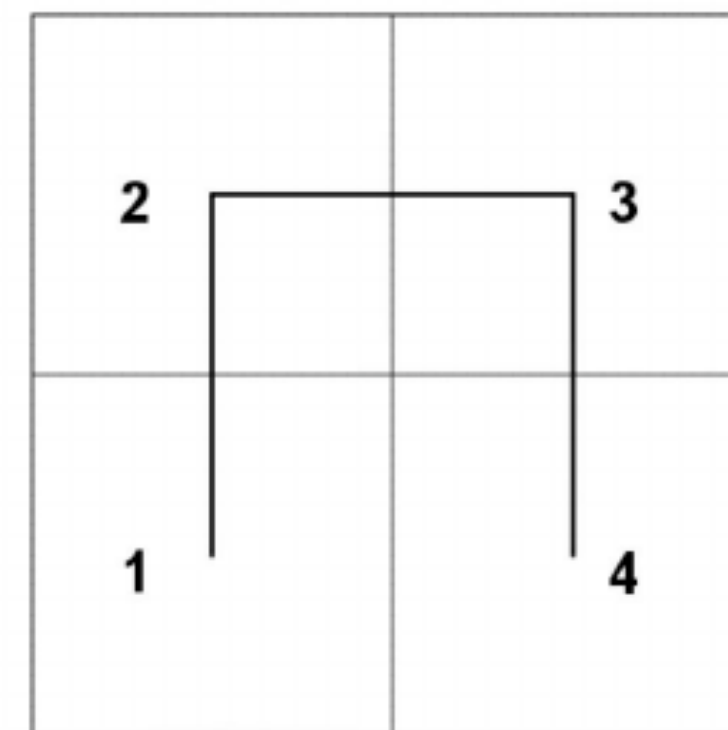


# Space Filling Curves

How to reduce complexity?

Curves determined by index mapping functions that pass once through every point of an  $N$ -dimensional space.

2D space examples



Hilbert curves

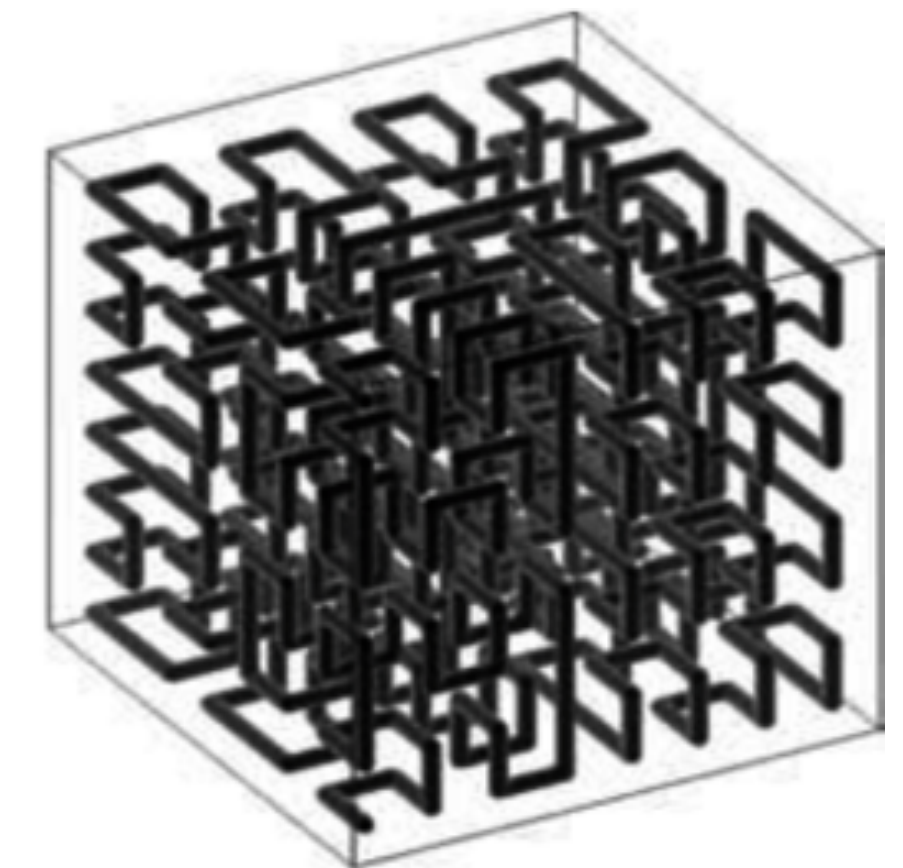
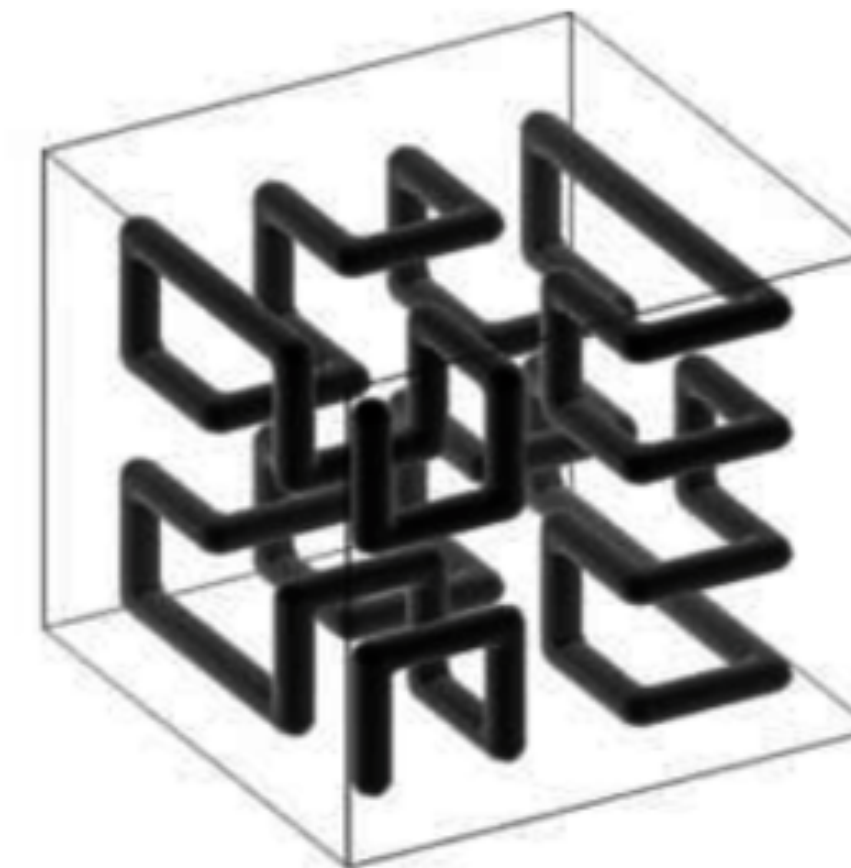
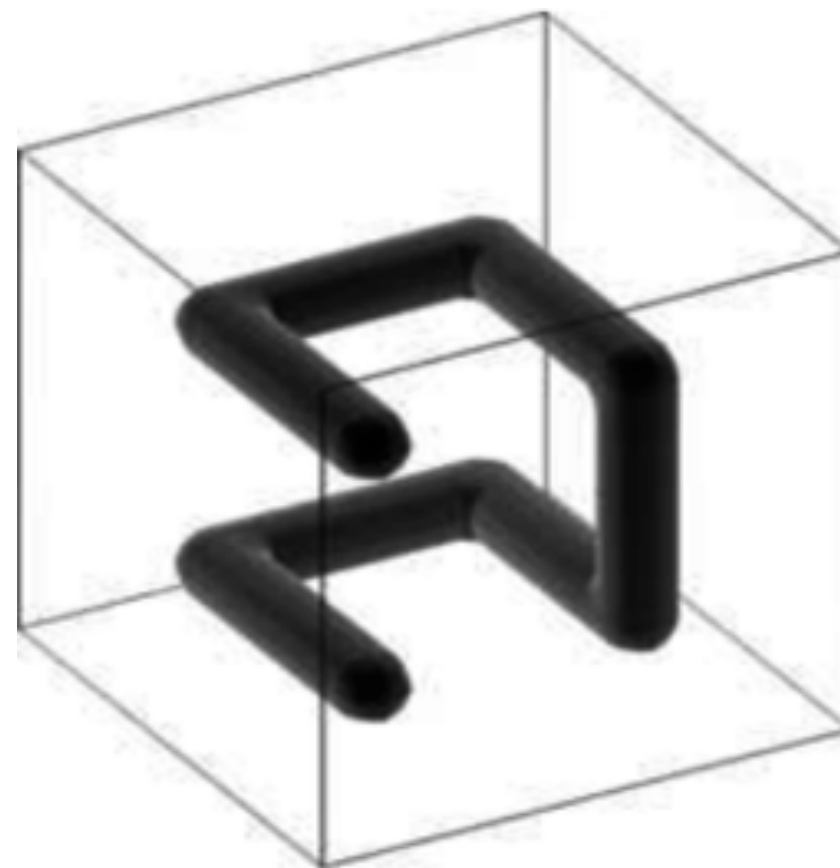
# Space Filling Curves

How to reduce complexity?

Curves determined by index mapping functions that pass once through every point of an  $N$ -dimensional space.

The mapping functions are executed in constant time, w.r.t. the number of features.

3D space examples



Hilbert curves

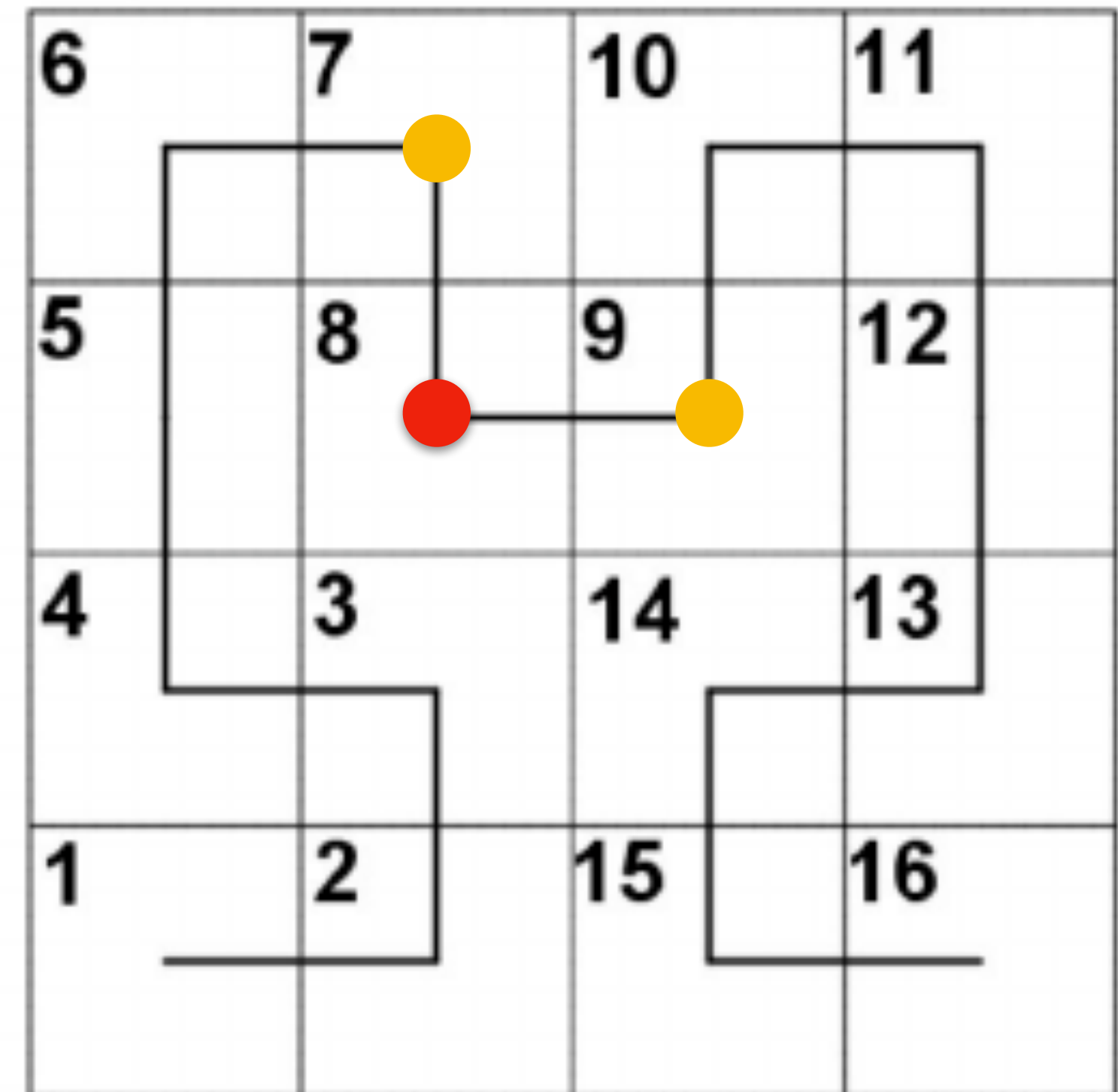
# Space Filling Curves

How to reduce complexity?

The curves are 1D and the elements indexed by them are “sorted” in an *approximation* of their distances in the original space.

If the curve is used as a binary tree, an approximation of the  $k$ -nearest elements can be obtained in  $O(\log(n))$ , where  $n$  is the number of features.

Example:  
2-nearest  
elements

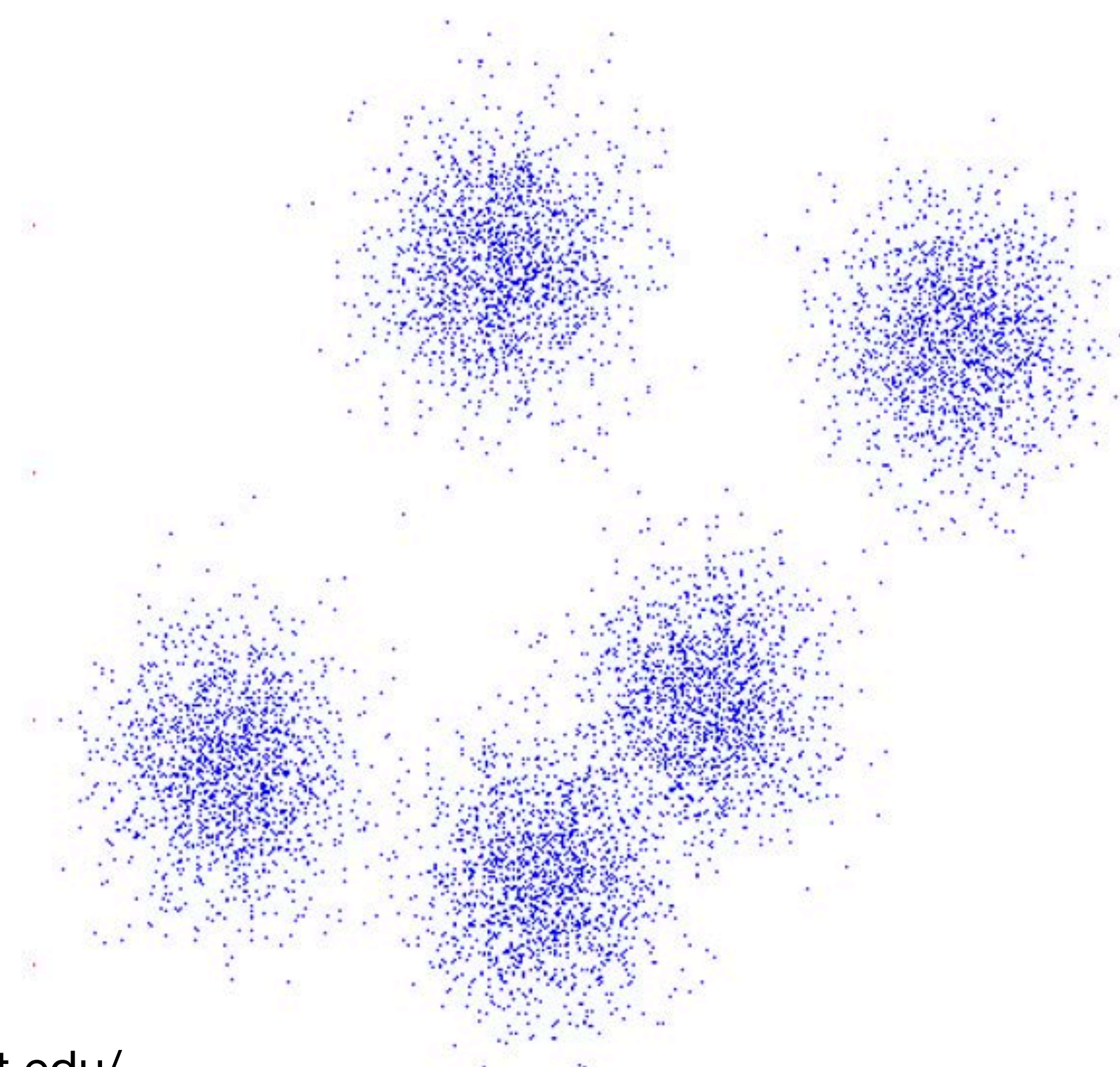


# Clustering

How to reduce complexity?

Cluster the features and limit the k-nearest search to one or a couple of clusters.

There will be less elements to consider



Source: <https://people.csail.mit.edu/dsontag/courses/ml12/slides/lecture14.pdf>

# Clustering

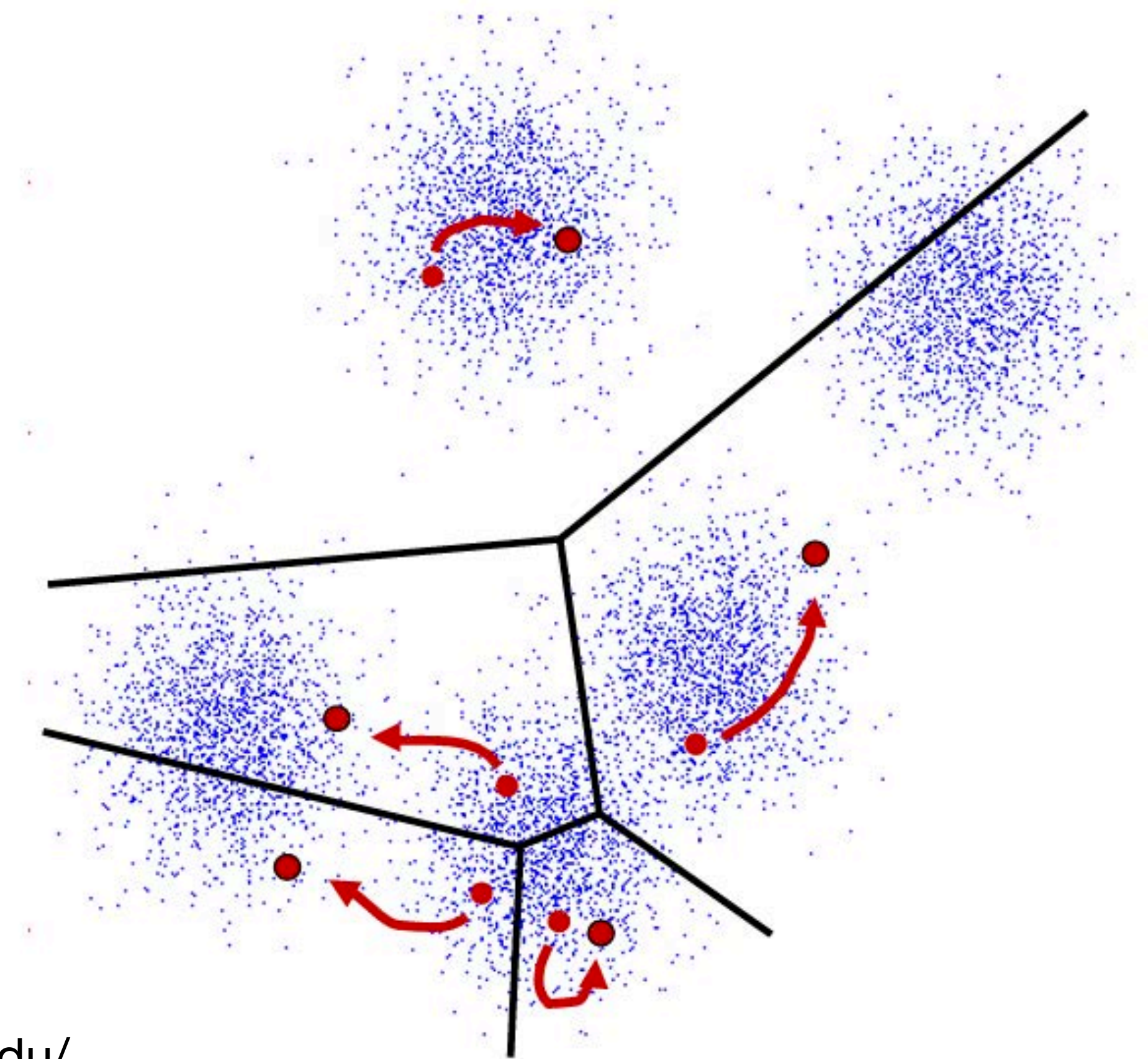
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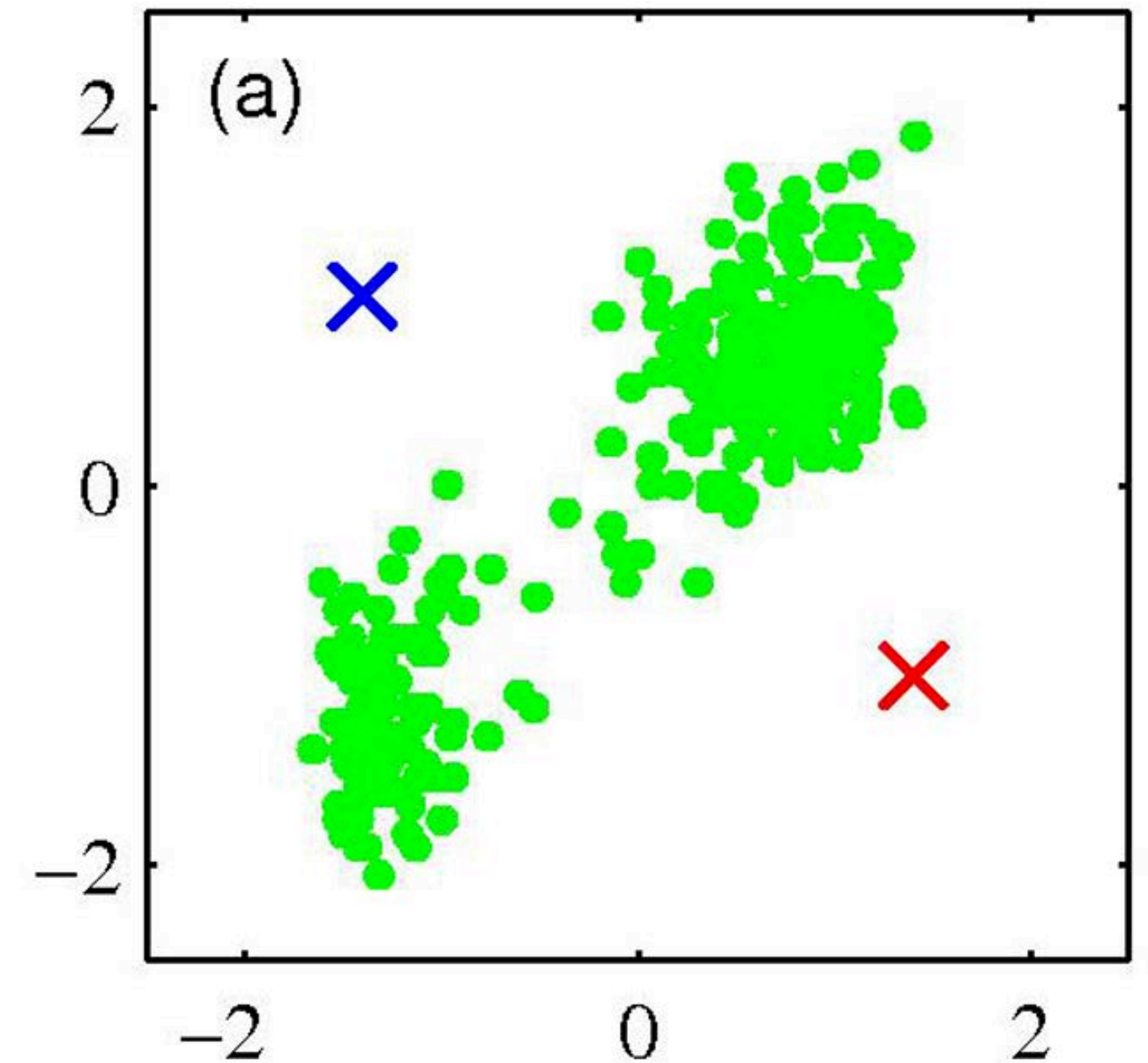
## K-Means



# Clustering

K-Means

Select K random features as cluster centers.

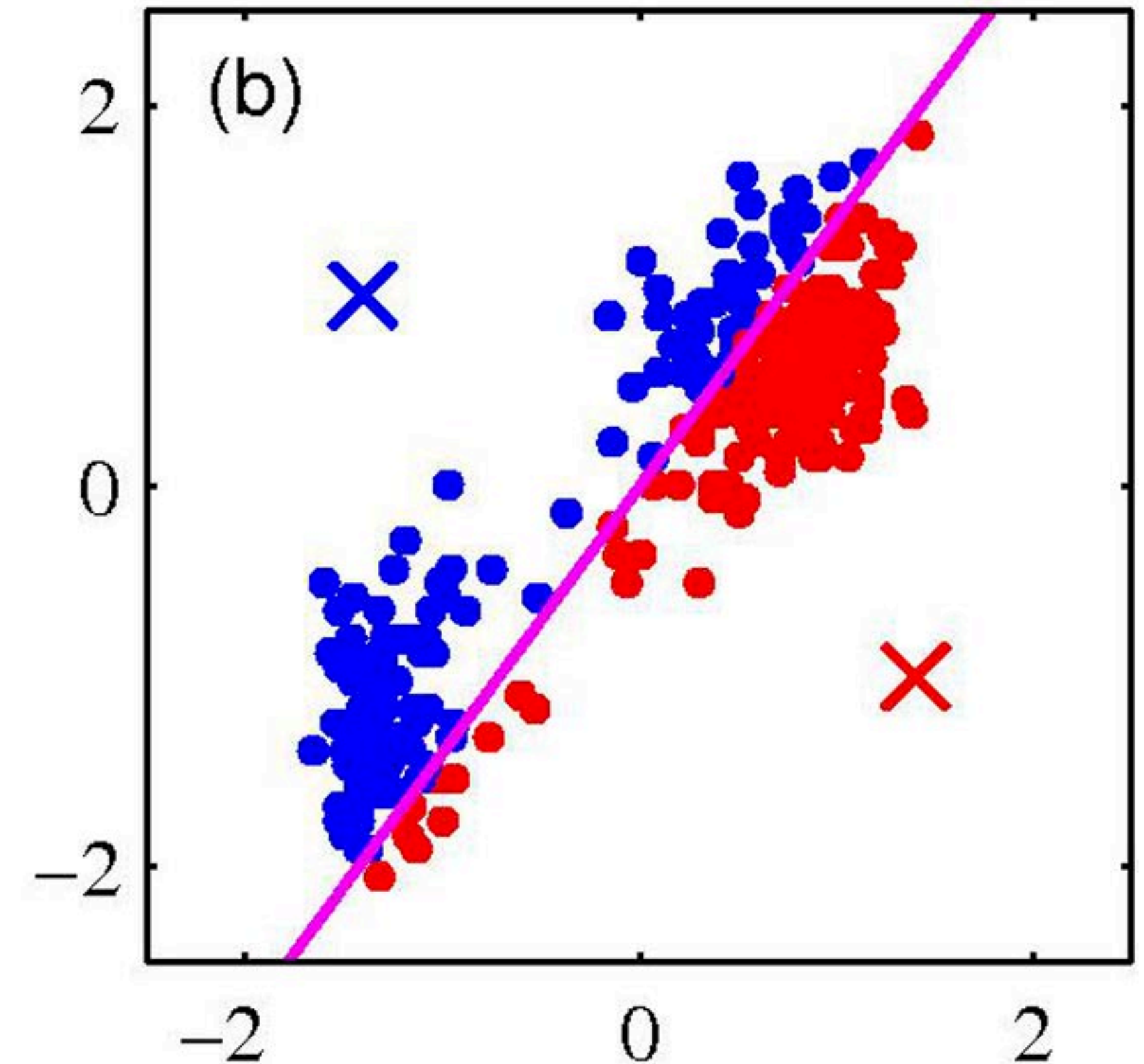


Source: <https://people.csail.mit.edu/dsontag/courses/ml12/slides/lecture14.pdf>

# Clustering

K-Means

Assign features to closes cluster centers.

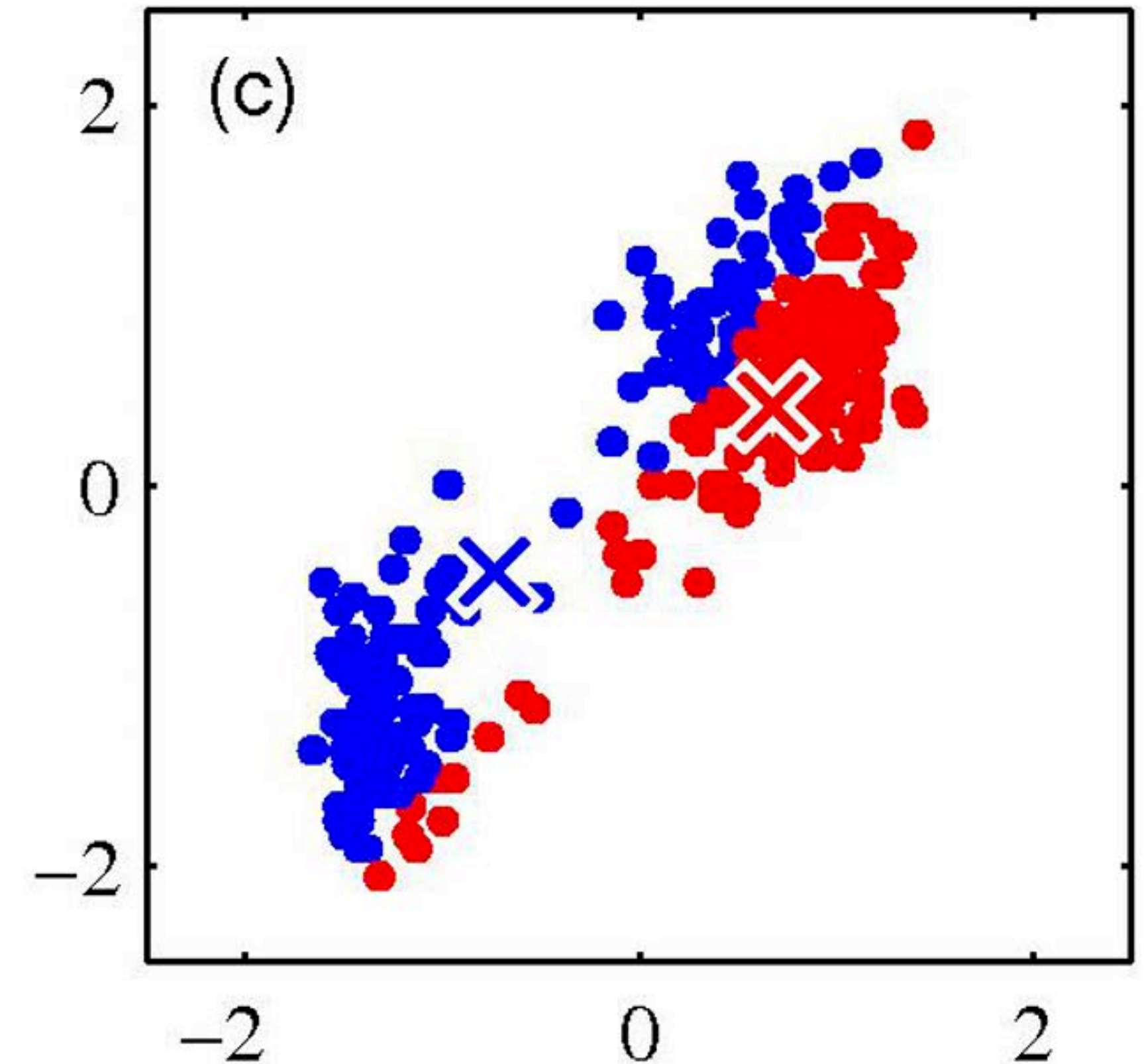


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# Clustering

K-Means

Update the cluster centers by taking the **means** of each cluster.



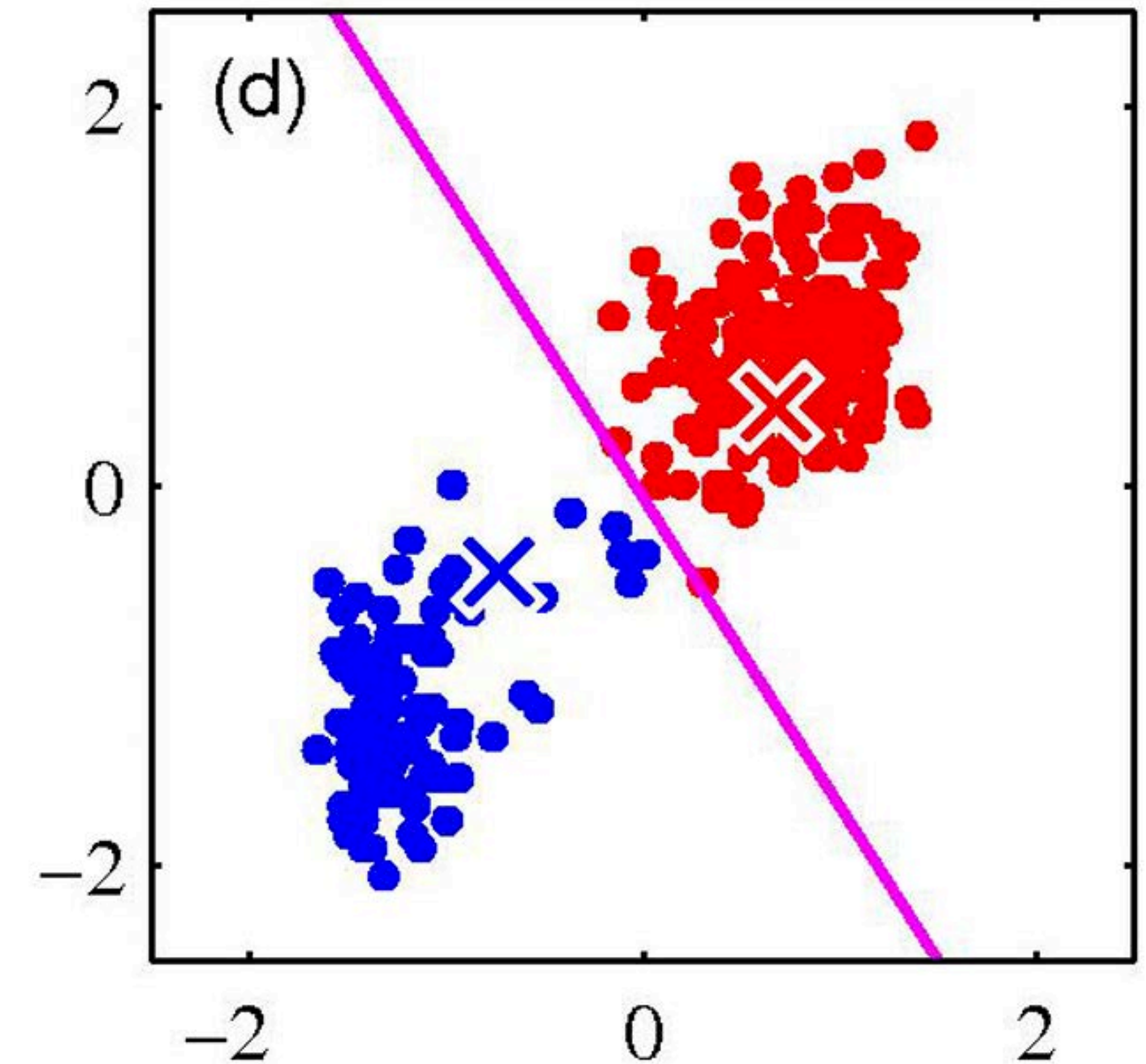
Source: <https://people.csail.mit.edu/dsontag/courses/ml12/slides/lecture14.pdf>



# Clustering

K-Means

Repeat until convergence.



Source: <https://people.csail.mit.edu/dsontag/courses/ml12/slides/lecture14.pdf>

# Clustering

## K-Means

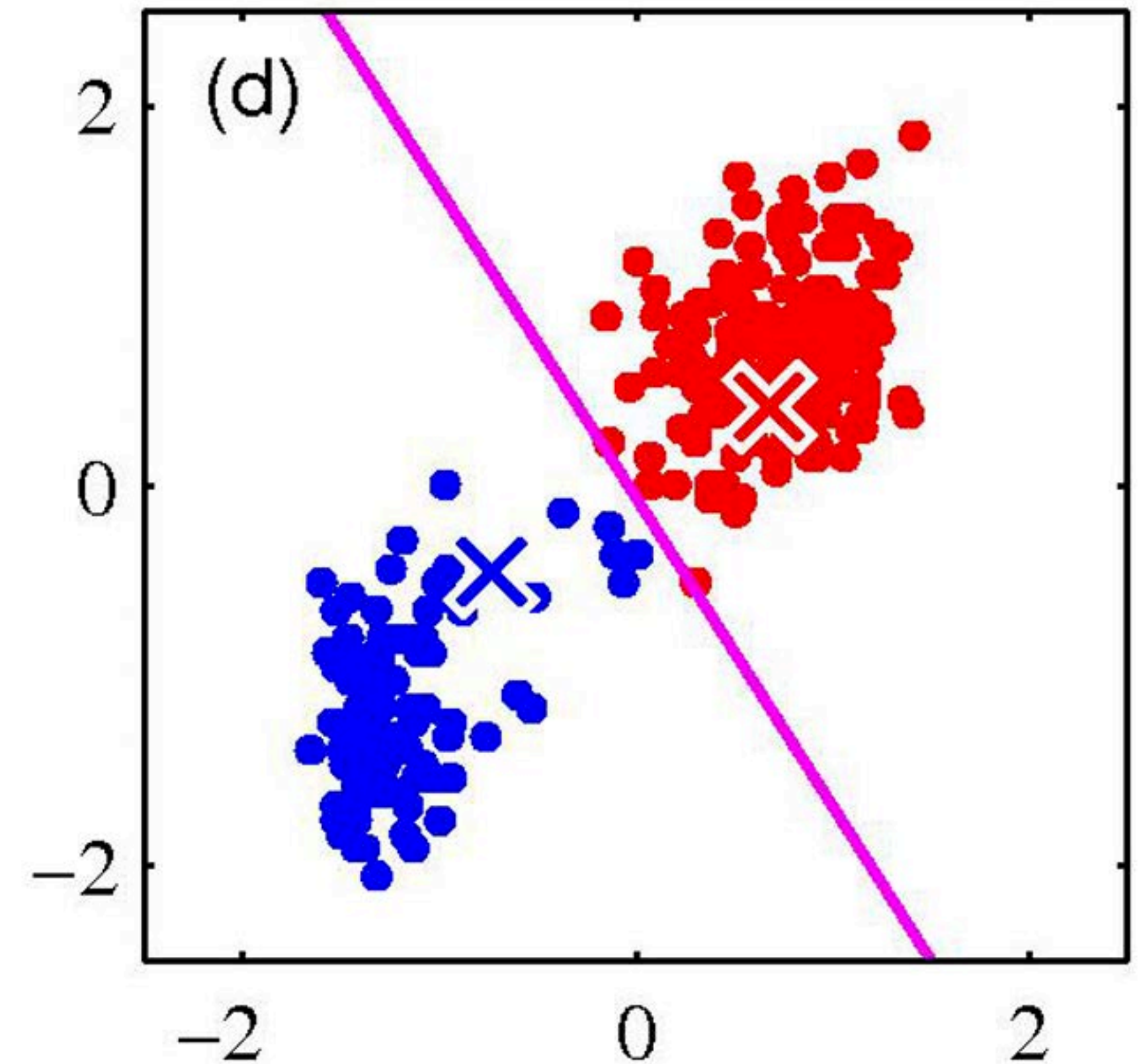
What are the limitations of this approach?

What is the ideal number of clusters?

Complexity of building clusters:  
 $O(Kn)$  in each step until convergence.

Clustering is *offline*: i.e., it does not happen at feature querying time.

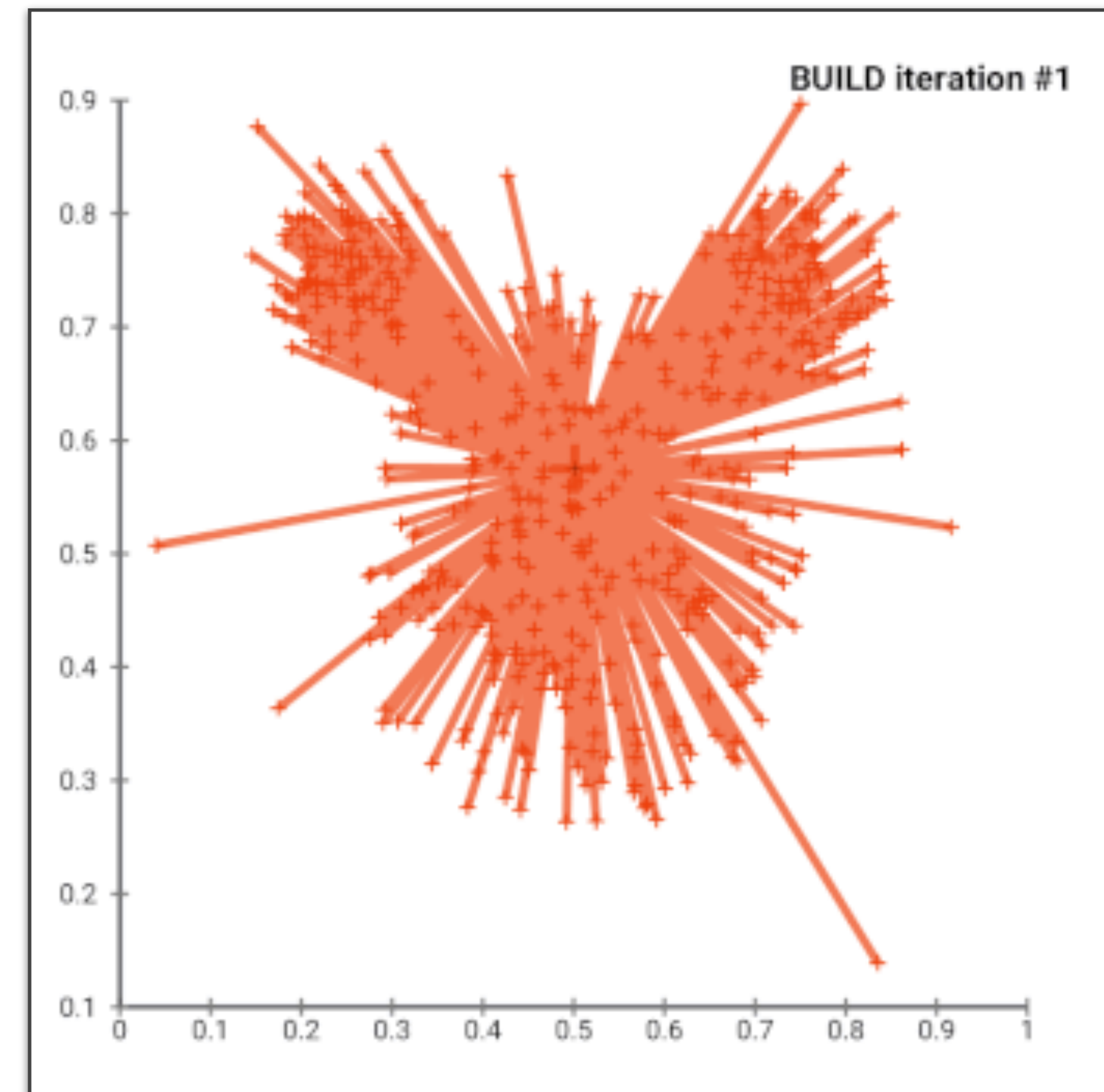
K: #clusters  
n: #features



# Clustering

Variation: K-medoids

Instead of using *means* as the cluster centers, use *medians*, which are actual existing features.



# KD Trees

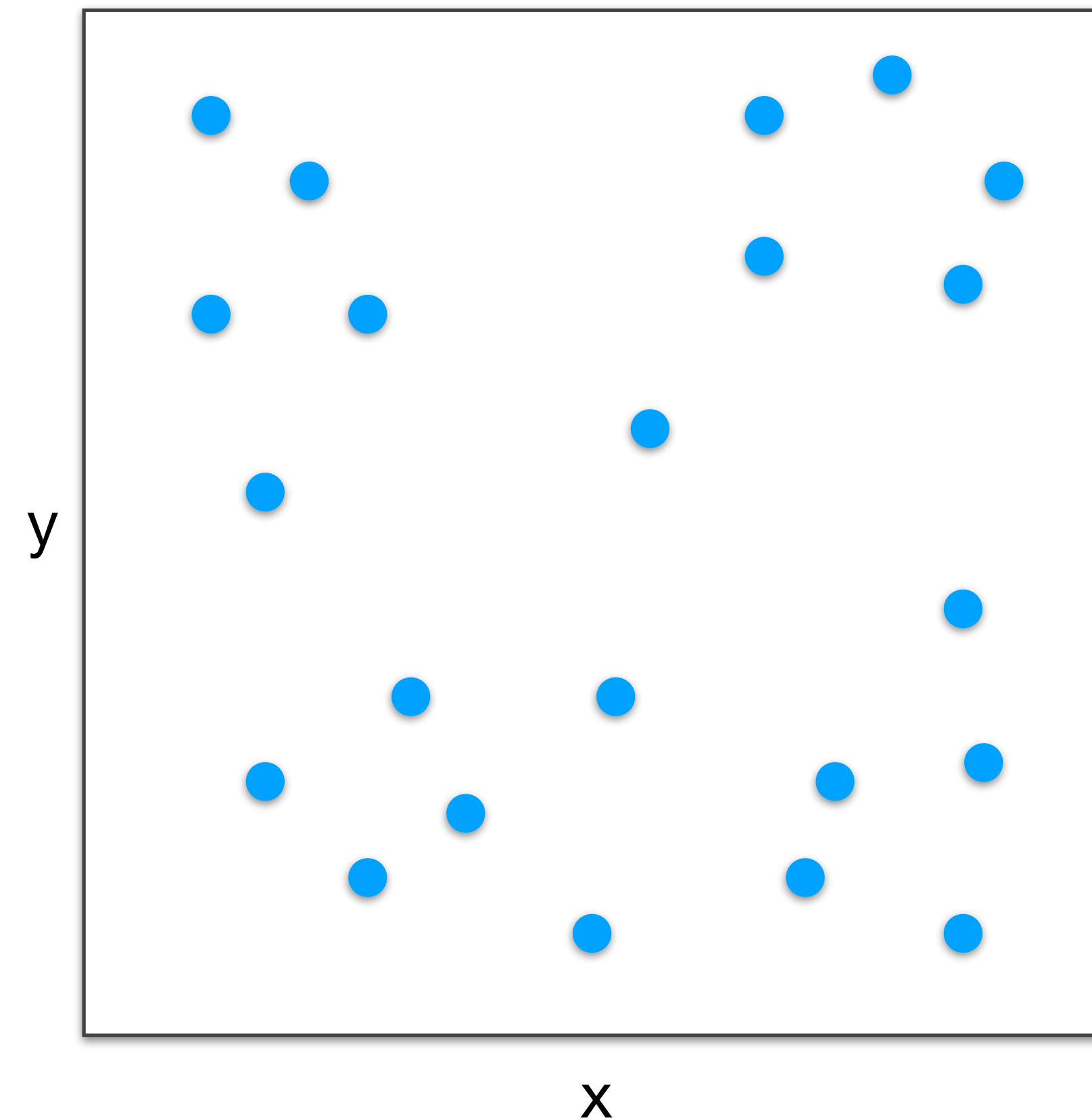
How to reduce complexity?

K-dimensional trees:

*For  $K$  times*

*Split one feature dimension into two halves.*

2D-features toy case



# KD Trees

How to reduce complexity?

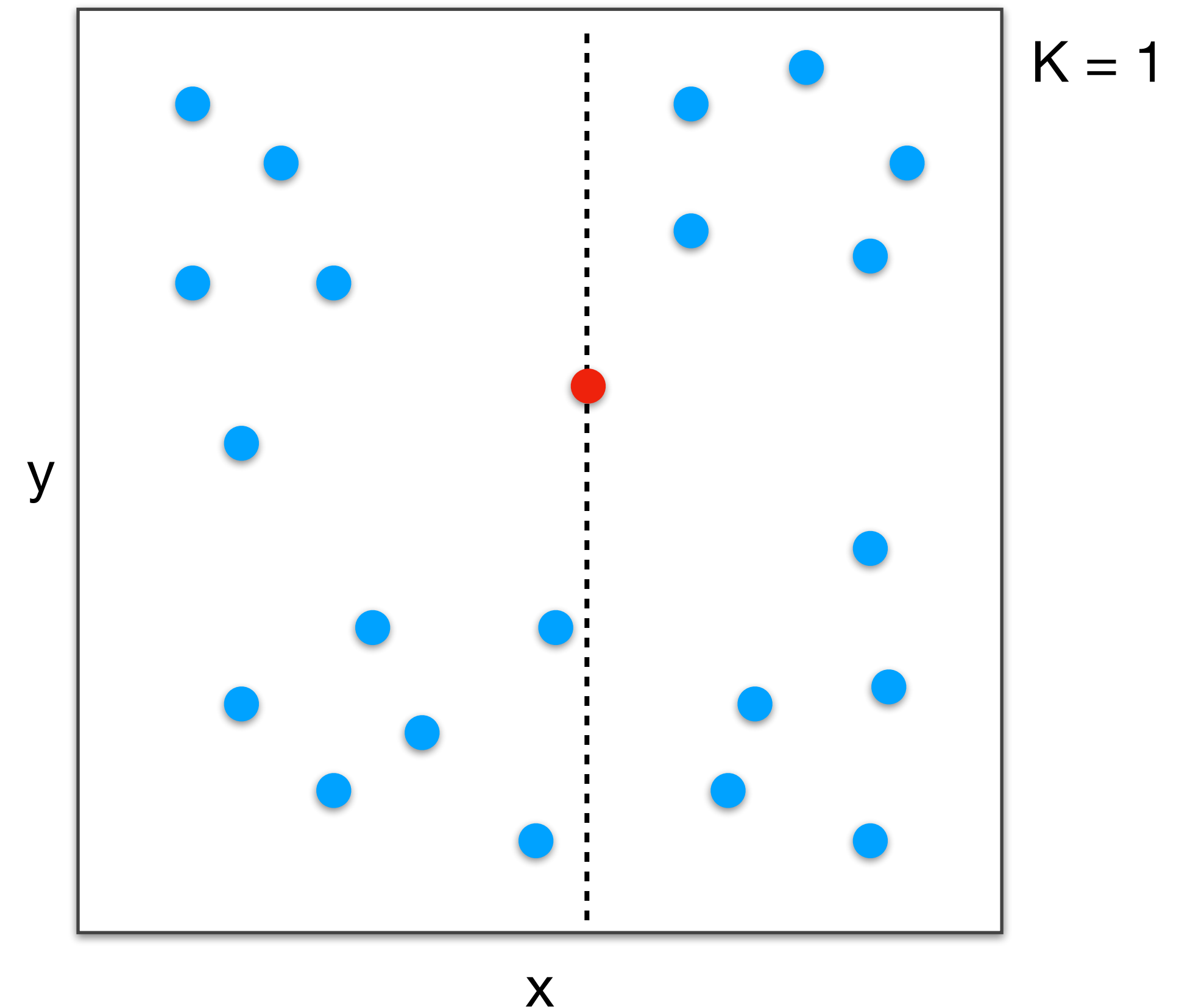
K-dimensional trees:

*For  $K$  times*

*Split one feature dimension into two partitions using medians.*

 indices

2D-features toy case



# KD Trees

How to reduce complexity?

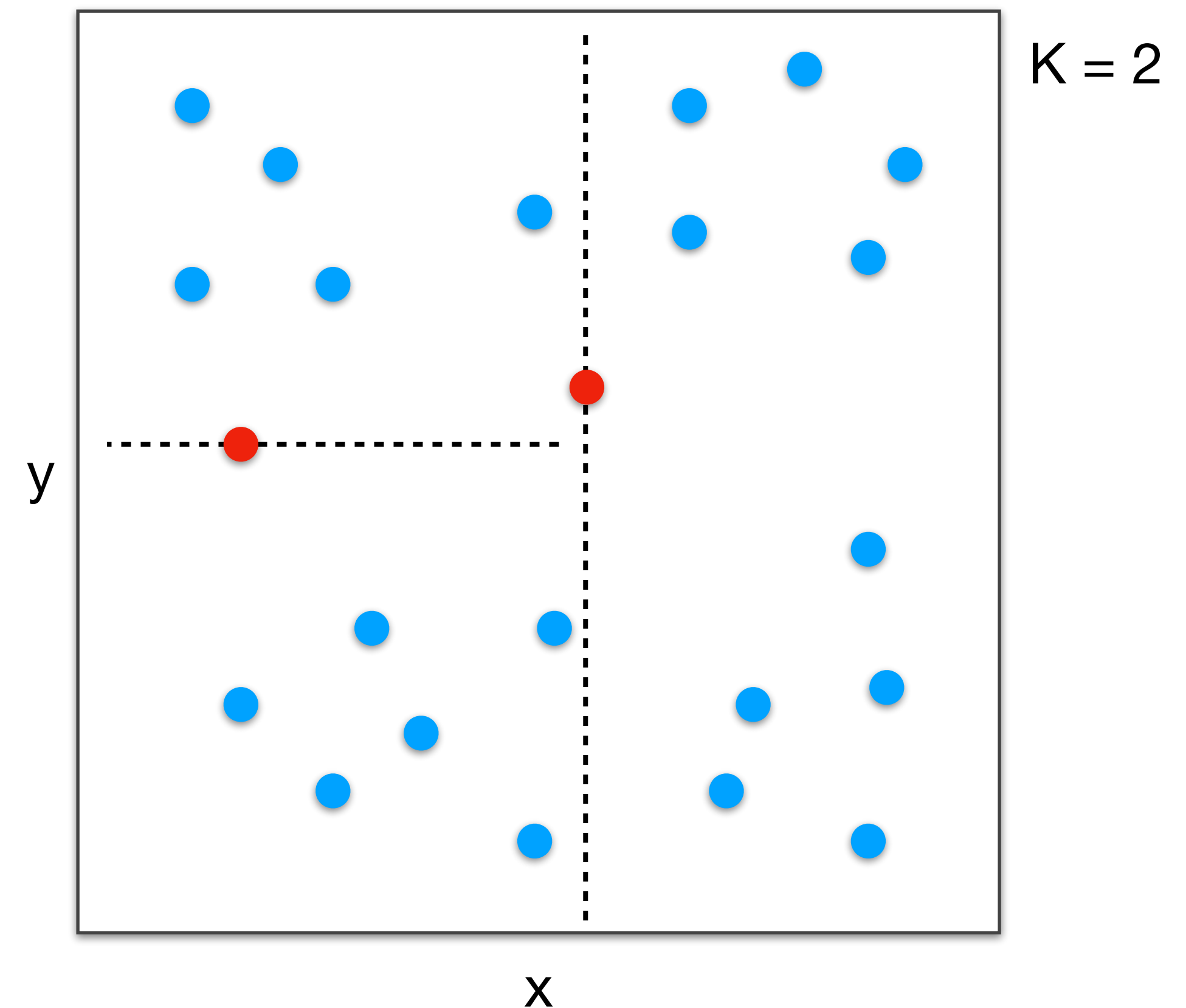
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2D-features toy case



# KD Trees

How to reduce complexity?

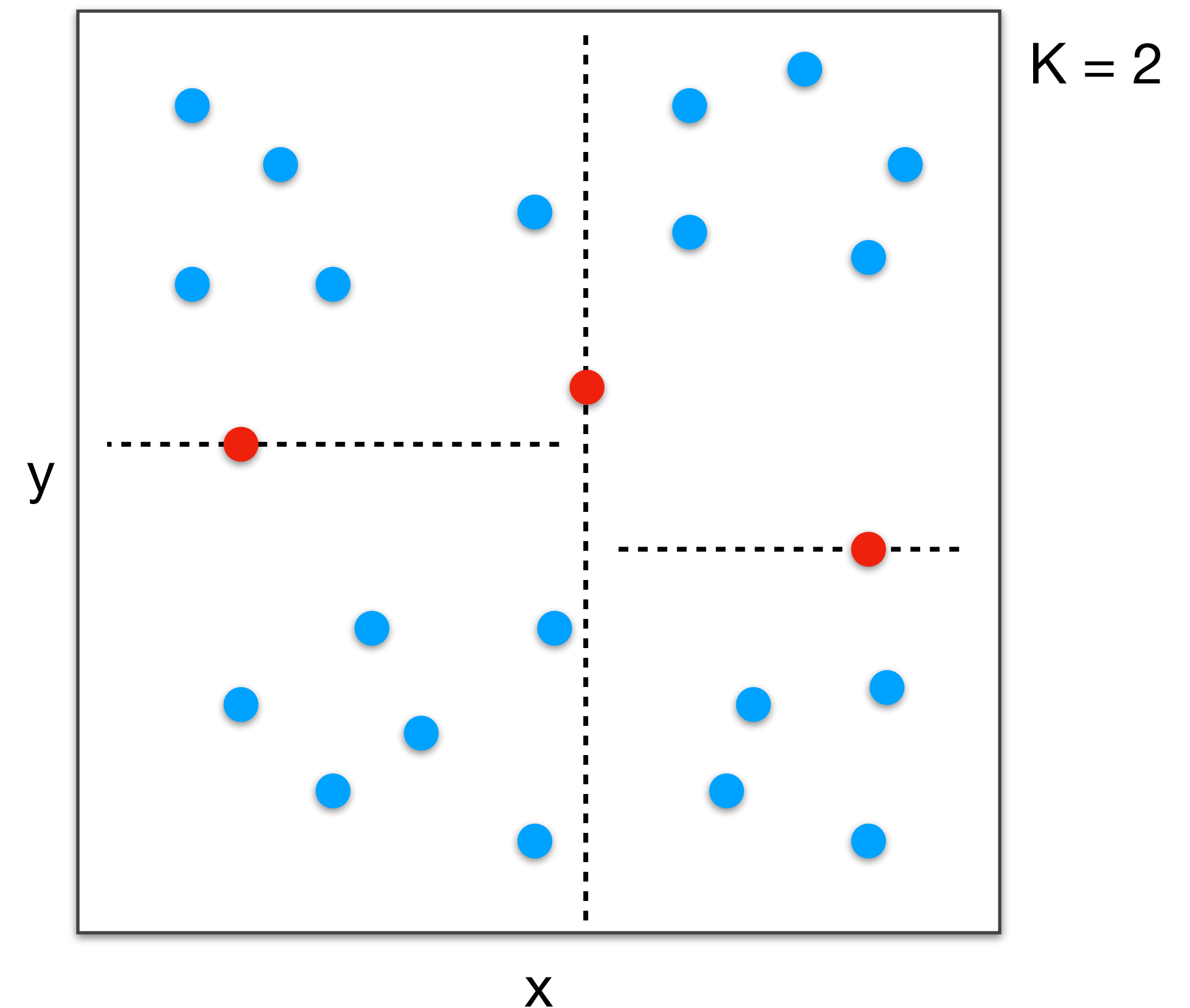
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 indices

2D-features toy case



# KD Trees

How to reduce complexity?

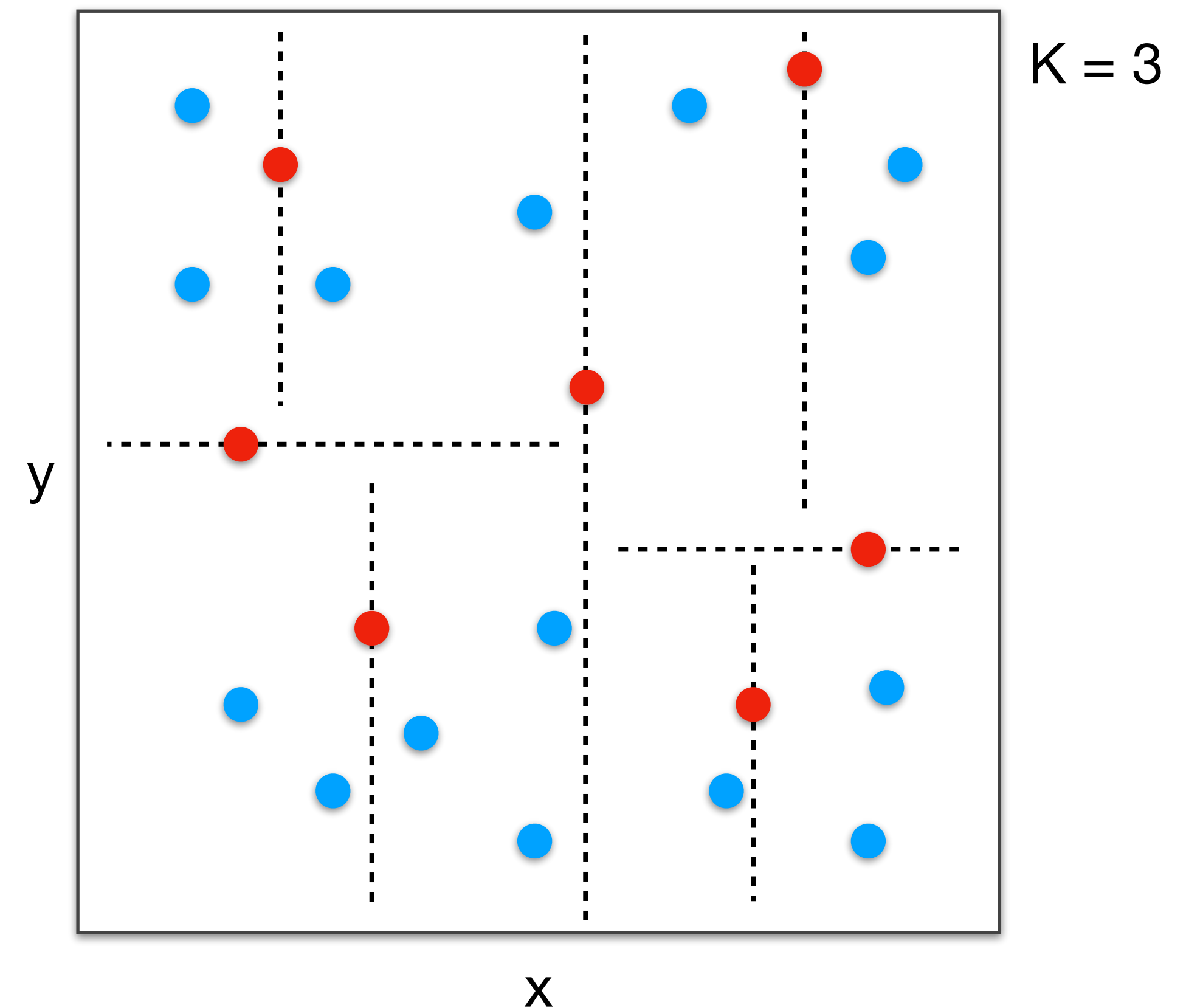
K-dimensional trees:

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 indices

2D-features toy case





# KD Trees

How to reduce complexity?

K-dimensional trees:

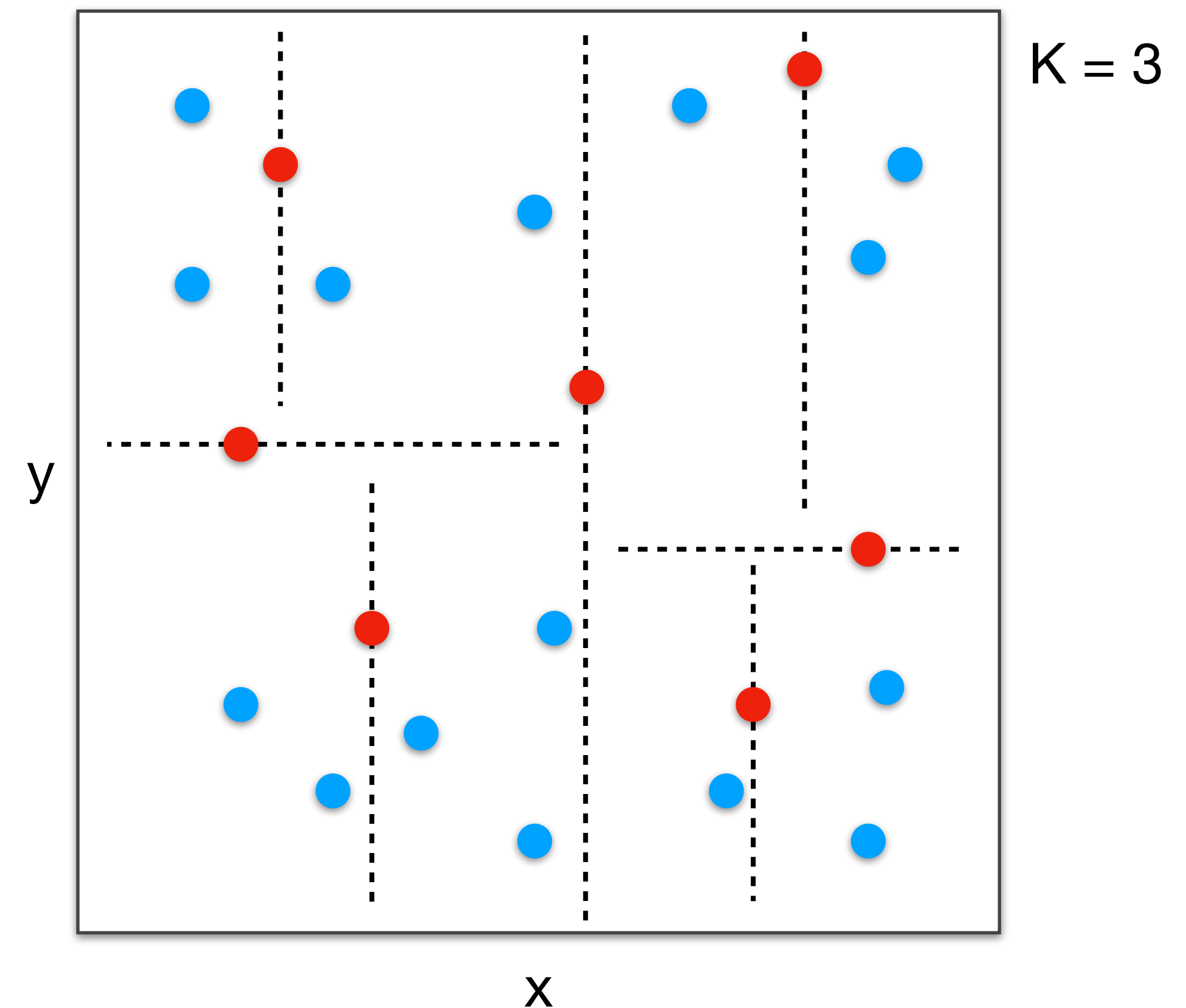
*For K times*

*Split one feature dimension into two partitions using medians.*

Complexity to build:  $O(n \log(n))$

Building is *offline*: i.e., it does not happen at feature querying time.

2D-features toy case



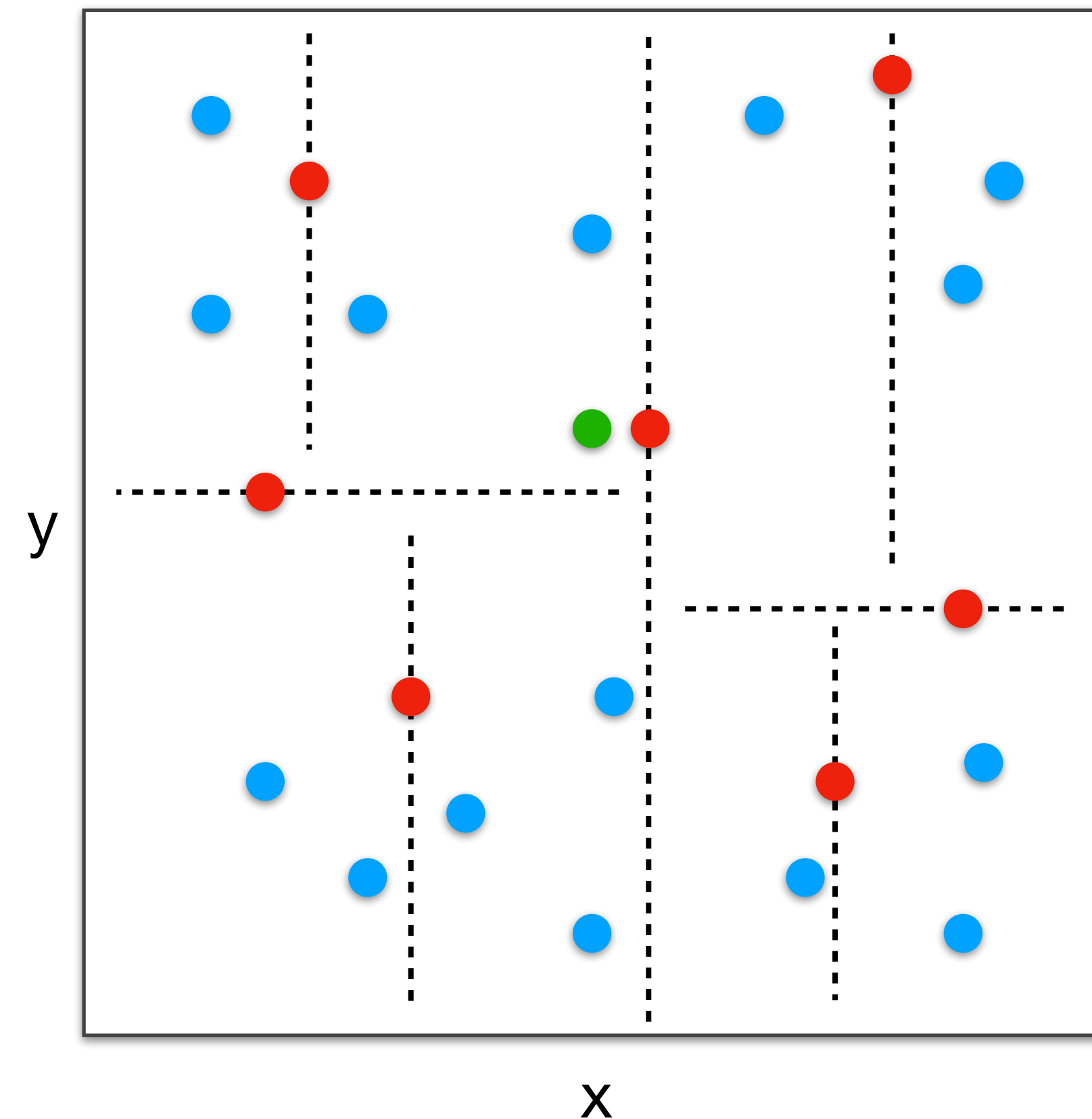
# KD Trees

How to reduce complexity?

How to obtain 3-nearest neighbors?

 query

2D-features toy case

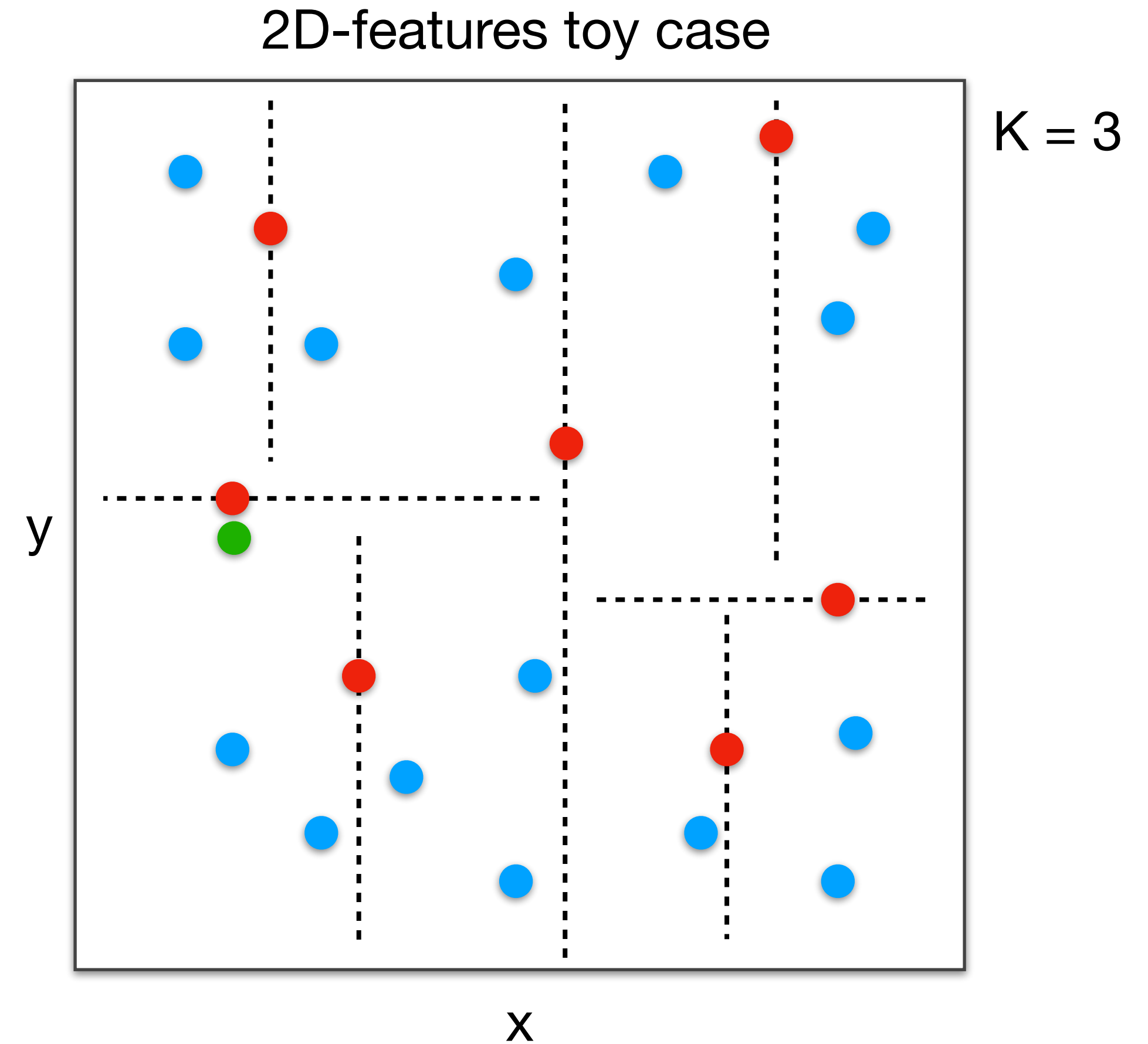


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How to reduce complexity?

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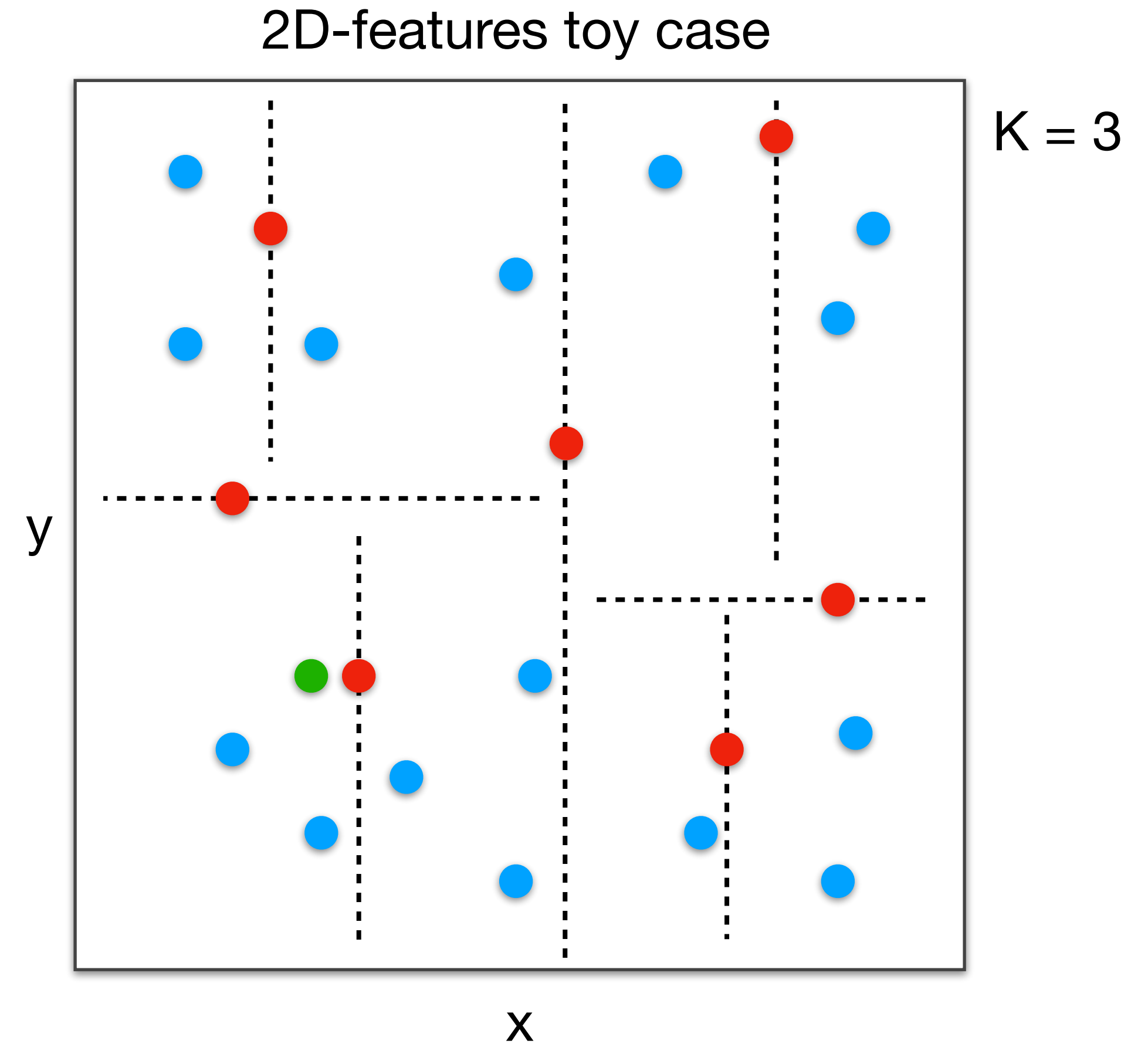


# KD Trees

How to reduce complexity?

How to obtain 3-nearest neighbors?

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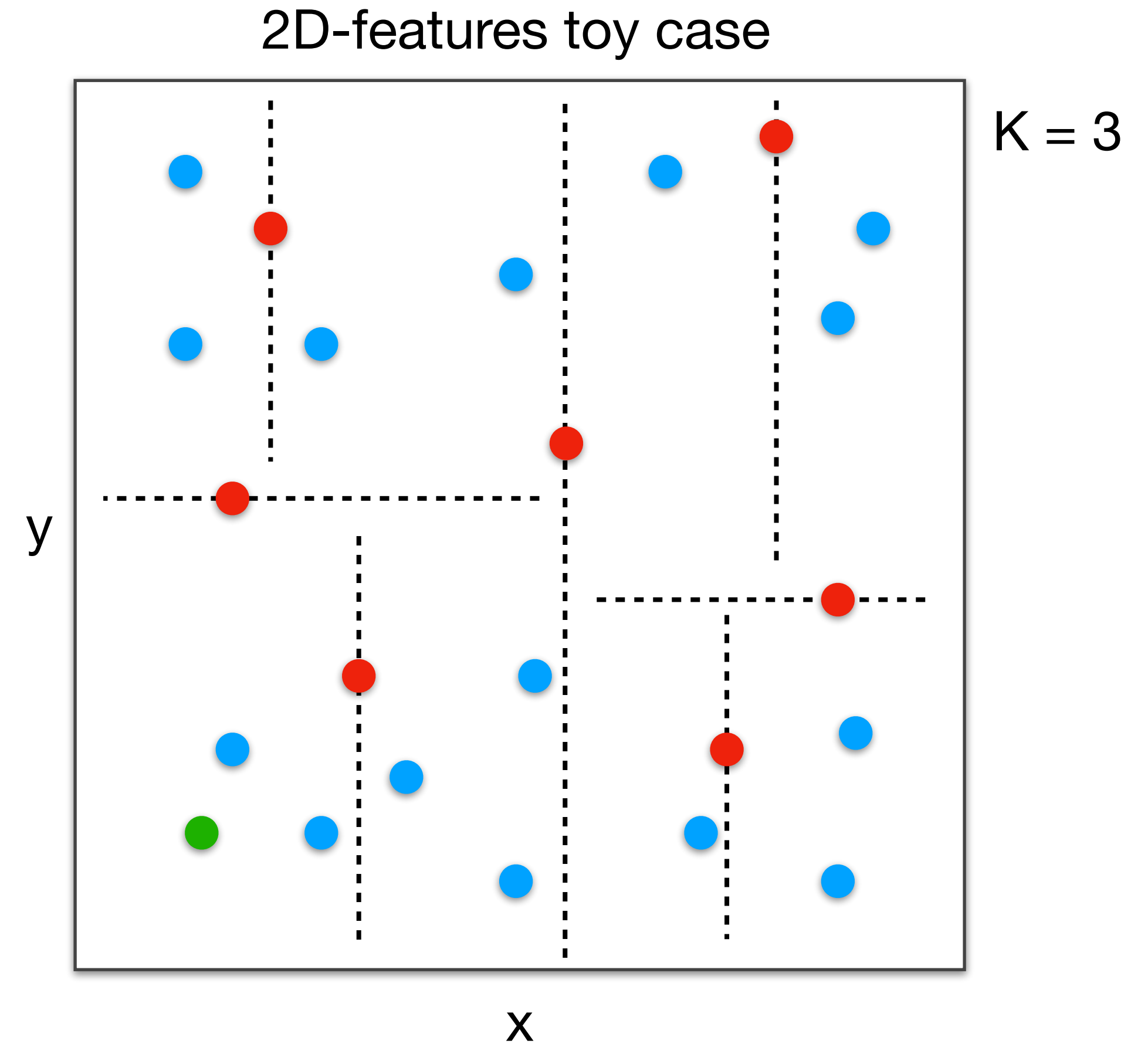


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How to reduce complexity?

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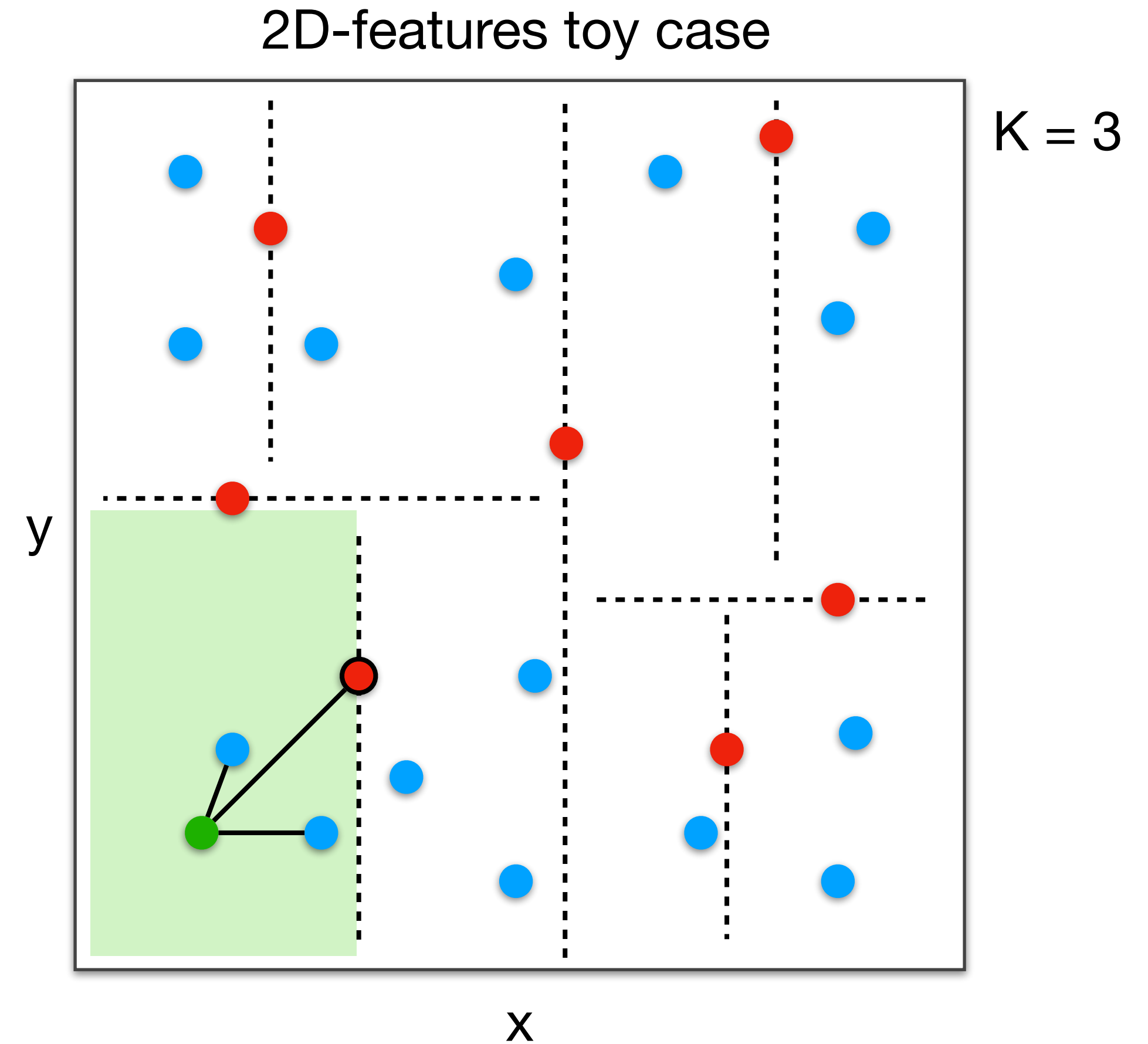


# KD Trees

How to reduce complexity?

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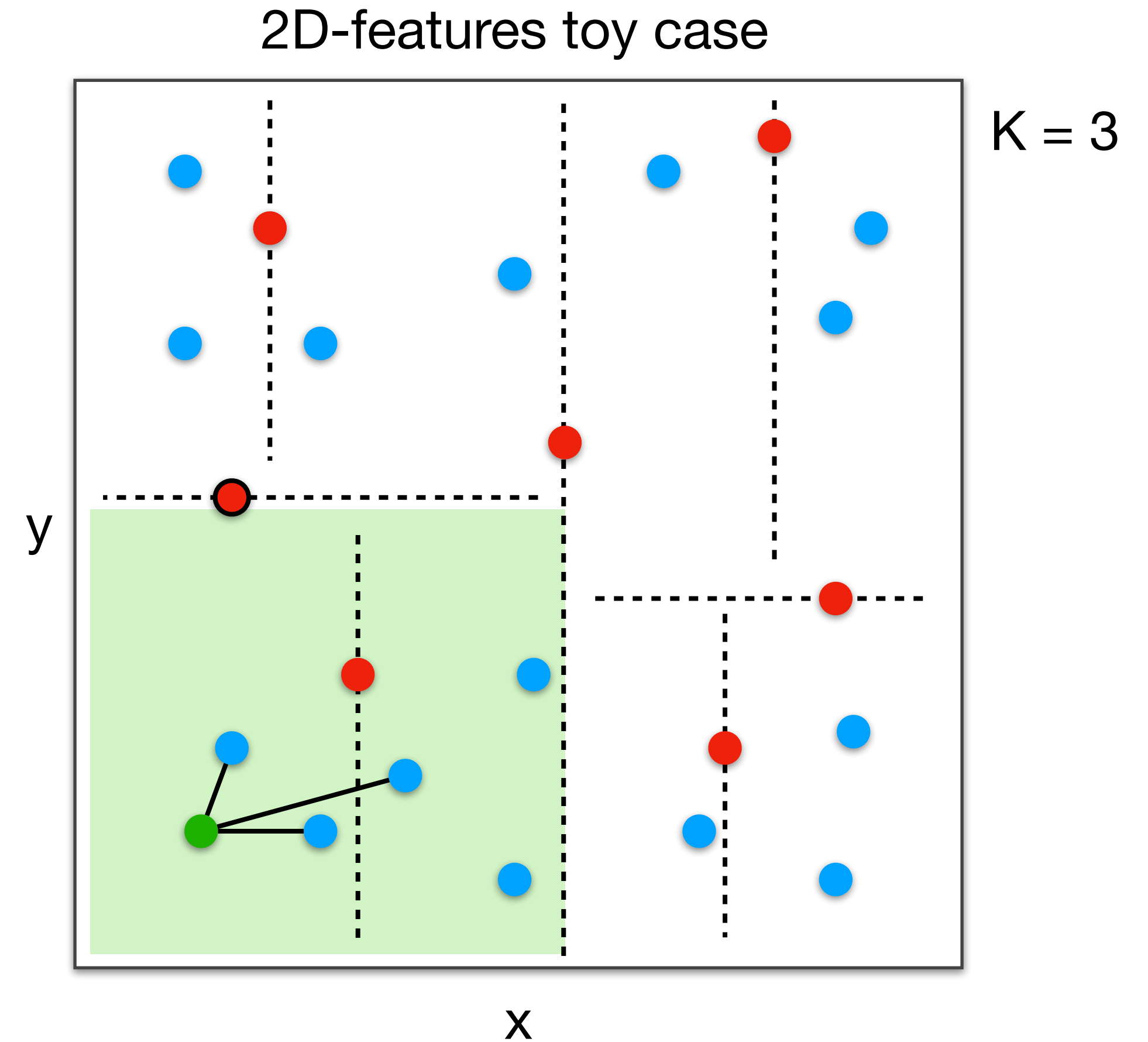


# KD Trees

How to reduce complexity?

How to obtain 3-nearest neighbors?

 query



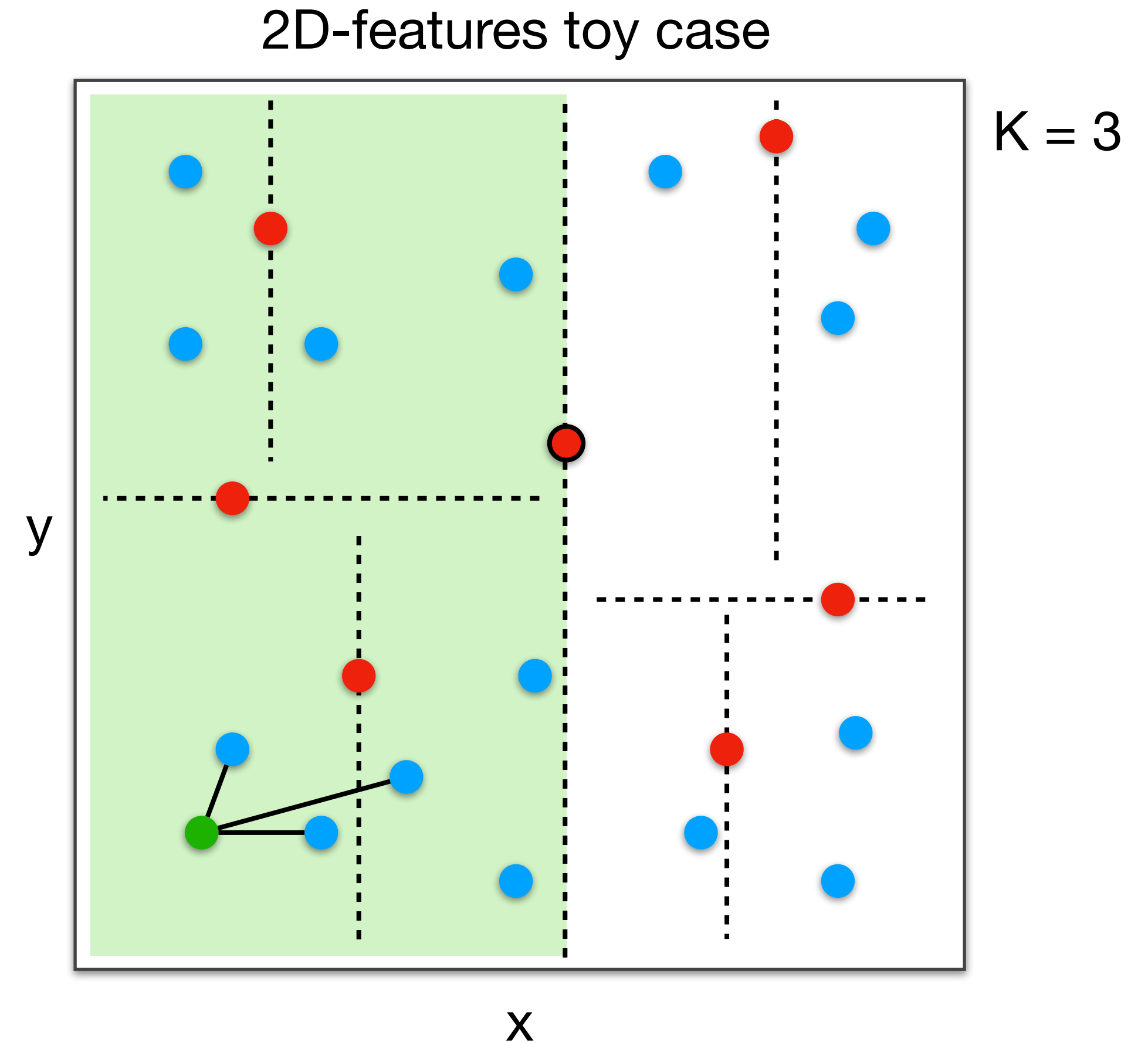
# KD Trees

How to reduce complexity?

How to obtain 3-nearest neighbors?

● query

No changes in 3-nearest, so stop.

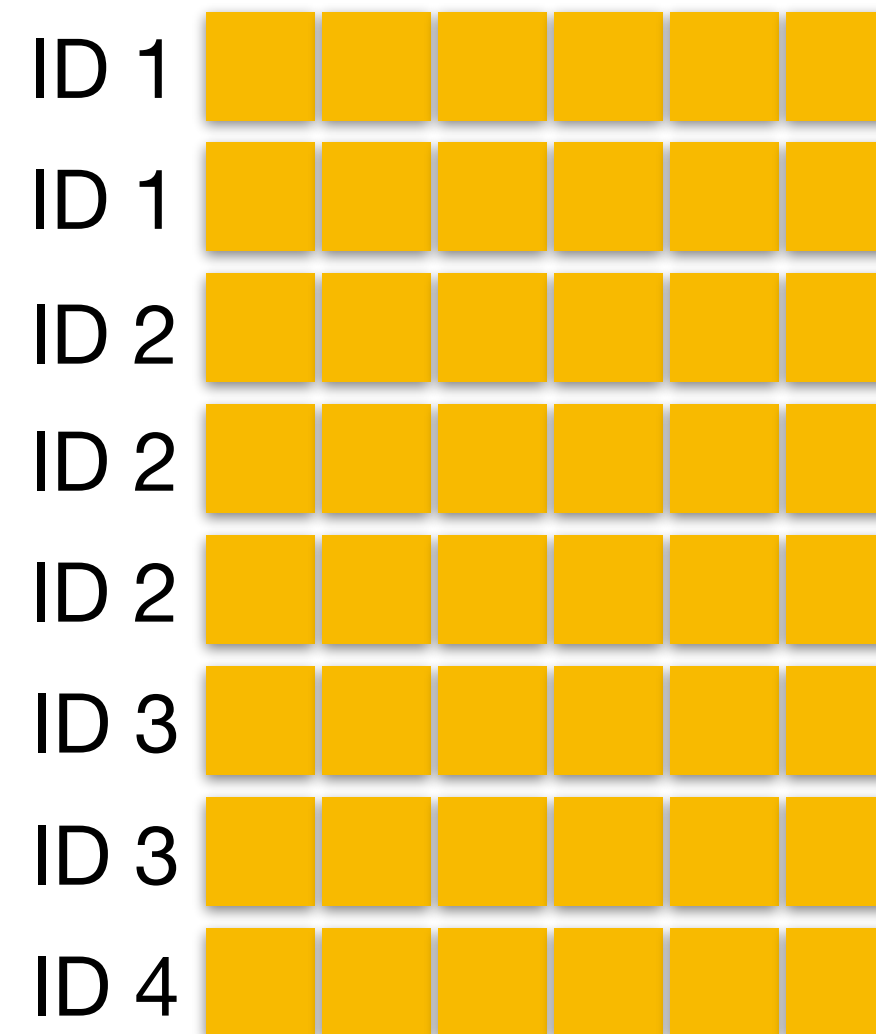




# Product Quantization

How to reduce size?

Toy Case (6D features, reality: 512D for faces)



...

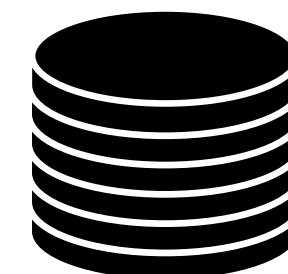


$P$  people

$M$  features



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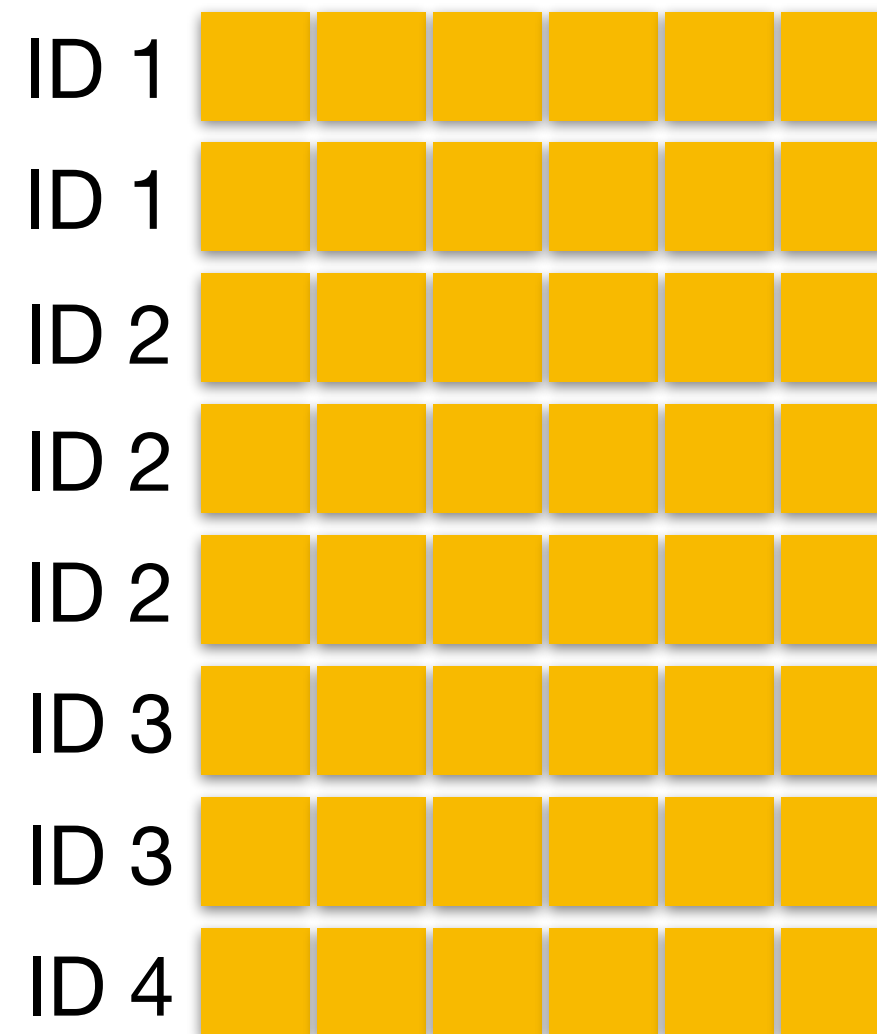
# Product Quantization

How to reduce size?

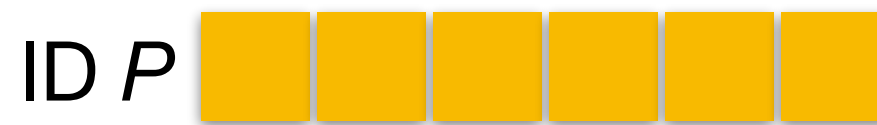
State-of-the-art feature indexing.

1. Start with a **coarse quantizer**.

Toy Case (6D features, reality: 512D for faces)



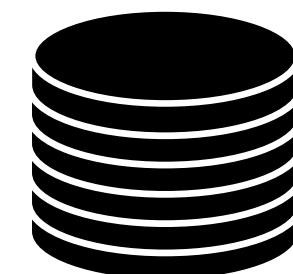
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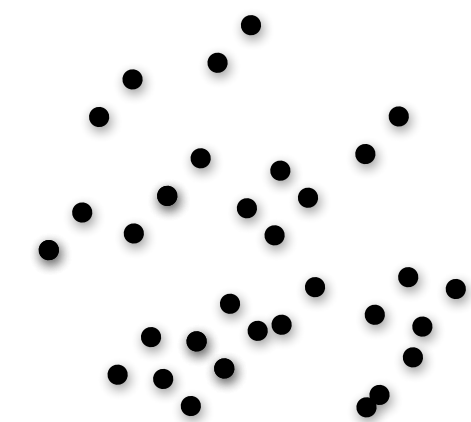
$P$  people

$M$  features

50



coarse quantizer



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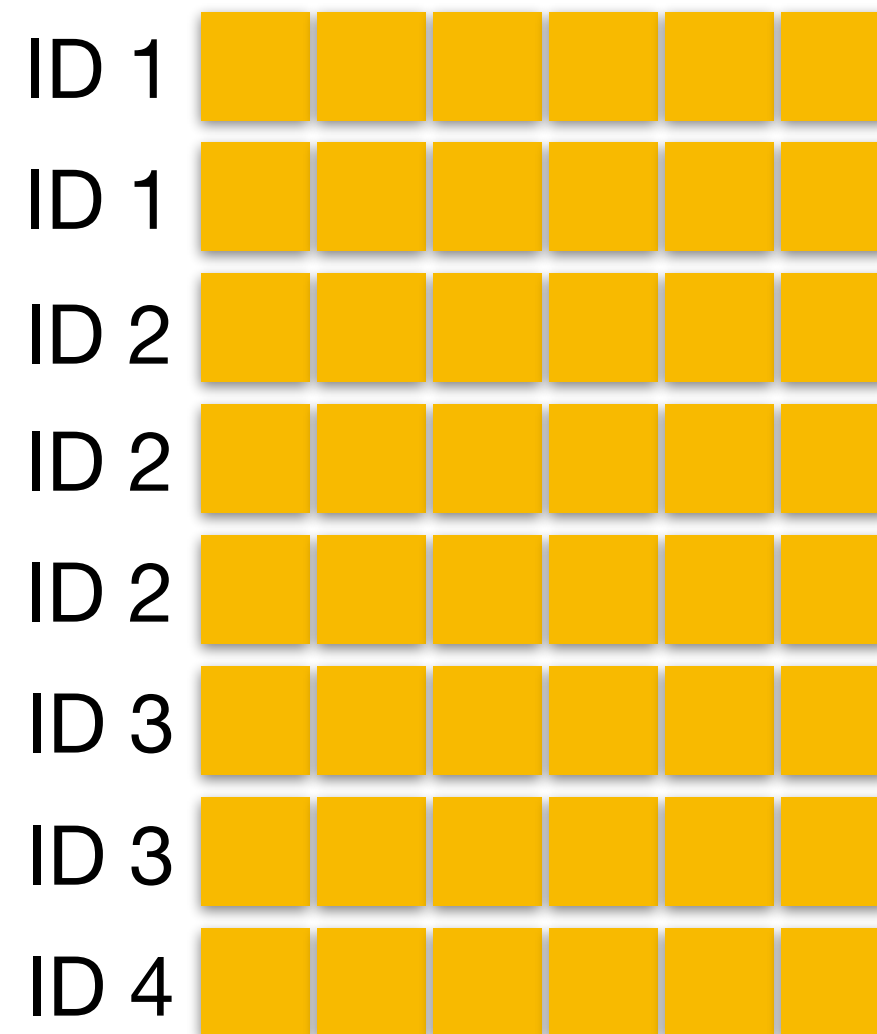
# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

1. Start with a **coarse quantizer**.

Toy Case (6D features, reality: 512D for faces)



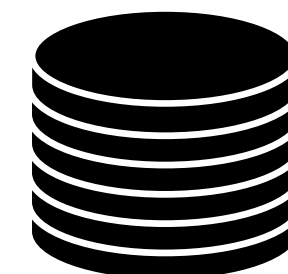
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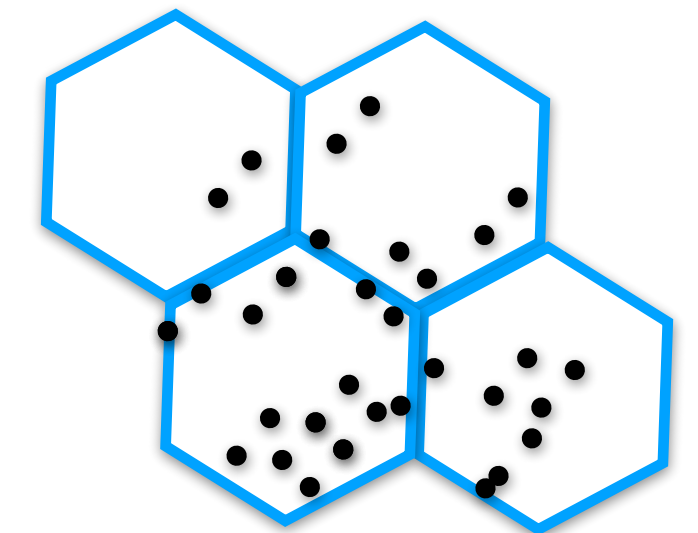
$P$  people

$M$  features

51



coarse quantizer



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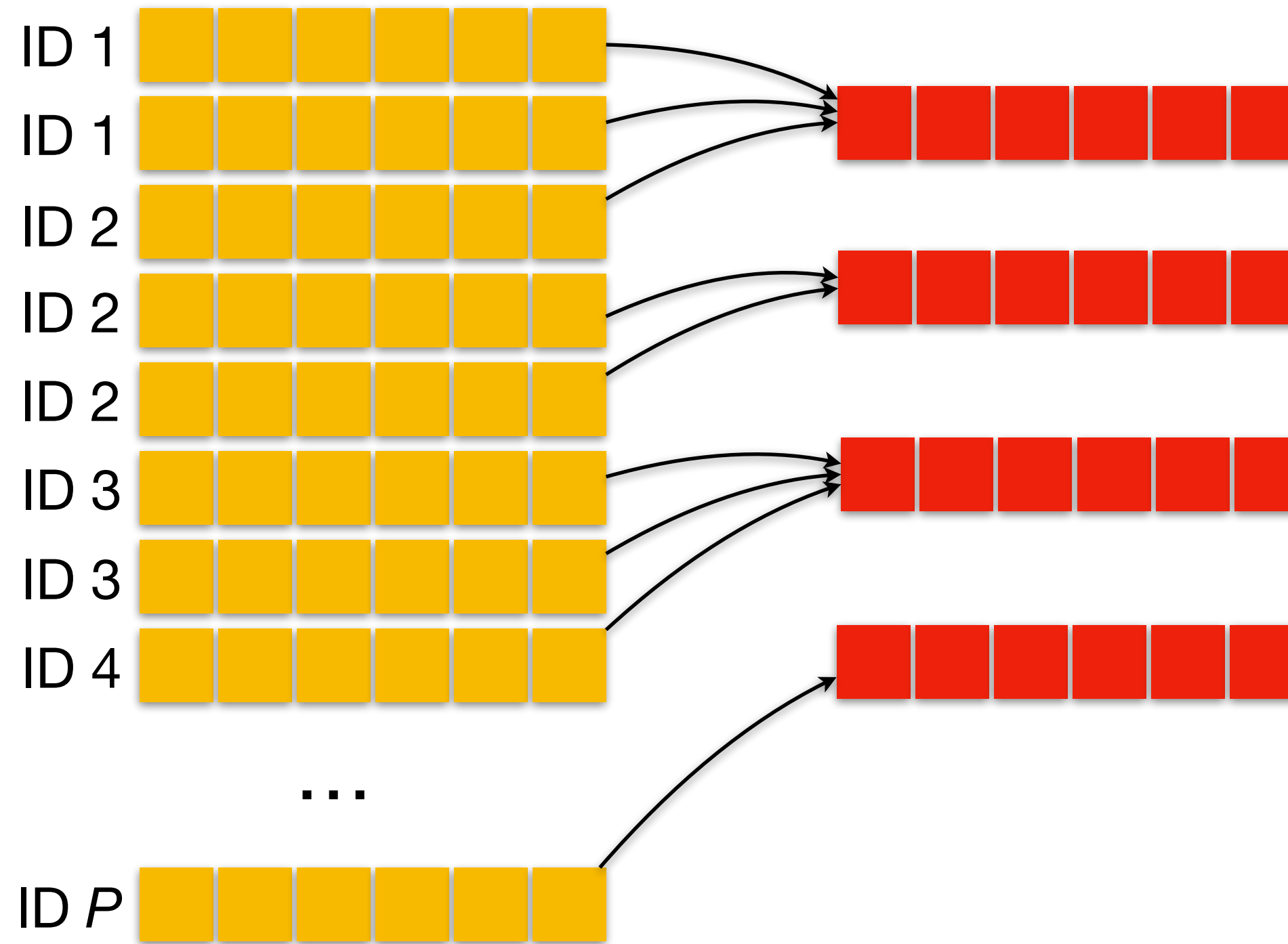
# Product Quantization

How to reduce size?

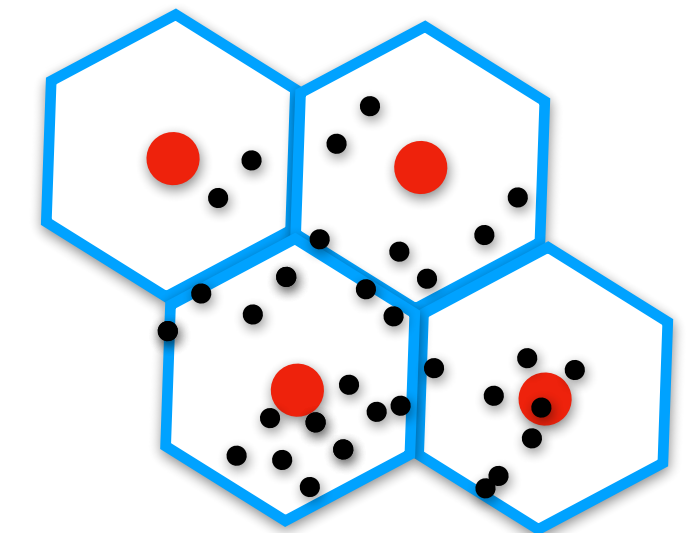
State-of-the-art feature indexing.

1. Start with a coarse quantizer.

Toy Case (6D features, reality: 512D for faces)

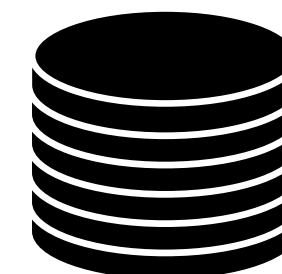


coarse quantizer



$P$  people

52



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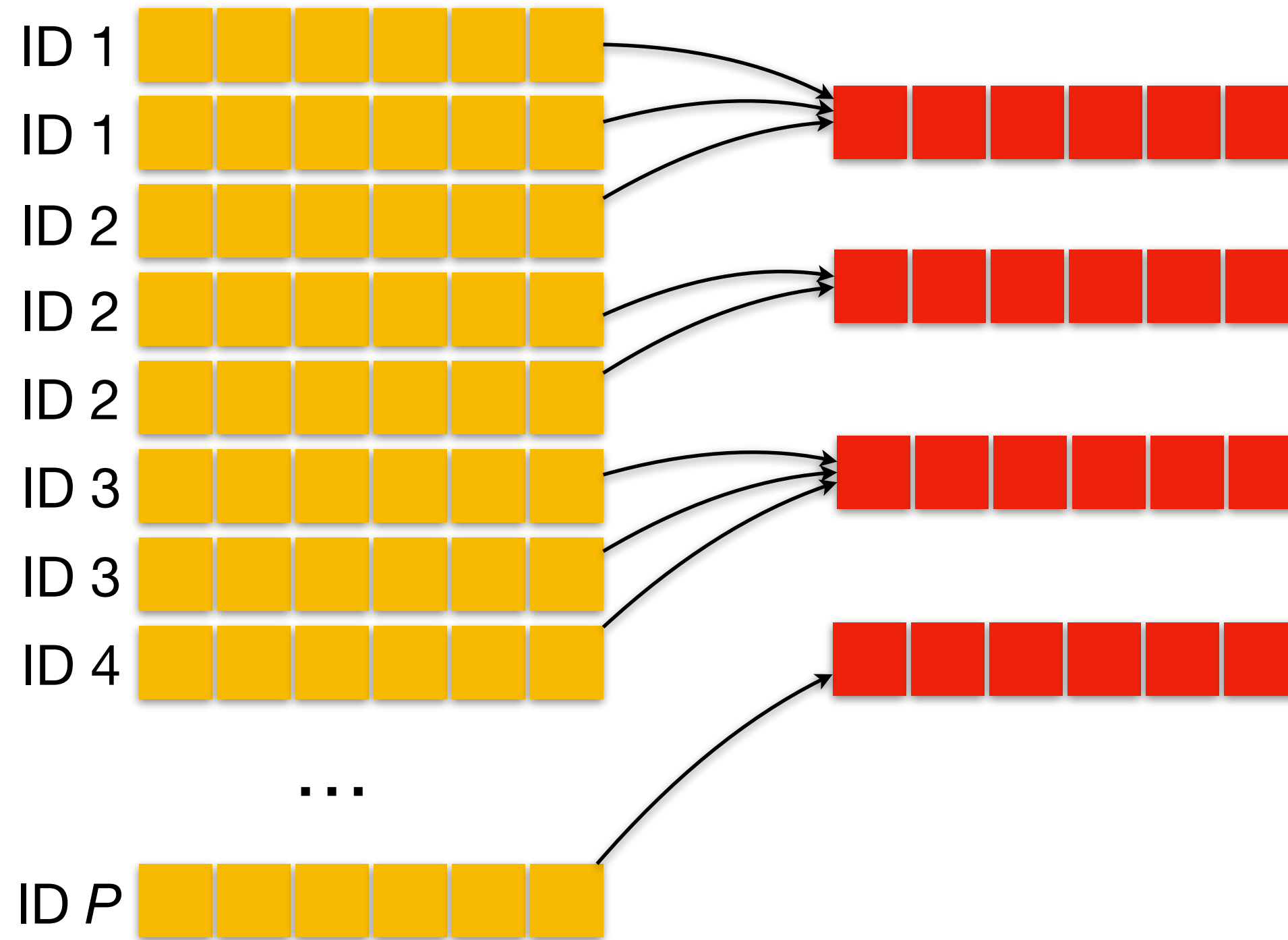
# Product Quantization

How to reduce size?

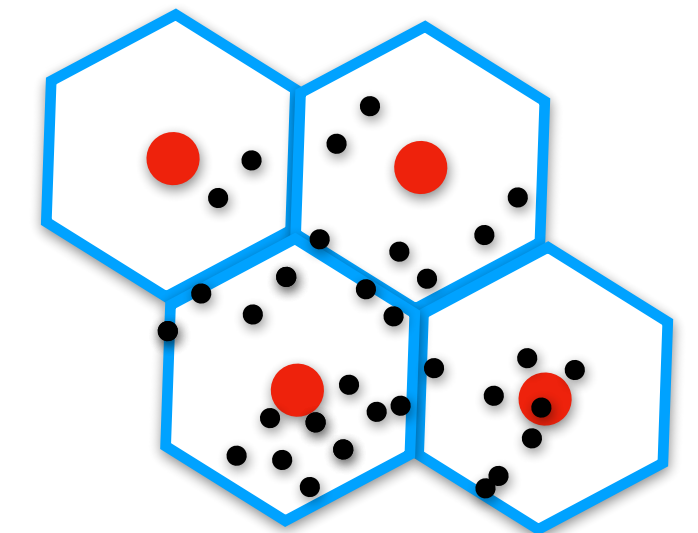
State-of-the-art feature indexing.

1. Start with a coarse quantizer.

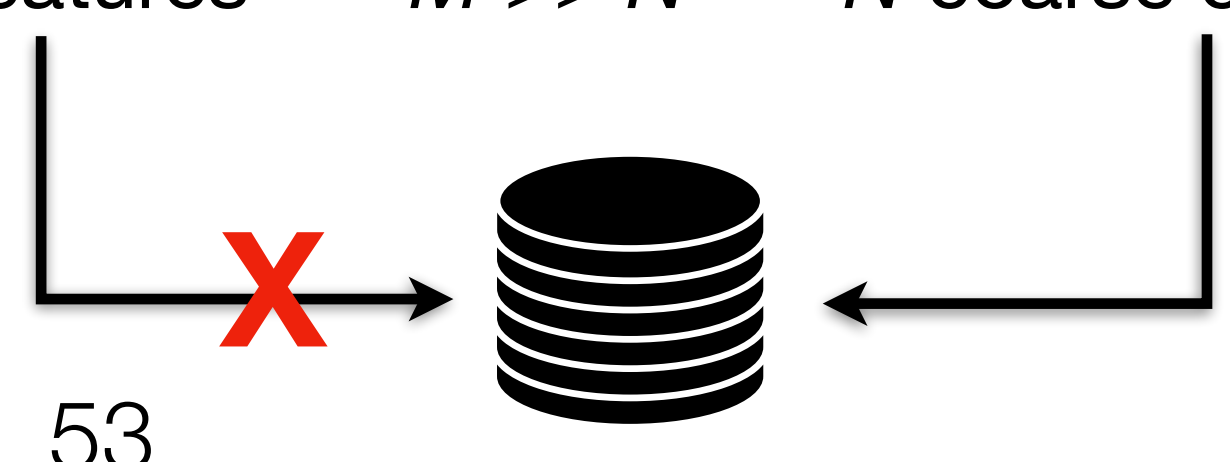
Toy Case (6D features, reality: 512D for faces)



coarse quantizer



$P$  people

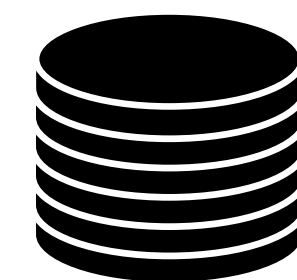
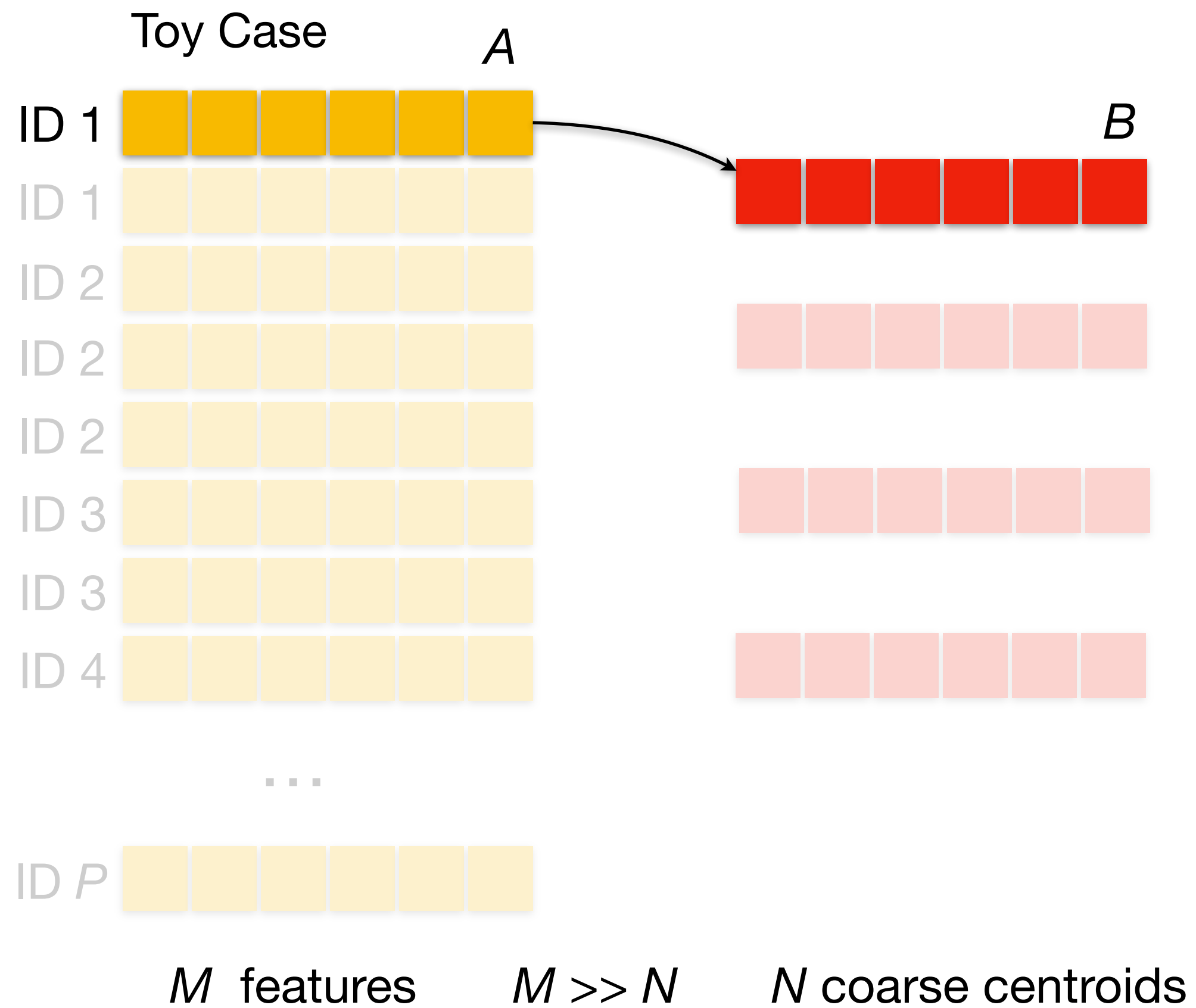


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

2. Compute **residuals** (differences) between features and their respective coarse centroids.

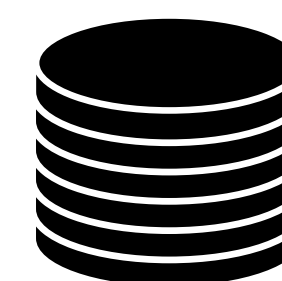
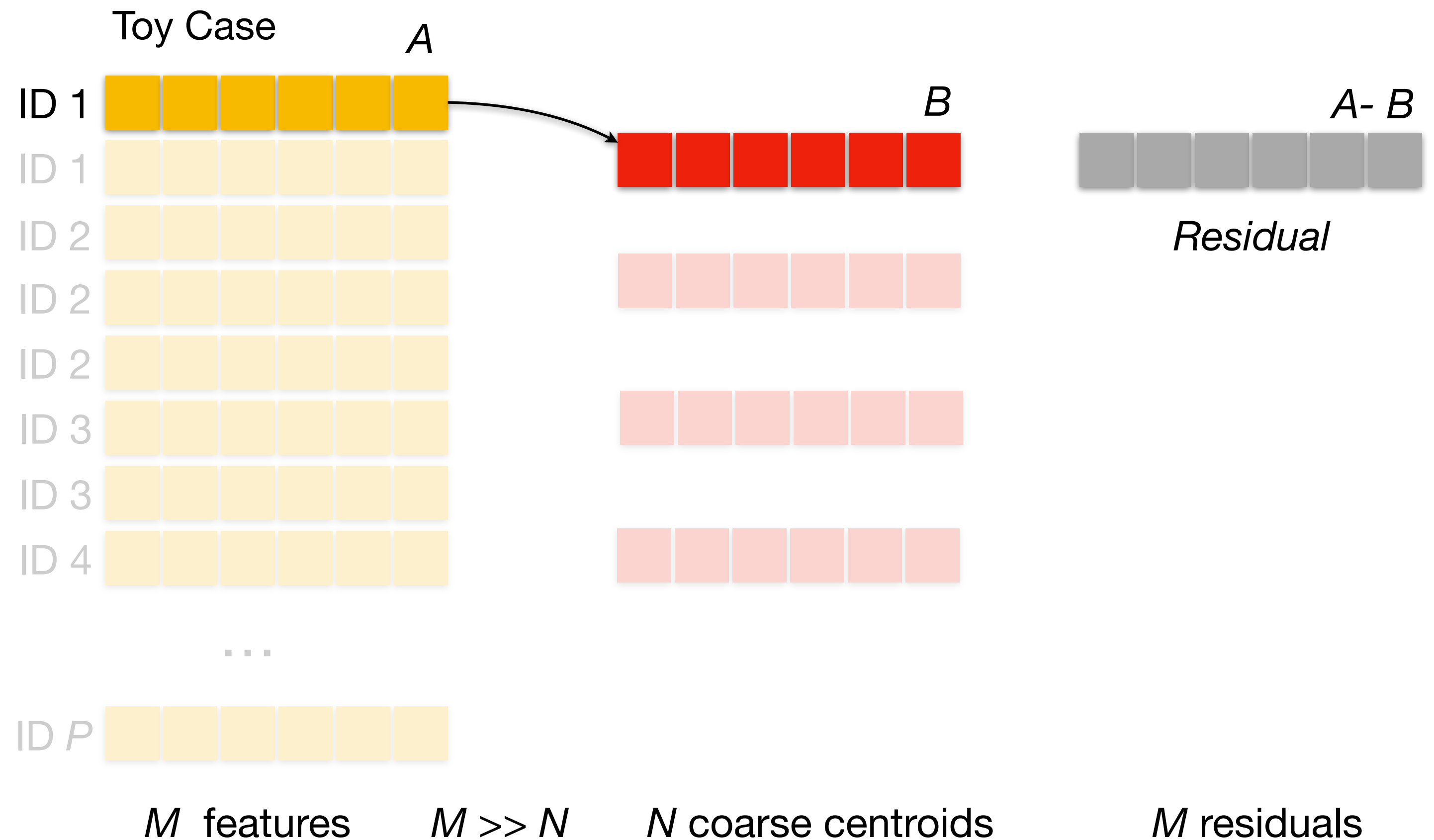


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

2. Compute **residuals** (differences) between features and their respective coarse centroids.

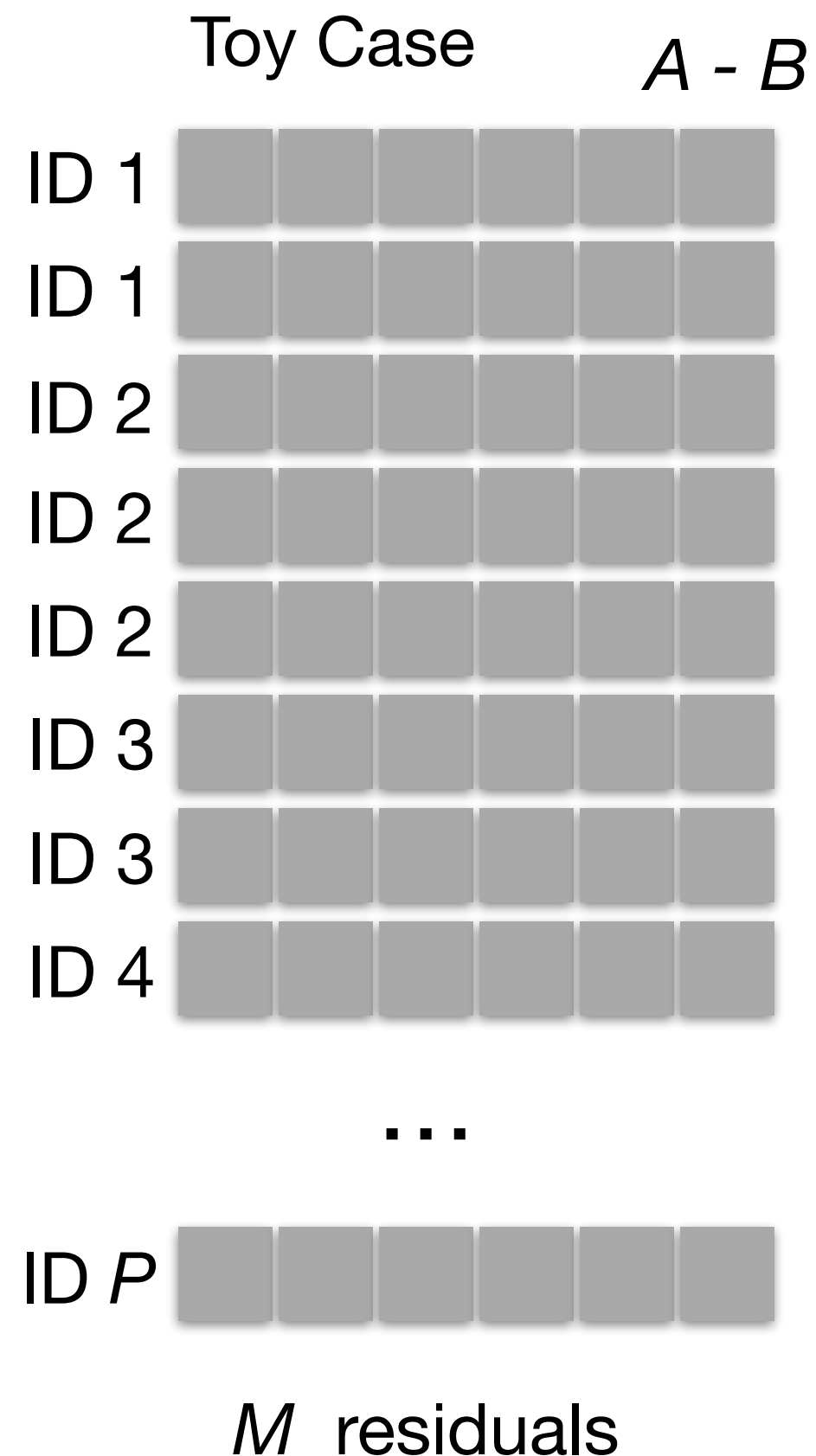


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

3. Reduce the dimensionality of residuals with **Product Quantization**.



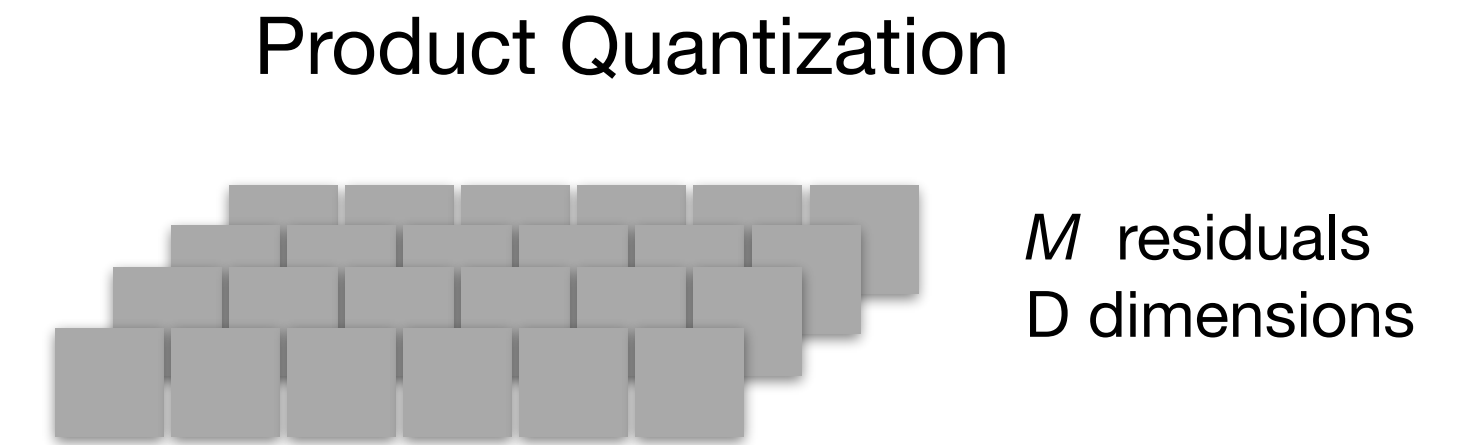
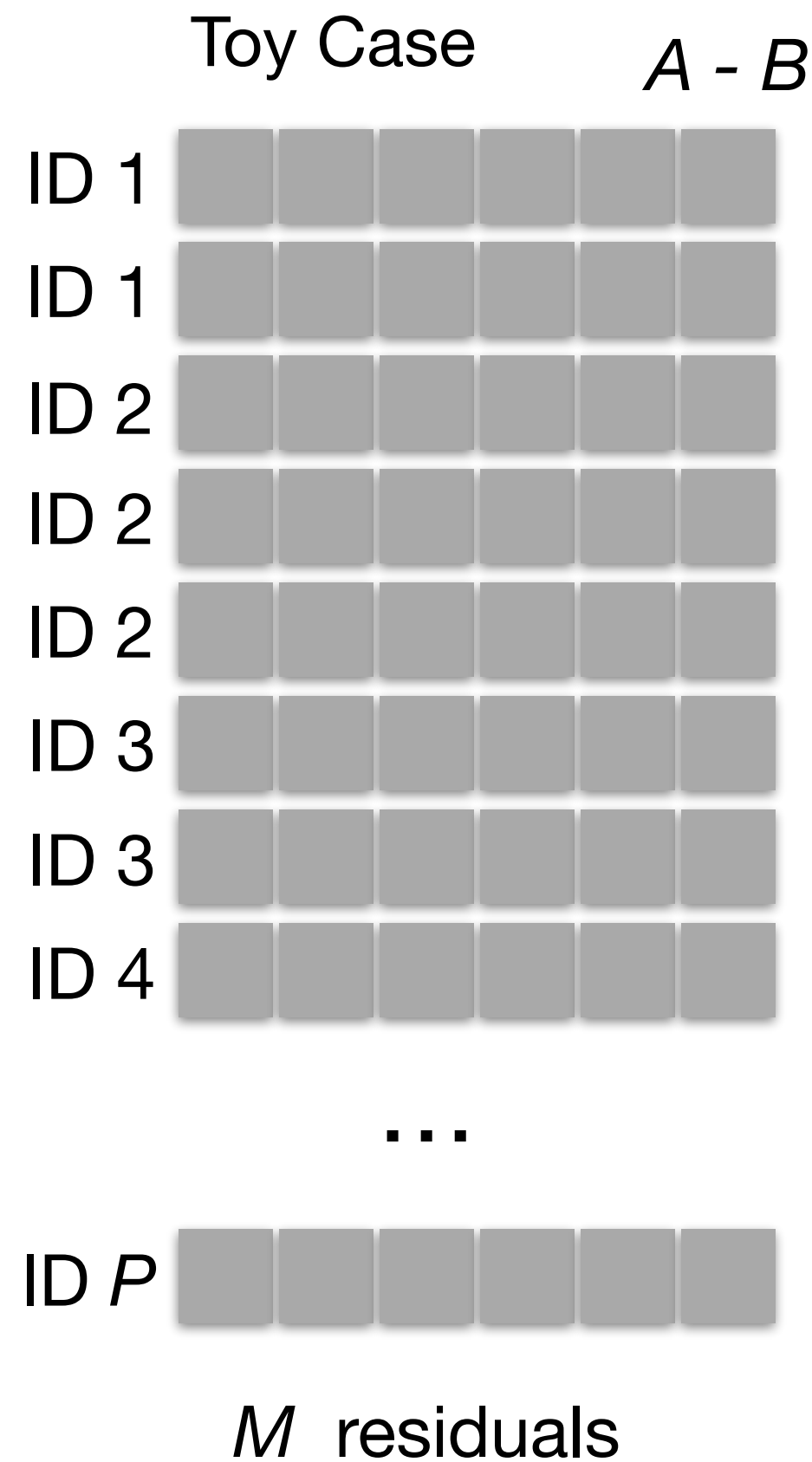


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

3. Reduce the dimensionality of residuals with **Product Quantization**.

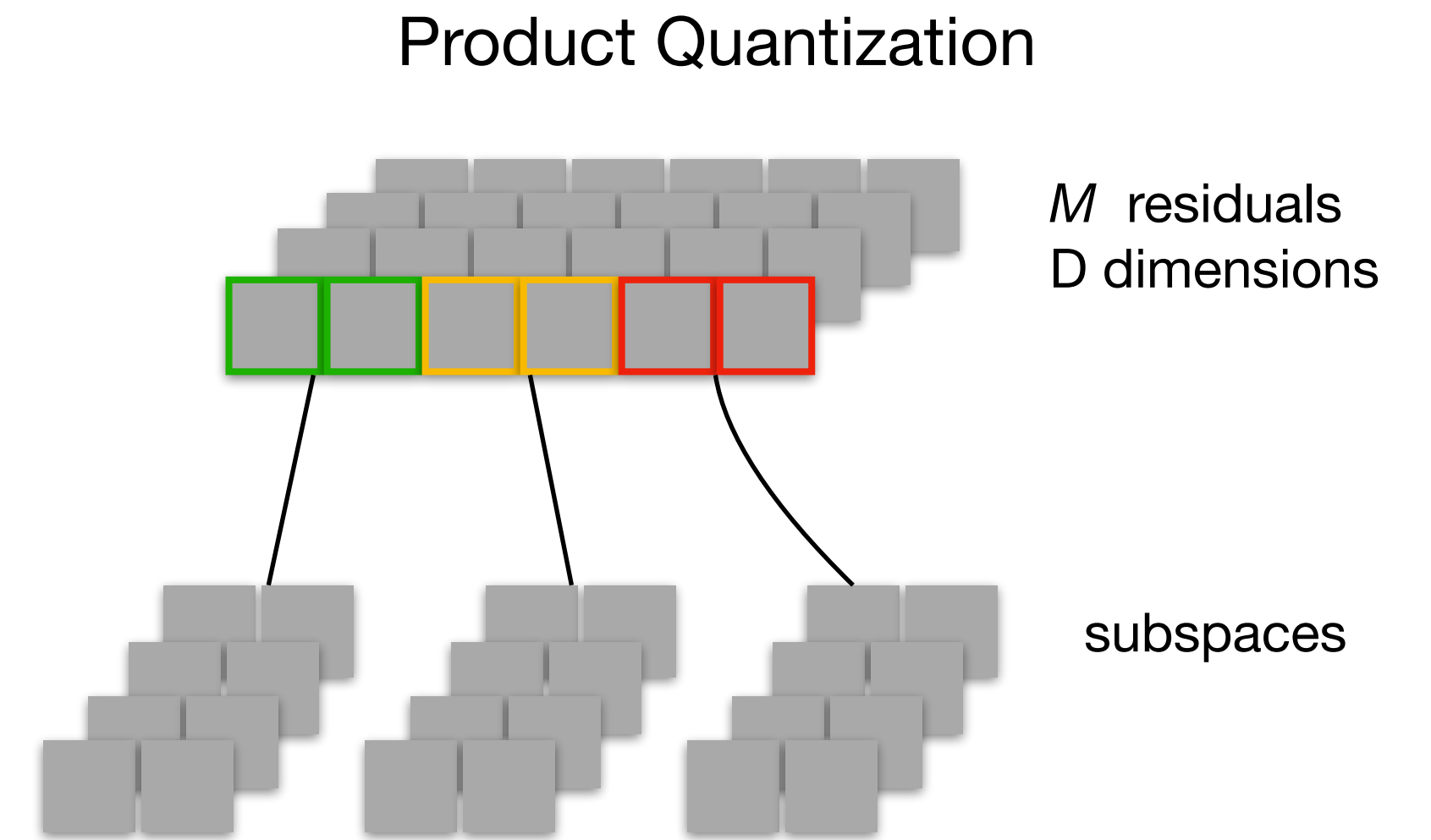
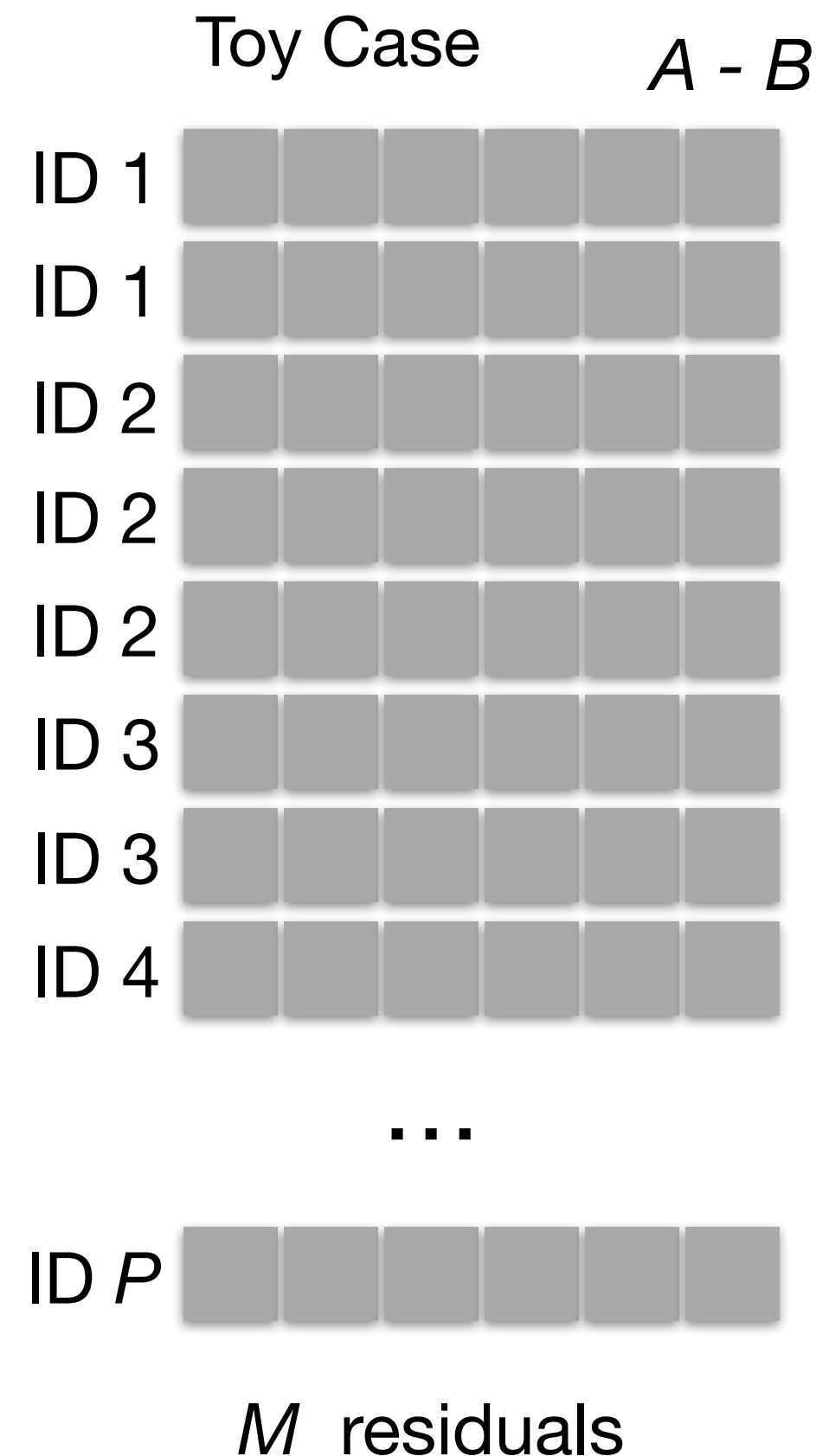


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

3. Reduce the dimensionality of residuals with **Product Quantization**.

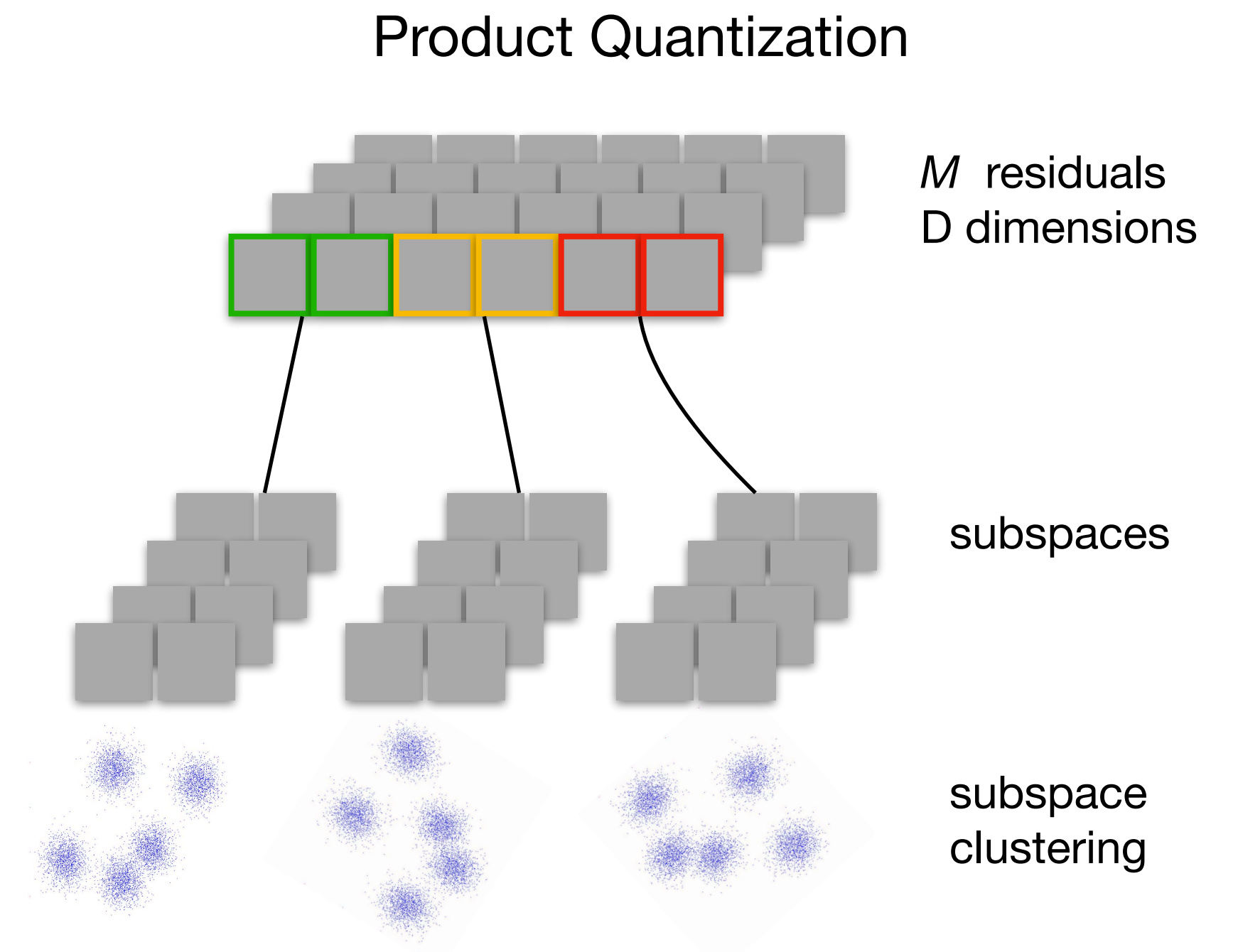
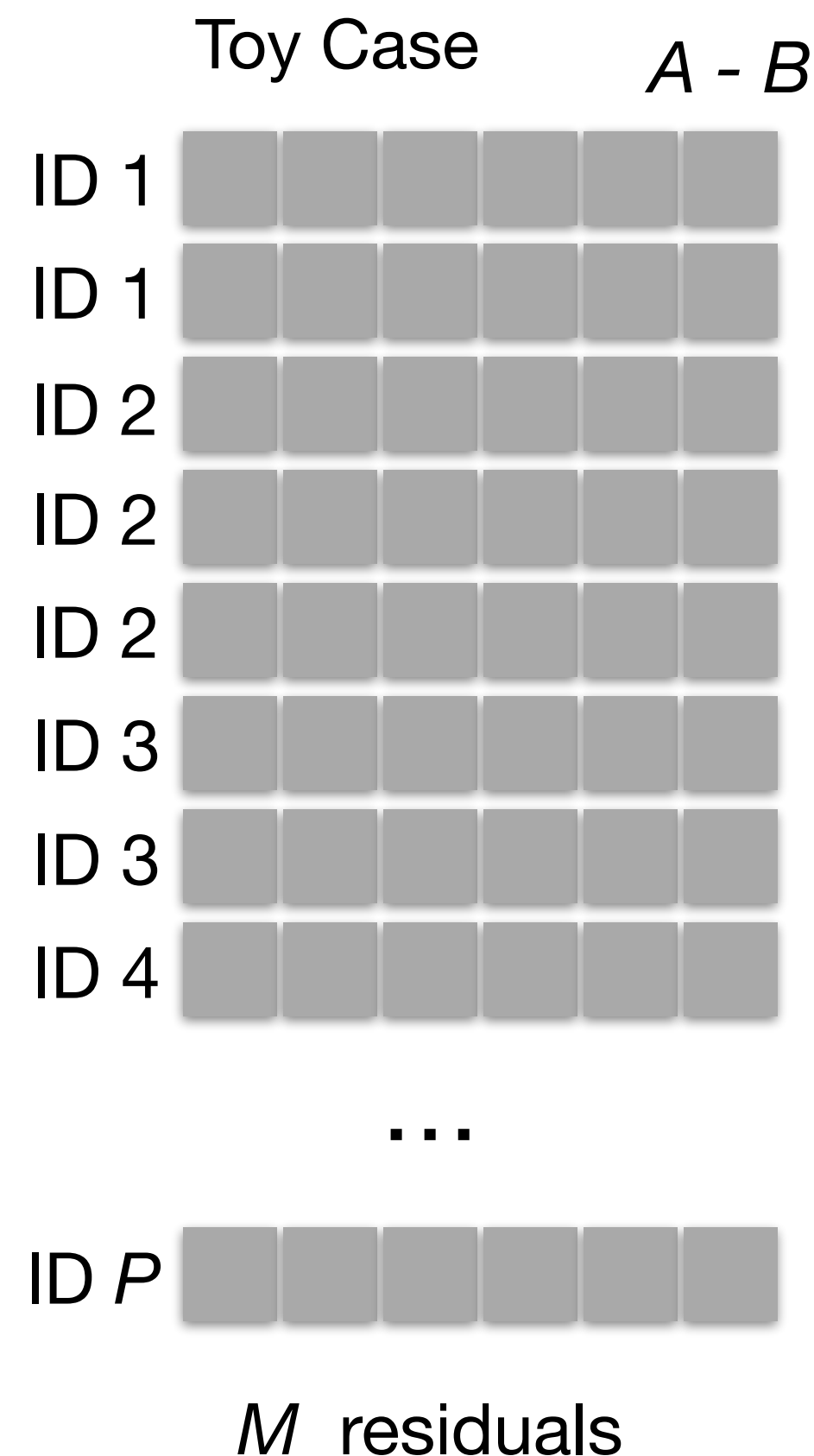


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

3. Reduce the dimensionality of residuals with **Product Quantization**.

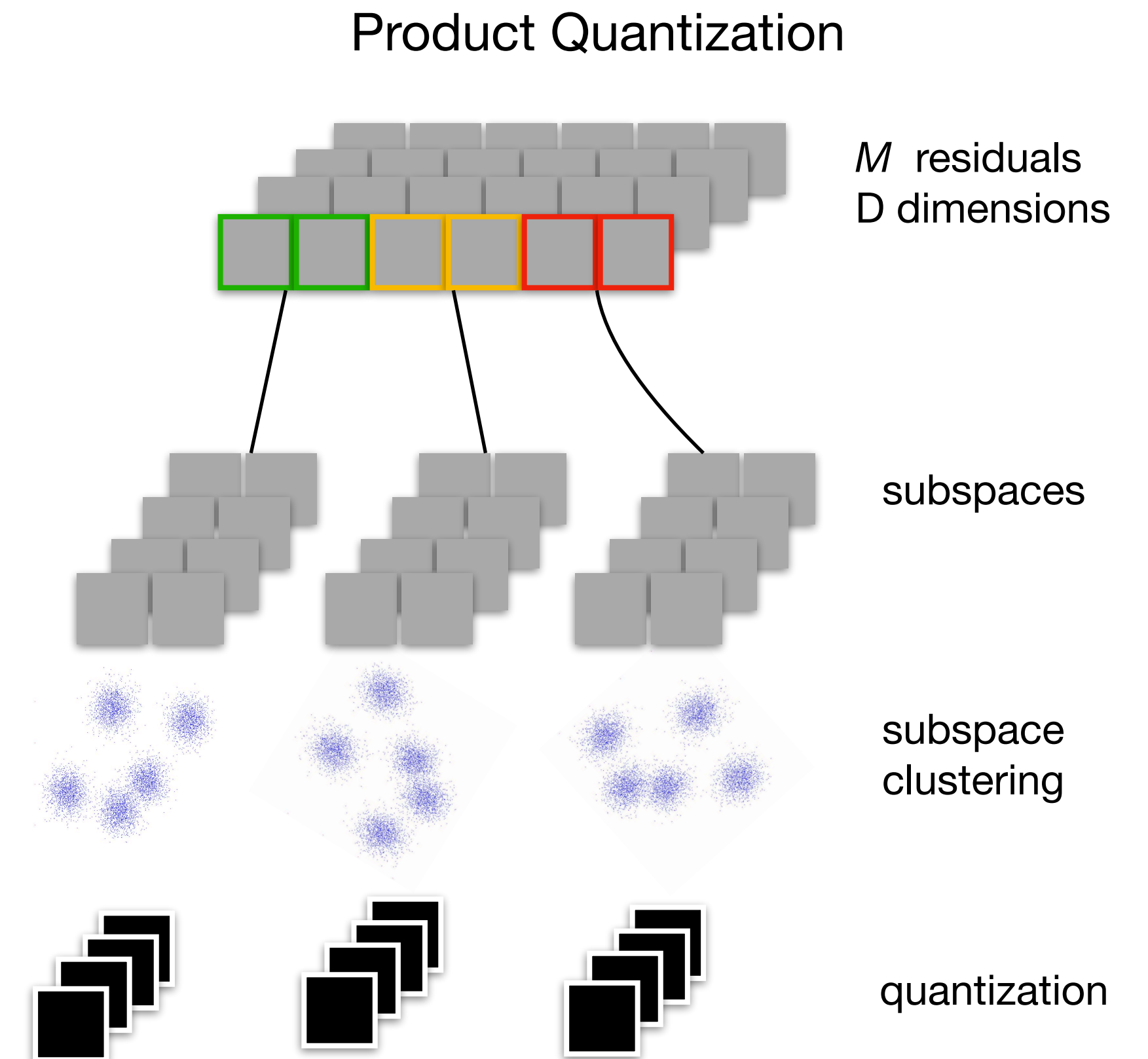
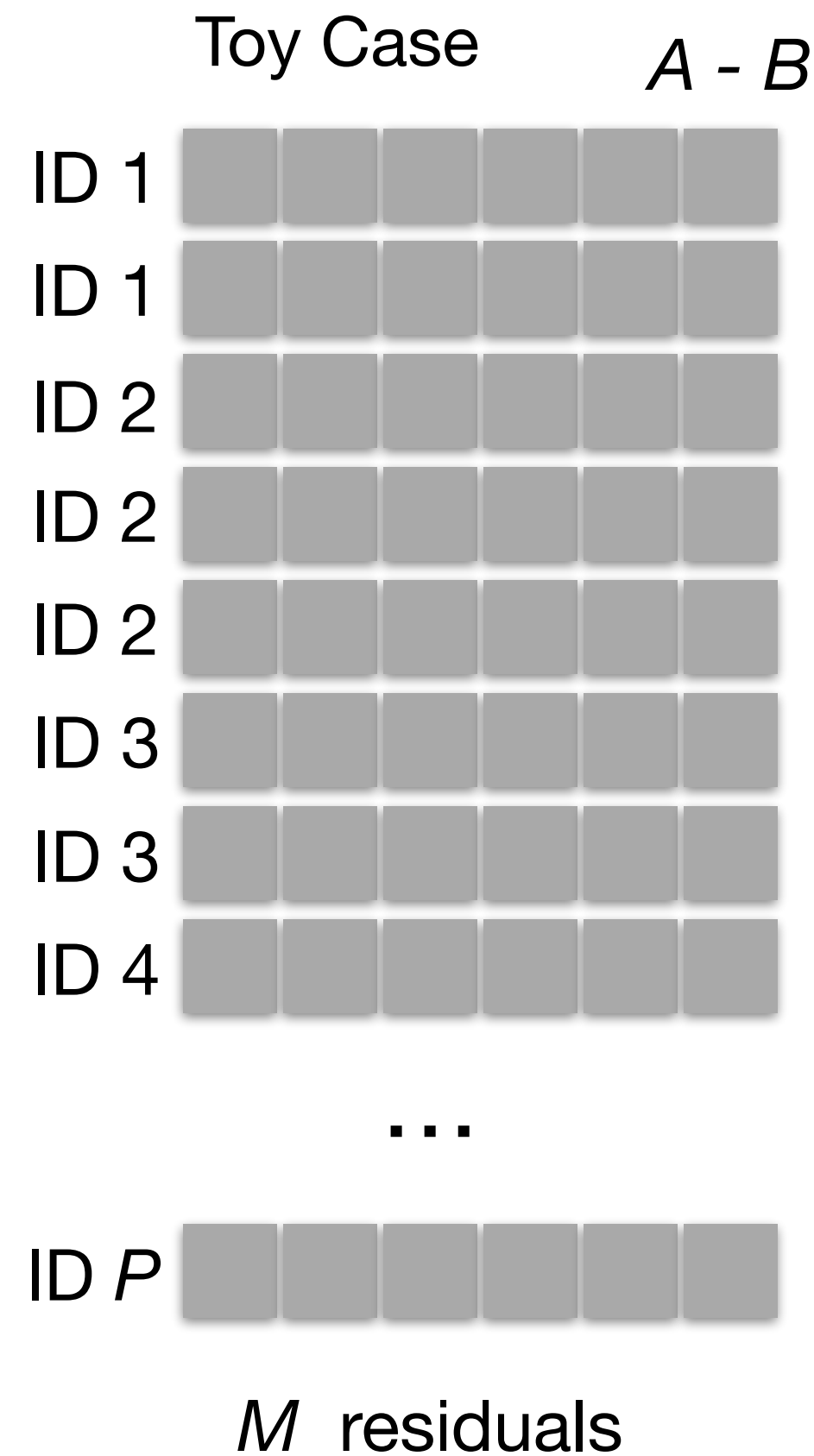


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

3. Reduce the dimensionality of residuals with **Product Quantization**.

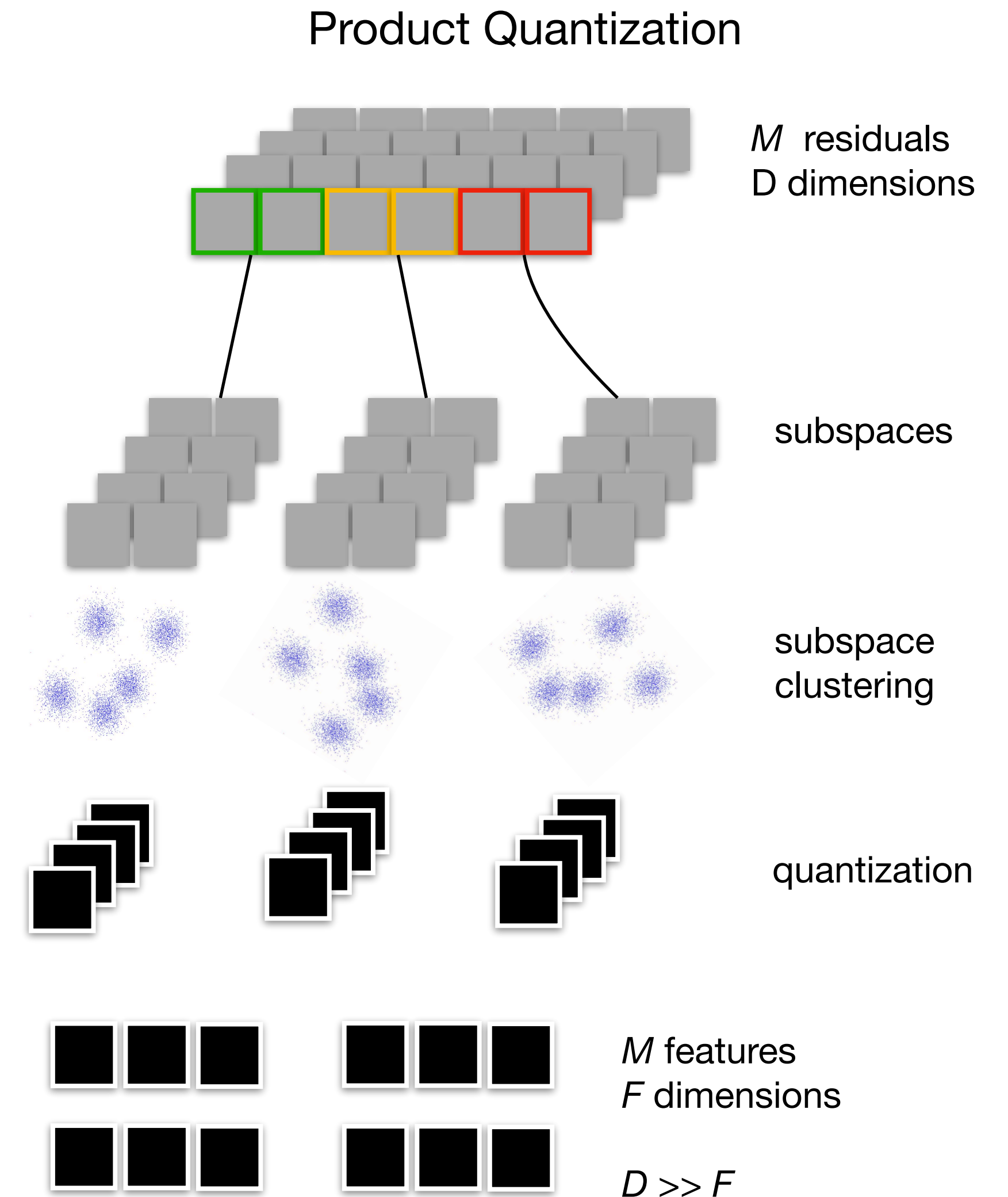
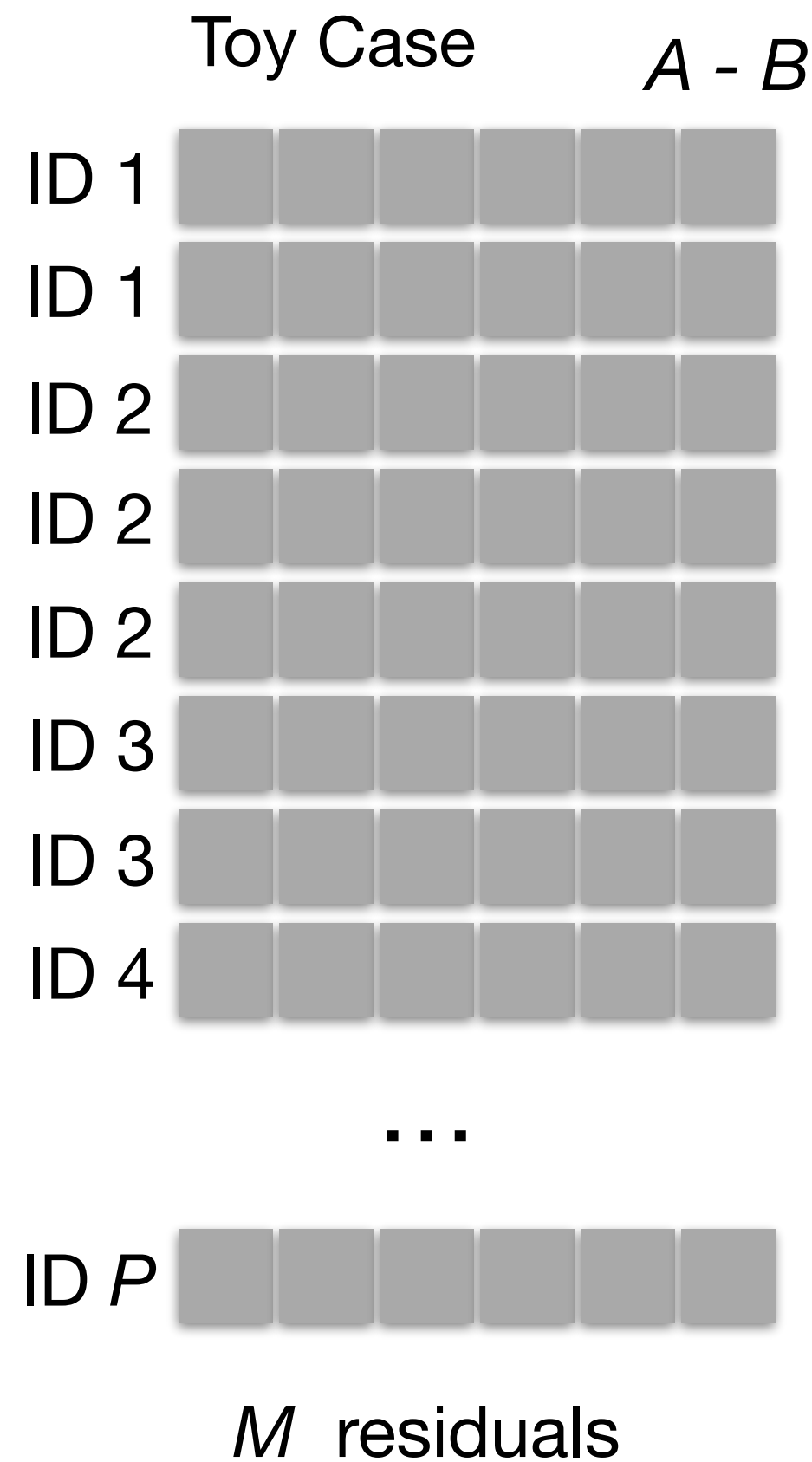


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

3. Reduce the dimensionality of residuals with **Product Quantization**.

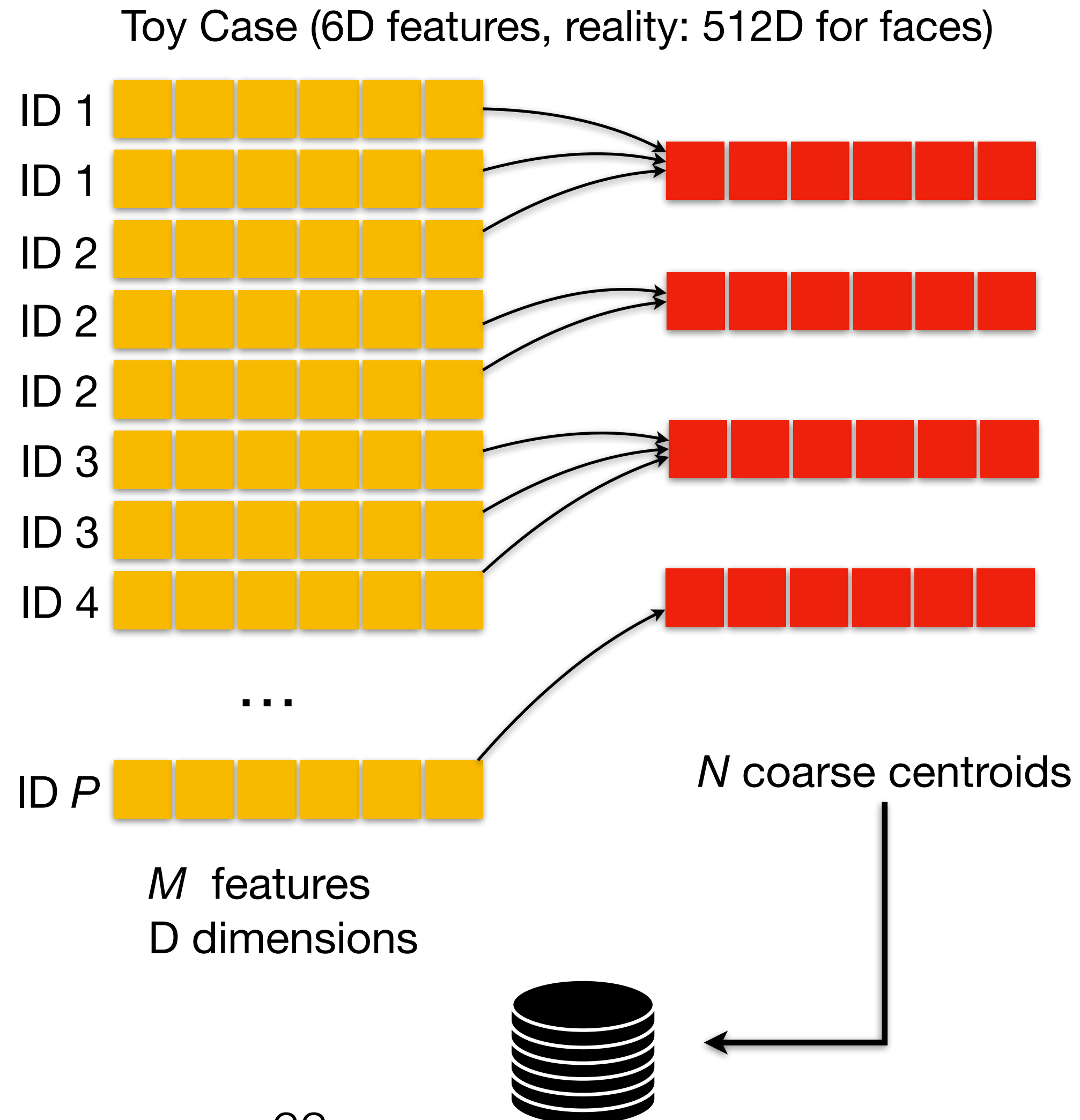


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

4. Append the product quantized residuals to an **inverted file index**.

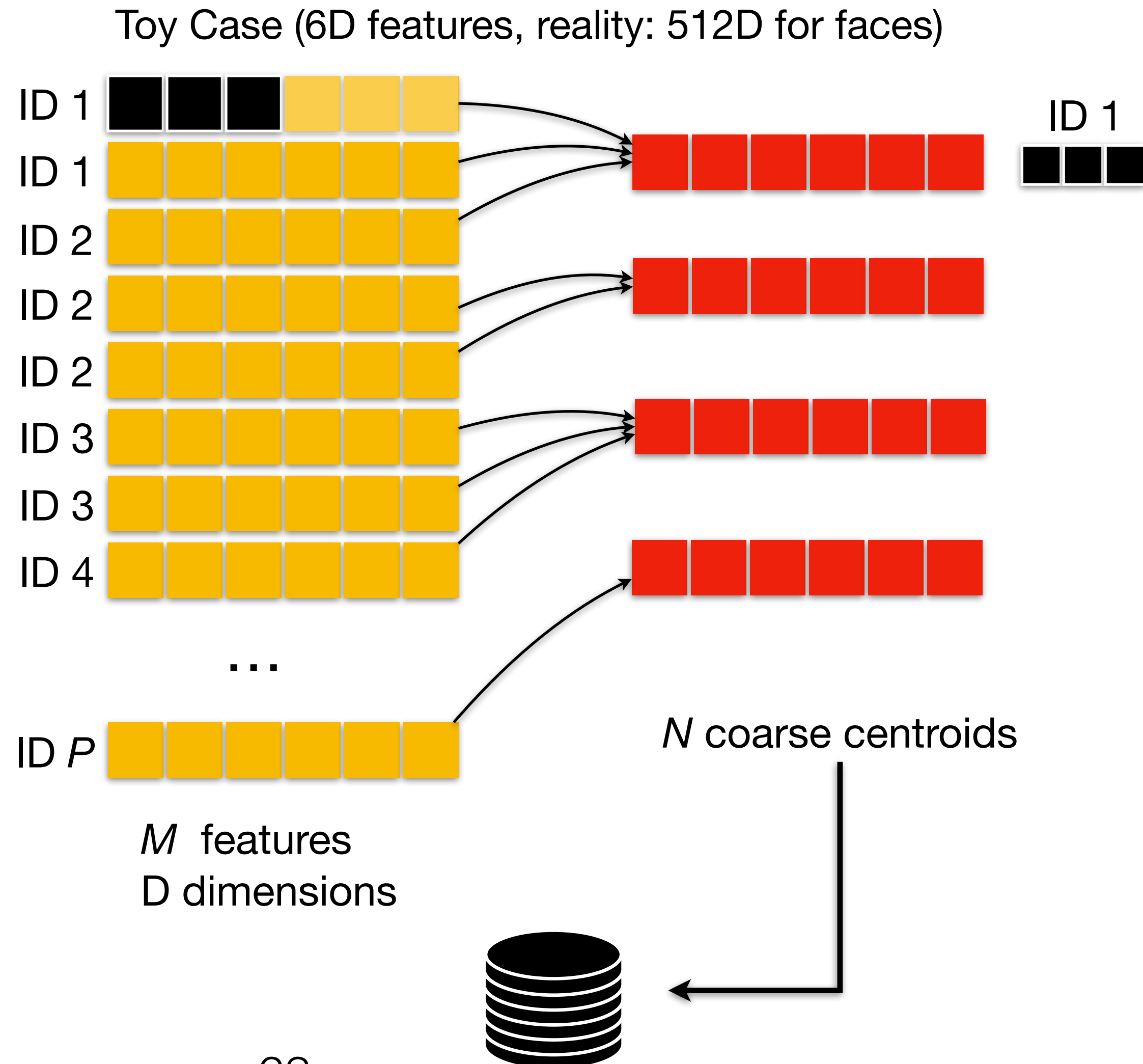


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

4. Append the product quantized residuals to an **inverted file index**.

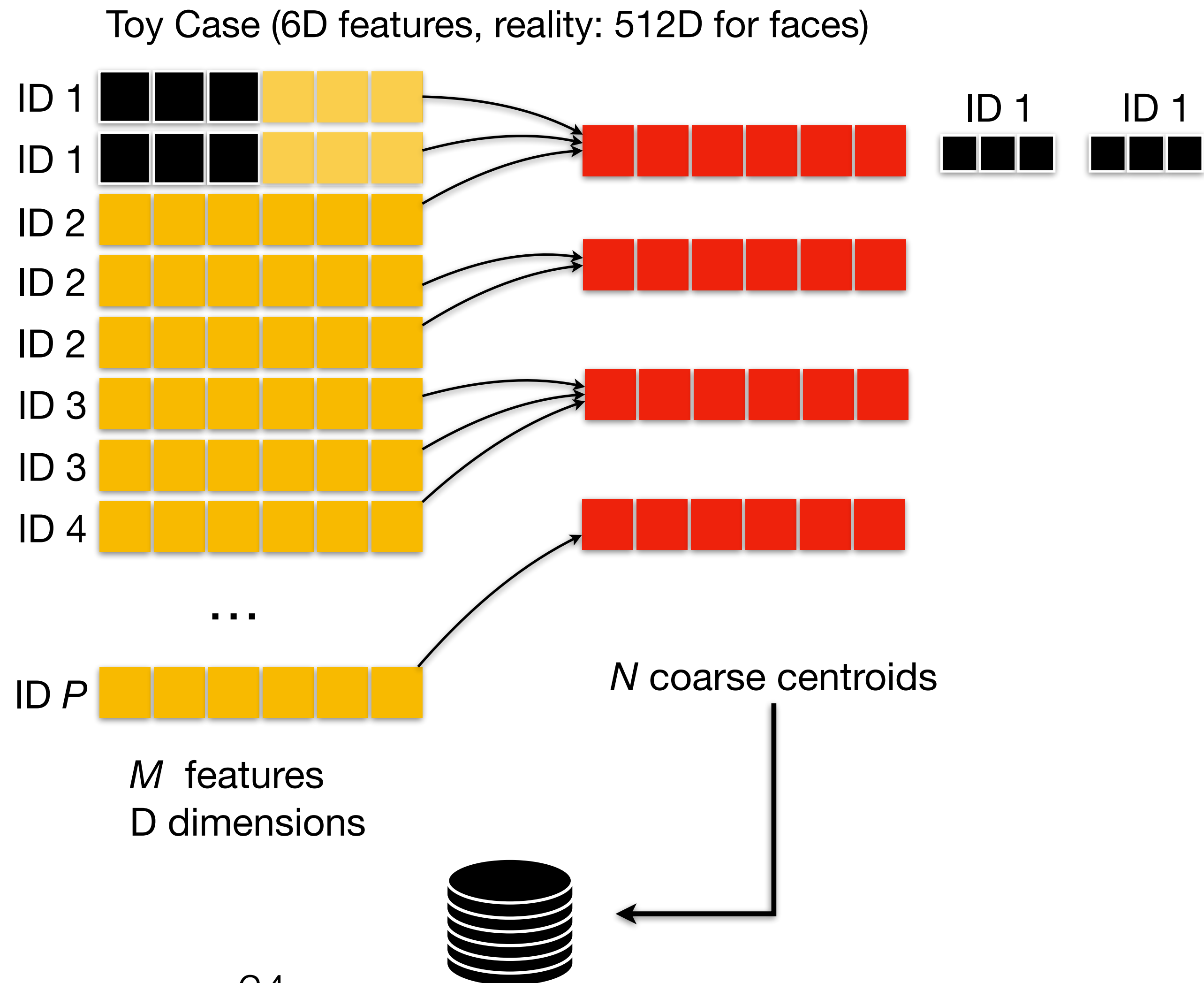


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

4. Append the product quantized residuals to an **inverted file index**.



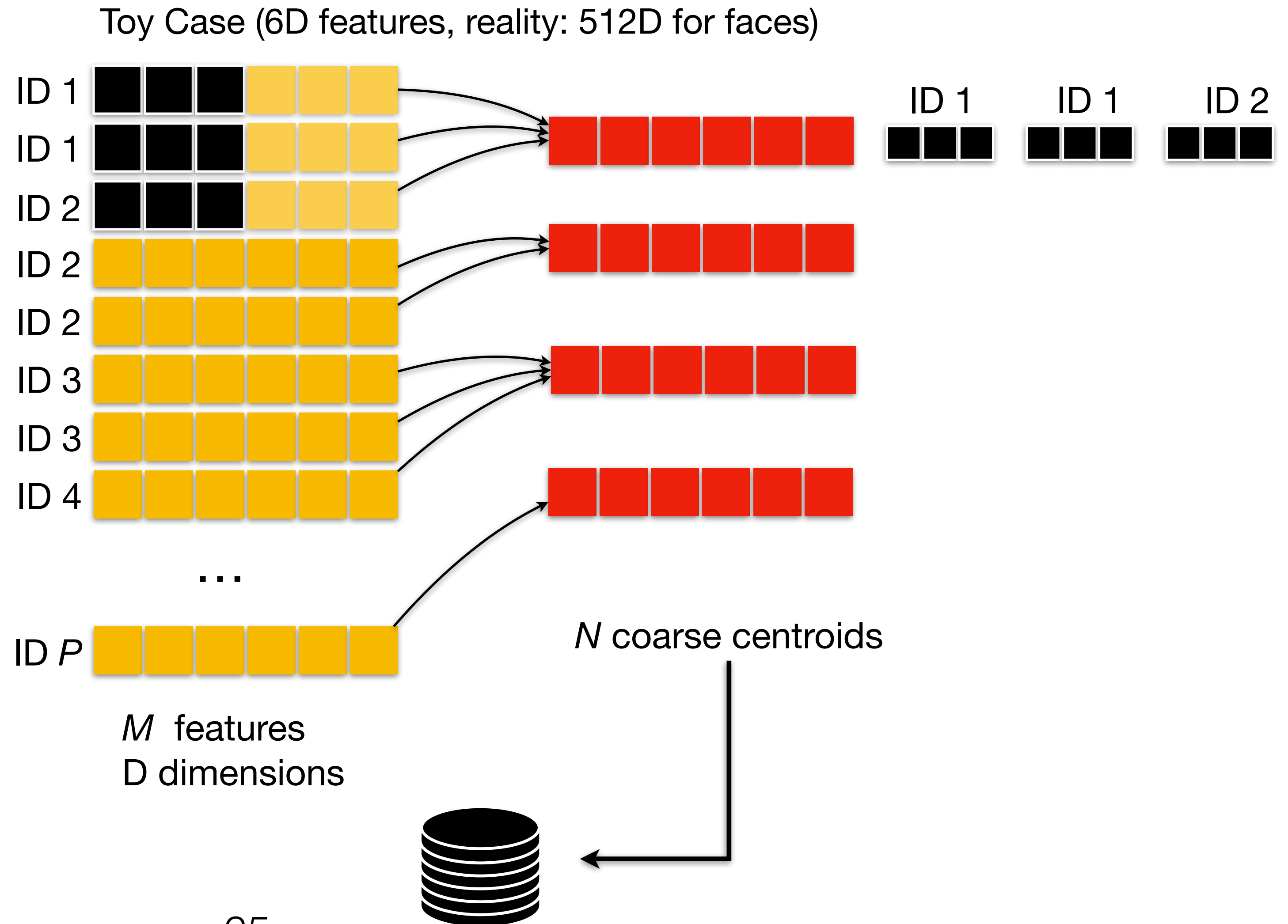


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

4. Append the product quantized residuals to an **inverted file index**.

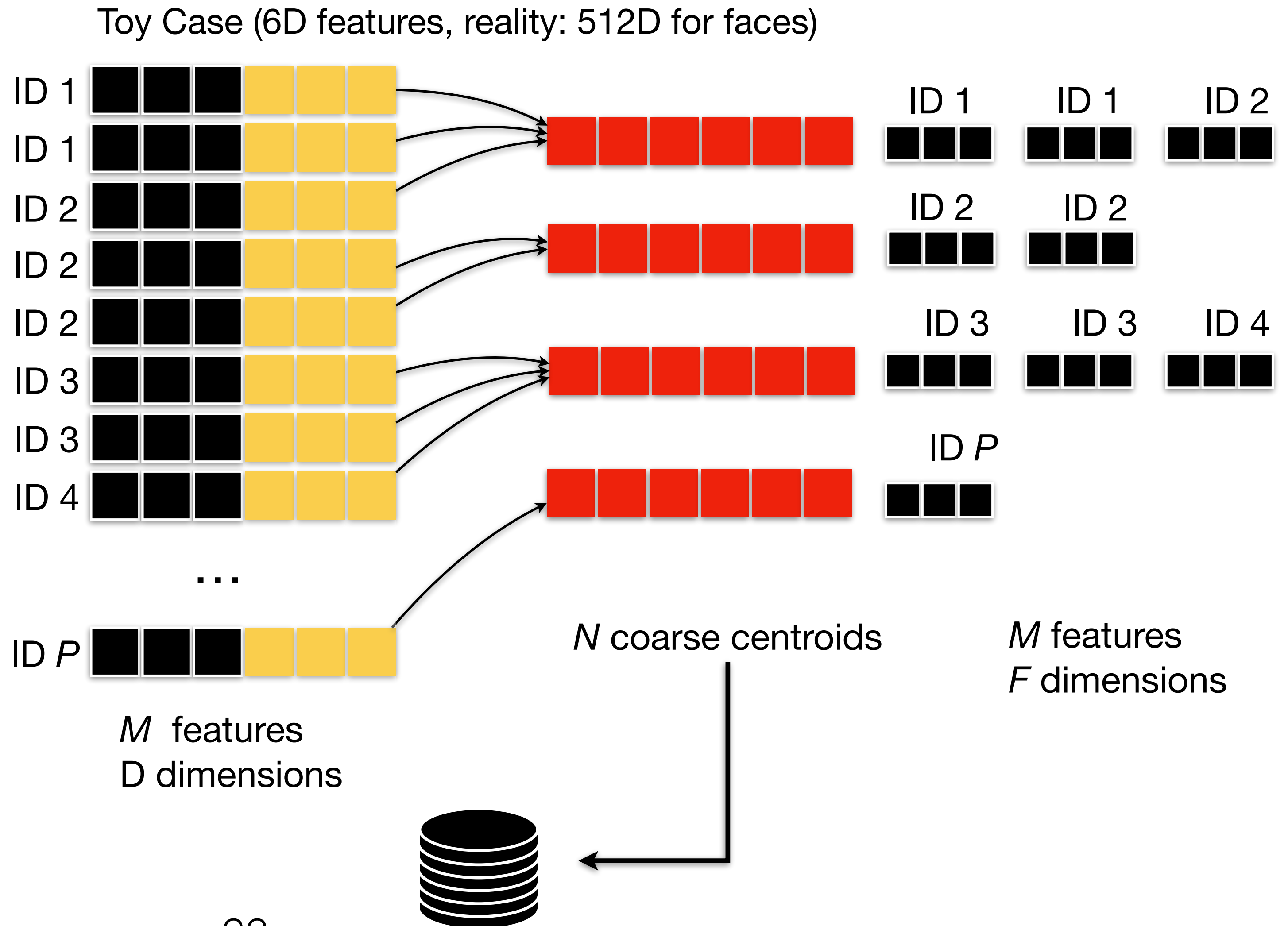


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

4. Append the product quantized residuals to an **inverted file index**.

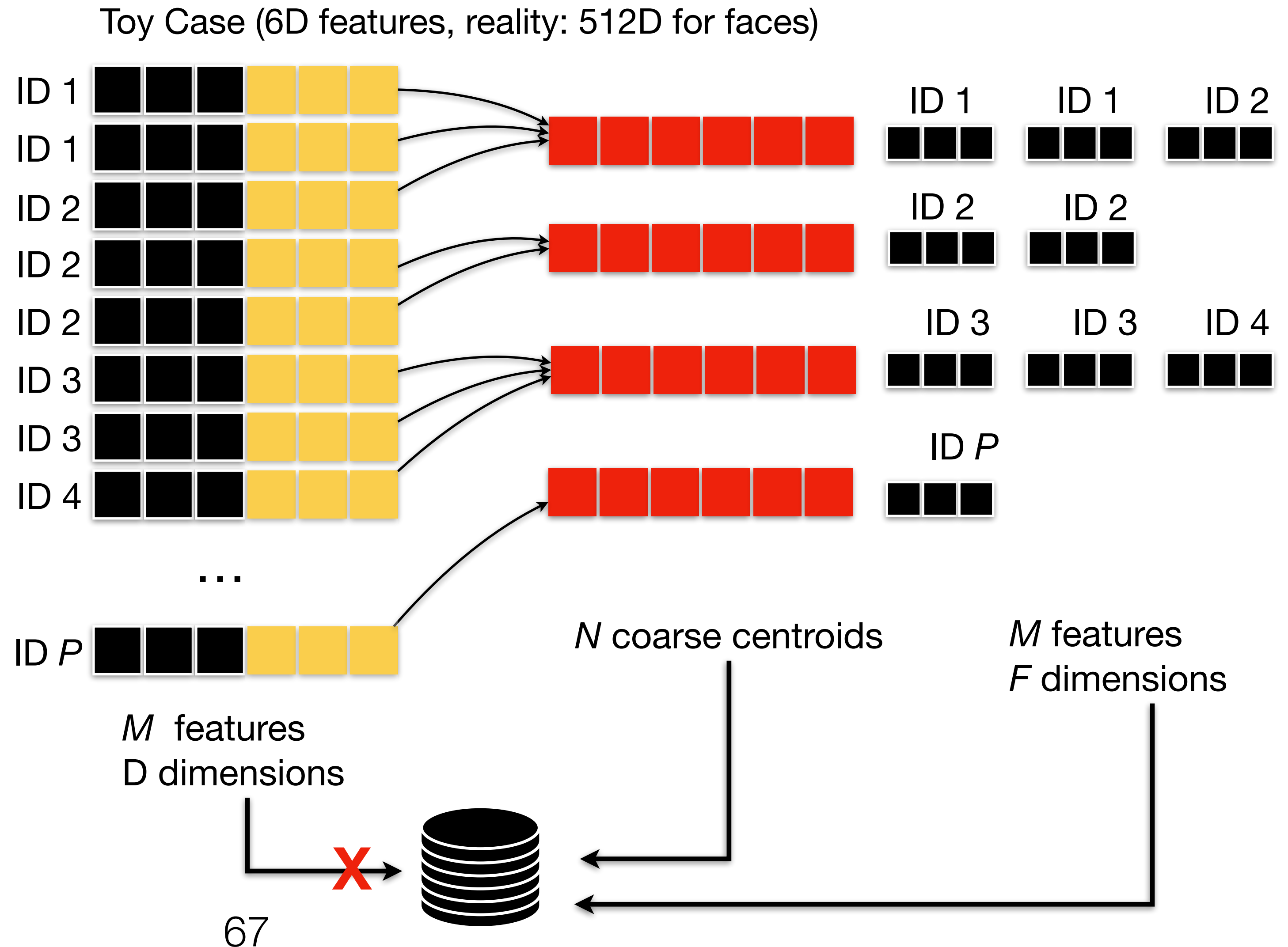


# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

4. Append the product quantized residuals to an **inverted file index**.



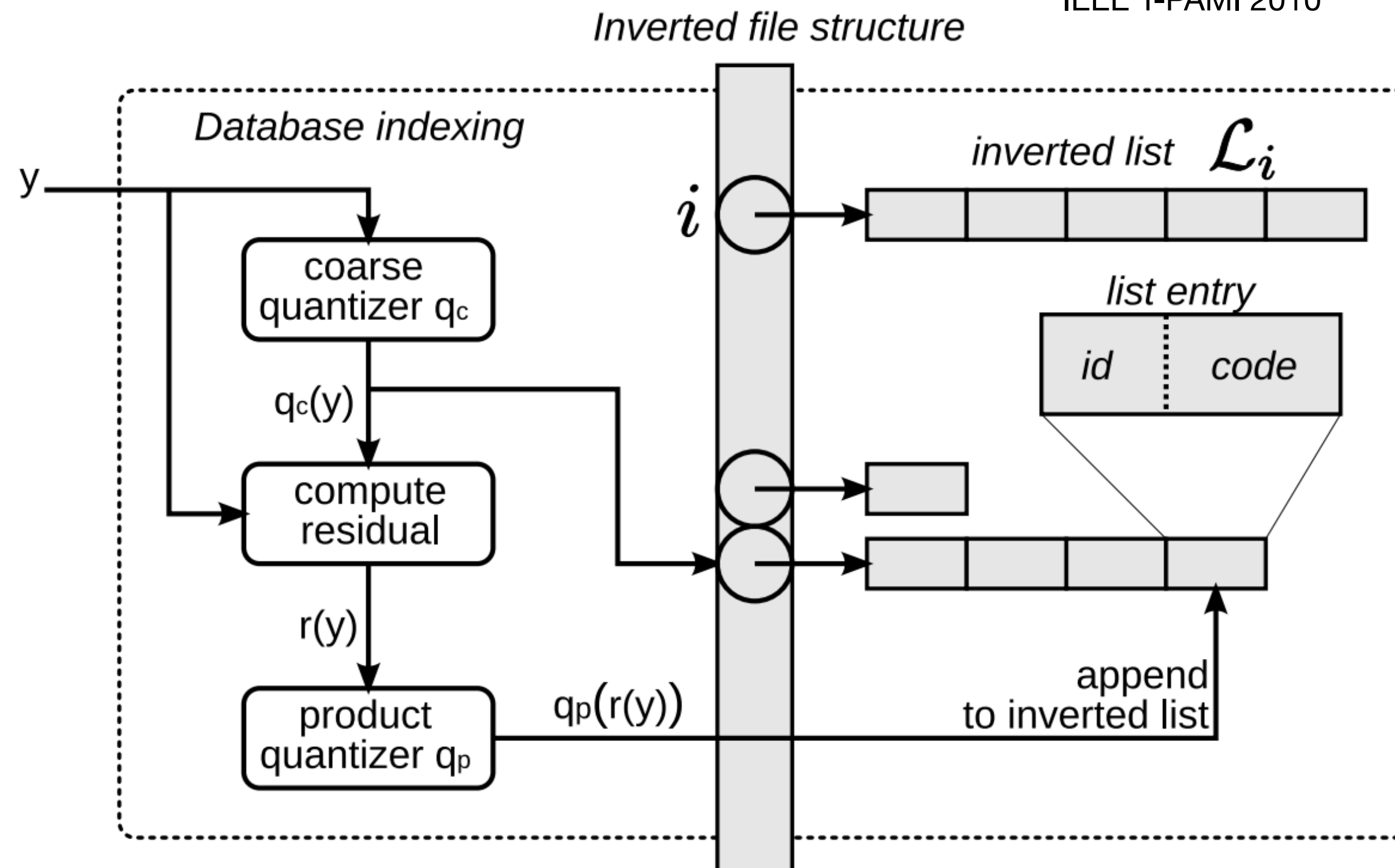
# Product Quantization

Source: Jegou et al.  
*Product quantization for nearest neighbor search*  
IEEE T-PAMI 2010

How to reduce size?

State-of-the-art feature indexing.

Usage example:  
**Indexing.**



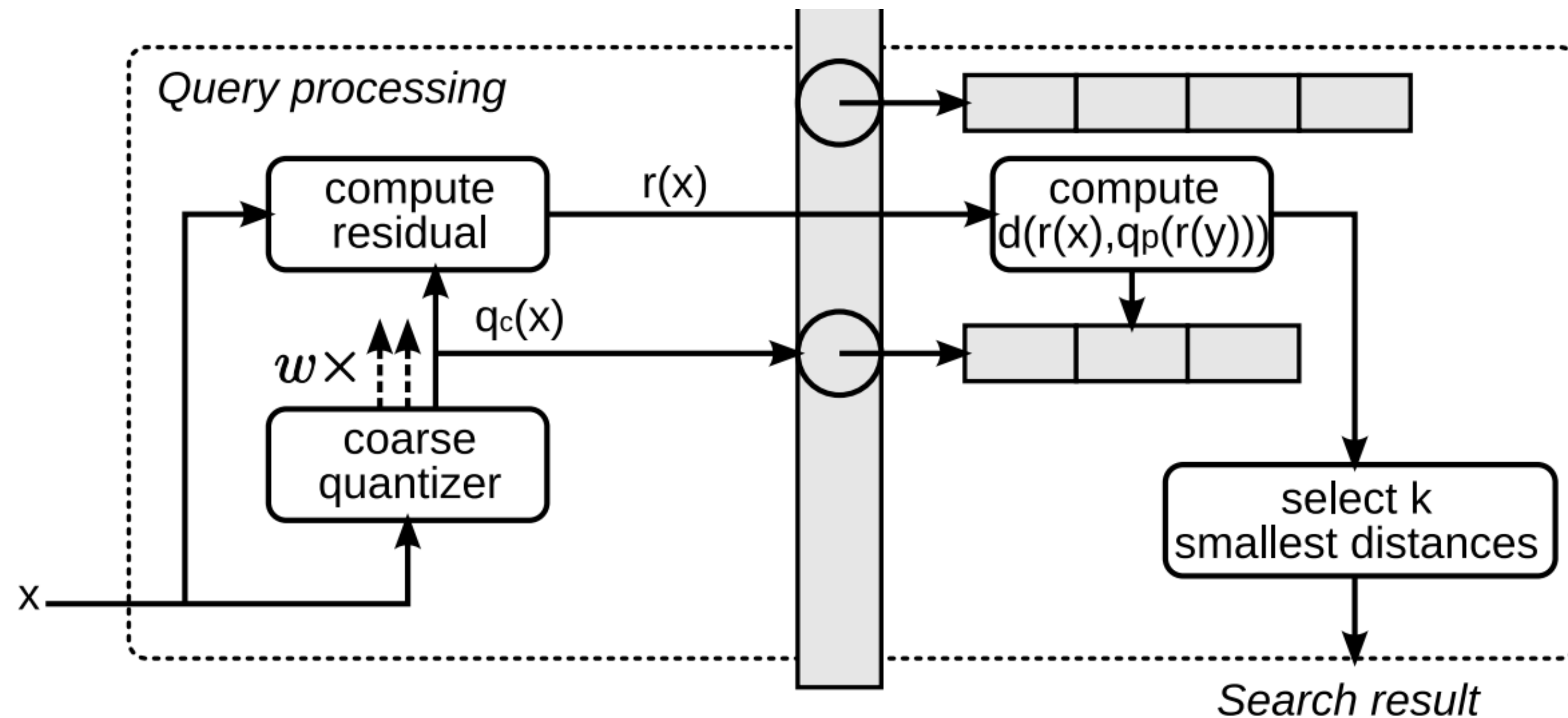
# Product Quantization

Source: Jegou et al.  
*Product quantization for nearest neighbor search*  
IEEE T-PAMI 2010

How to reduce size?

State-of-the-art feature indexing.

Usage example:  
**Retrieving k-nearest.**



# Product Quantization

How to reduce size?

State-of-the-art feature indexing.

Available implementation.

## [Faiss](#)

Faiss is a library for efficient similarity search and clustering of dense vectors. It contains algorithms that search in sets of vectors of any size, up to ones that possibly do not fit in RAM. It also contains supporting code for evaluation and parameter tuning. Faiss is written in C++ with complete wrappers for Python/numpy. Some of the most useful algorithms are implemented on the GPU. It is developed primarily at [Facebook AI Research](#).

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main 13 branches 17 tags Go to file Code

mdouze and facebook-github-bot Auto... 1806c6a yesterday 609 commits

.circleci	Add IndexNSGPQ and IndexNSGSQ (#2218)	last month
.github	Change default branch references from master ...	7 months ago
benchs	contrib clustering module (#2217)	last month
c_api	Generalize DistanceComputer for flat indexes (...)	11 days ago
cmake	Move from TravisCI to CircleCI (#1315)	2 years ago
conda	Fix packaging (#2121)	4 months ago
contrib	contrib clustering module (#2217)	last month
demos	Add NNDescent to faiss (#1654)	13 months ago
faiss	Automatic type conversions for Python API (#2...	yesterday
misc	Enable clang-format + autofix.	13 months ago
tests	Automatic type conversions for Python API (#2...	yesterday

About  
A library for efficient similarity search and clustering of dense vectors.  
[faiss.ai](#)  
Readme  
MIT License  
Code of conduct  
16.6k stars  
443 watching  
2.6k forks

Releases 13  
Faiss 1.7.2 Latest on Jan 10  
+ 12 releases

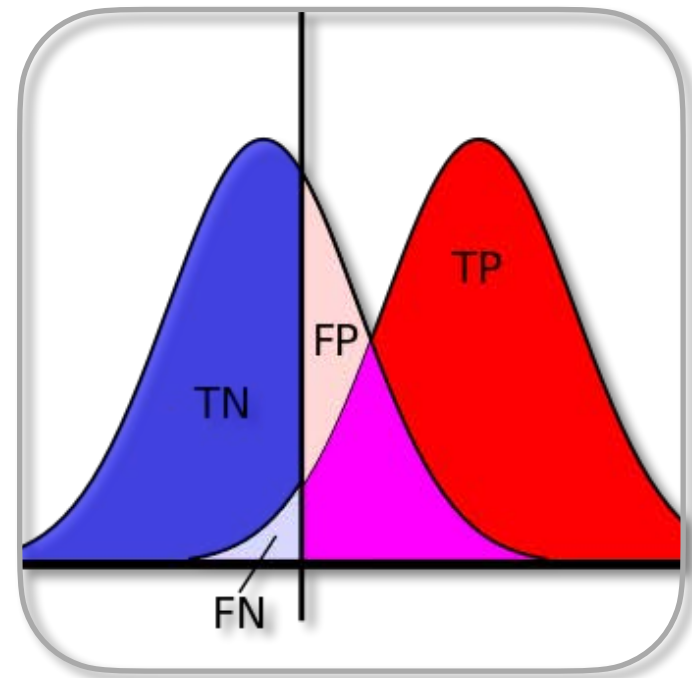
<https://github.com/facebookresearch/faiss>



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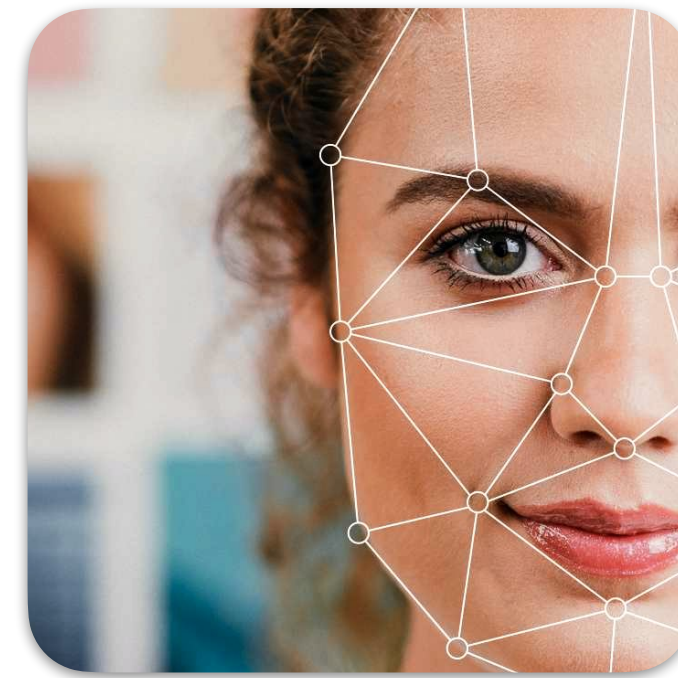
# What's Next?

## Content



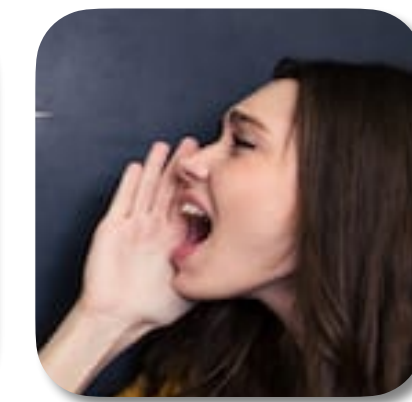
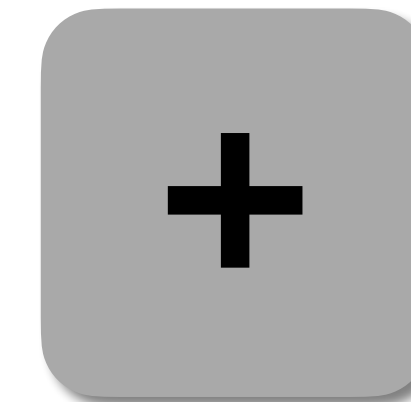
### Basics

Concepts  
Metrics  
Metric  
implementation



### Core Traits (3)

Concepts  
Baseline implementation  
Data collection  
Evaluation  
Attacks  
Assignments



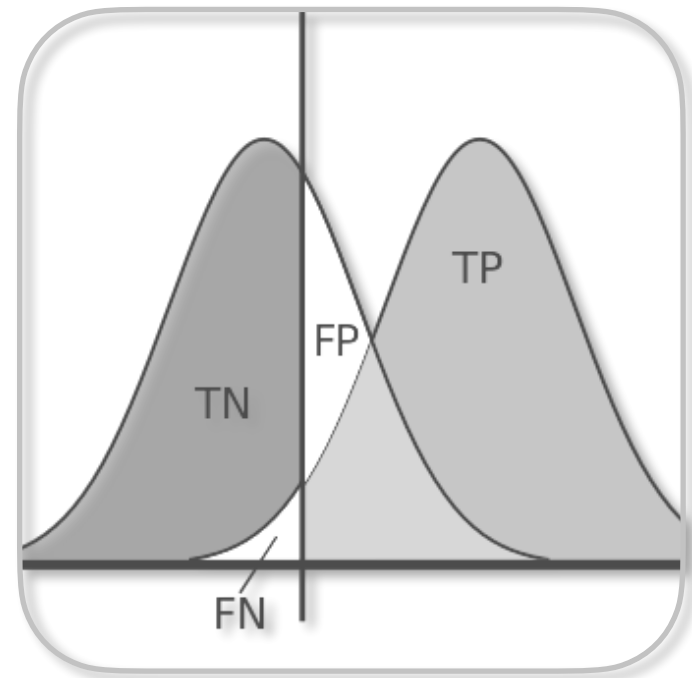
**Alternative Traits and Fusion Concepts**



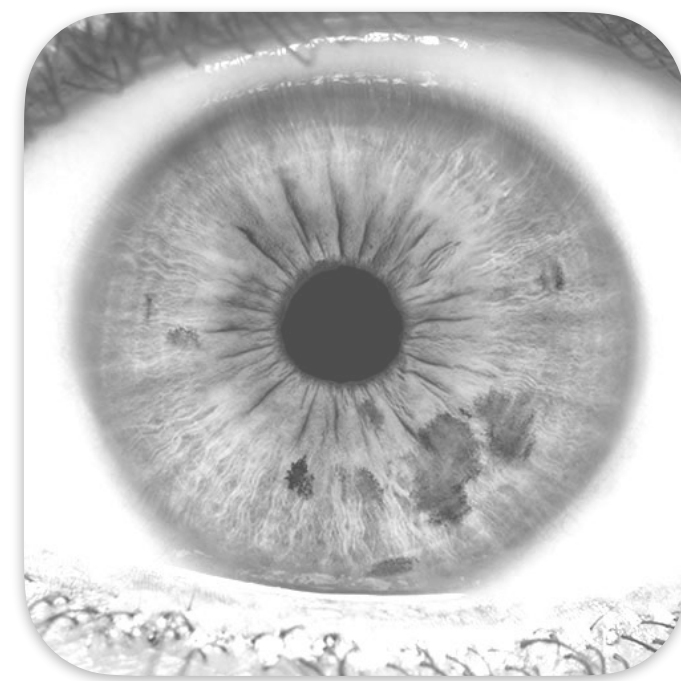
**Invited Talks (2)**  
State of the art  
Future work

# What's Next?

## Content



**Basics**  
Concepts  
Metrics  
Metric  
implementation



**Core Traits (3)**  
Concepts  
Baseline implementation  
Data collection  
Evaluation  
Attacks  
Assignments



**Alternative Traits and Fusion Concepts**



**Invited Talks (2)**  
State of the art  
Future work